Video games are all about change! How fast is this character moving? How does the score change if the player collects a coin? Where on the screen should we draw a castle?

We can break down a game into parts, and figure out which parts change and which ones stay the same. For example:

- Computers use coordinates to position a character on the screen. These coordinates specify how far from the left (x-coordinate) and the bottom (y-coordinate) a character should be. Negative values can be used to "hide" a character, by positioning them somewhere off the screen.

- When a character moves, those coordinates change by some amount. When the score goes up or down, it also changes by some amount.

From the computer's point of view, the whole game is just a bunch of numbers that are changing according to some equations. We might not be able to see those equations, but we can definitely see the effect they have when a character jumps on a mushroom, flies on a dragon, or mines for rocks!

Modern video games are incredibly complex, costing millions of dollars and several years to make, and relying on hundreds of programmers and digital artists to build them. But building even a simple game can give us a good idea of how the complex ones work!
Write down what you notice and wonder about the Ninja Cat game screenshot.
“Notices” should be statements, not questions. What stood out to you? What do you remember?

<table>
<thead>
<tr>
<th>What do you Notice?</th>
<th>What do you Wonder?</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Reverse Engineer a Video Game

What is changing in the game? The first example is filled in for you.

<table>
<thead>
<tr>
<th>Thing in the Game</th>
<th>What Changes About It?</th>
<th>More Specifically?</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dog</td>
<td>Position</td>
<td>x-coordinate</td>
</tr>
</tbody>
</table>

- Dog's position is changing, specifically its x-coordinate.
The coordinates for the PLAYER (NinjaCat) are: (__________,__________)

The coordinates for the DANGER (Dog) are: (__________,__________)

The coordinates for the TARGET (Ruby) are: (__________,__________)
Brainstorm Your Own Game

Created by: ________________________________

Background

Our game takes place: ____________________________

In space? The desert? A mall?

Player

The Player is a ________________________________
The Player moves only up and down.

Target

Your Player GAINS points when they hit The Target.
The Target is a ________________________________
The Target moves only to the left or right.

Danger

Your Player LOSES points when they hit The Danger.
The Danger is a ________________________________
The Danger moves only to the left or right.

Artwork/Sketches/Proof of Concept

Draw a rectangle representing your game screen, and label the bottom-left corner as the coordinate (0,0). Then label the other four corners. Then, in the rectangle, sketch a picture of your game!
Order of Operations is incredibly important when programming. To help us organize our math into something we can trust, we can diagram a math expression using the Circles of Evaluation. For example, the expression $1 - 4 \div 10 \times 7$ can be diagrammed as shown below.

To convert a Circle of Evaluation into Code, we walk through the circle from outside-in, moving left-to-right. We type an open parenthesis when we start a circle, and a close parenthesis when we end one. Once we’re in a circle, we first write the function at the top, then write the inputs from left to right. The circle above, for example, would be programmed as $(/ (- 1 4) (* 10 7))$. 

1−4÷10 × 7
For each expression on the left, finish the Circle of Evaluation on the right by filling in the blanks.

<table>
<thead>
<tr>
<th>Arithmetic Expression</th>
<th>Circle of Evaluation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$4 + 2 - \frac{10}{5}$</td>
<td>![Diagram for first expression]</td>
</tr>
<tr>
<td>$7 - 1 + 5 \times 8$</td>
<td>![Diagram for second expression]</td>
</tr>
<tr>
<td>$-15 \div 5 + -8$</td>
<td>![Diagram for third expression]</td>
</tr>
<tr>
<td>$(4 + (9 - 8)) \times 5$</td>
<td>![Diagram for fourth expression]</td>
</tr>
<tr>
<td>$6 \times 4 + \frac{9 - -6}{5}$</td>
<td>![Diagram for fifth expression]</td>
</tr>
<tr>
<td>$\frac{20}{6+4} - \frac{5 \times 9}{-12-3}$</td>
<td>![Diagram for sixth expression]</td>
</tr>
</tbody>
</table>
Matching Circles of Evaluation and Arithmetic Expressions

Draw a line from each Circle of Evaluation on the left to the corresponding arithmetic expression on the right.

<table>
<thead>
<tr>
<th>Circle of Evaluation</th>
<th>Arithmetic Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>A</td>
</tr>
<tr>
<td>2</td>
<td>B</td>
</tr>
<tr>
<td>3</td>
<td>C</td>
</tr>
<tr>
<td>4</td>
<td>D</td>
</tr>
<tr>
<td>5</td>
<td>E</td>
</tr>
</tbody>
</table>

A: \( \frac{1}{1} \) \( \div \) \( (1 \times 1) \) |
B: \( (1 + 1) - 1 \) |
C: \( (1 \times 1) \) \( \div \) \( 1 \) |
D: \( (1 + (1 - 1)) \times (1 + 1) \) |
E: \( (1 - 1) \times (1 + 1) \)
Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

<table>
<thead>
<tr>
<th>Arithmetic</th>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>(3 × 7) − (1 + 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3 − (1 + 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3 − (1 + (5 × 6))</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1 + (5 × 6)) − 3</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
## Completing Partial Code from Circles of Evaluation

For each Circle of Evaluation on the left, finish the Code on the right by filling in the blanks.

<table>
<thead>
<tr>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1" alt="Circle 1" /></td>
<td>$(+ \underline{\hspace{1cm}} (+ 6 \underline{\hspace{1cm}}))$</td>
</tr>
<tr>
<td><img src="image2" alt="Circle 2" /></td>
<td>$(\underline{\hspace{1cm}} (+ \underline{\hspace{1cm}} 13) (\underline{\hspace{1cm}} \underline{\hspace{1cm}} 4))$</td>
</tr>
<tr>
<td><img src="image3" alt="Circle 3" /></td>
<td>$(\underline{\hspace{1cm}} (+ \underline{\hspace{1cm}} 4) \underline{\hspace{1cm}})$</td>
</tr>
<tr>
<td><img src="image4" alt="Circle 4" /></td>
<td>$(\underline{\hspace{1cm}} \underline{\hspace{1cm}} 13 (\underline{\hspace{1cm}} 7 (\underline{\hspace{1cm}} 2 -4)))$</td>
</tr>
<tr>
<td><img src="image5" alt="Circle 5" /></td>
<td>$(\underline{\hspace{1cm}} (\underline{\hspace{1cm}} (\underline{\hspace{1cm}} 8 1) 3) (\underline{\hspace{1cm}} 5 3))$</td>
</tr>
<tr>
<td><img src="image6" alt="Circle 6" /></td>
<td>$(/ (+ \underline{\hspace{1cm}} \underline{\hspace{1cm}}) (+ \underline{\hspace{1cm}} \underline{\hspace{1cm}}))$</td>
</tr>
</tbody>
</table>
### Matching Circles of Evaluation & Code

Draw a line from each Circle of Evaluation on the left to the corresponding Code on the right.

<table>
<thead>
<tr>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Circle 1" /></td>
<td>1 A (*) (- 1 (+ 1 1)) 1</td>
</tr>
<tr>
<td><img src="image2.png" alt="Circle 2" /></td>
<td>2 B (*) (- 1 1) (+ 1 1)</td>
</tr>
<tr>
<td><img src="image3.png" alt="Circle 3" /></td>
<td>3 C (*) (+ 1 1) (- (+ 1 1) 1)</td>
</tr>
<tr>
<td><img src="image4.png" alt="Circle 4" /></td>
<td>4 D (- (+ 1 1) 1)</td>
</tr>
<tr>
<td><img src="image5.png" alt="Circle 5" /></td>
<td>5 E (+ (- 1 1) 1)</td>
</tr>
</tbody>
</table>
Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

<table>
<thead>
<tr>
<th>Arithmetic</th>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>6 \times 8 + (7 - 23)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>18 \div 2 + 24 \times 4 - 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>22 - 7 \div 3 + 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>24 \div 4 \times 2 - 6 + 20 \times 2</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

<table>
<thead>
<tr>
<th>Arithmetic</th>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\frac{16 + 3^2}{\sqrt{49 - 2}}$</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>$45 - 9 \times (3 + (2 - 4)) - 7$</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>$50 \div 5 \times 2 - ((3 + 4) \times 2 - 5)$</td>
<td></td>
</tr>
</tbody>
</table>
Introduction to Programming

The Editor is a software program we use to write Code. Our Editor allows us to experiment with Code on the right-hand side, in the Interactions Area. For Code that we want to keep, we can put it on the left-hand side in the Definitions Area. Clicking the "Run" button causes the computer to re-read everything in the Definitions Area and erase anything that was typed into the Interactions Area.

Data Types

Programming languages involve different data types, such as Numbers, Strings, Booleans, and even Images.

- **Numbers** are values like 1, 0.4, 1/3, and -8261.003.
  - Numbers are usually used for quantitative data and other values are usually used as categorical data.

- **Strings** are values like "Emma", "Rosanna", "Jen and Ed", or even "08/28/1980".
  - All strings must be surrounded in quotation marks.

- **Booleans** are either true or false.

All values evaluate to themselves. The program 42 will evaluate to 42, the String "Hello" will evaluate to "Hello", and the Boolean false will evaluate to false.

Operators

Operators (like +, -, *, <, etc.) are treated the same way as functions: after all, they have inputs and outputs and obey the same rules!

Applying Functions

Applying functions (and operators!) works much the way it does in math. Every function has a name, takes some inputs, and produces some output. The function name is written first, followed by a list of arguments.

- In math this could look like \( f(5) \) or \( g(10, 4) \).
- In WeScheme, these examples would be written as \((f 5)\) and \((g 10 4)\).
- Applying the operator + to the inputs 1 and 2 would look like \((+ 1 2)\).
- Applying a function to make images would look like \((\text{star} 50 \ "\text{solid}\" \ "\text{red}\")\).
- There are many other functions, for example \(\text{num-sqr}, \text{num-sqrt}, \text{triangle}, \text{square}, \text{string-repeat}\), etc.

Functions have contracts, which help explain how a function should be used. Every contract has three parts:

- The Name of the function - literally, what it's called.
- The Domain of the function - what types of values the function consumes, and in what order.
- The Range of the function - what type of value the function produces.
Numbers and Strings

Make sure you've loaded the wescheme.org editor, clicked "Run", and are working in the Interactions Area.

Numbers

1) Try typing 42 into the Interactions Area and hitting "Enter". What is the largest number the editor can handle?

2) Try typing 8.5. Then try typing .5. Then try clicking on the answer. Experiment with other decimals. Explain what you understand about how decimals work in this programming language.

3) What happens if you try a fraction like 1/3?

4) Try writing negative integers, fractions and decimals.

Strings

String values are always in quotes.

5) Is 42 the same as "42"? Why or why not? Write your answer below:

6) Try typing your name (in quotes!).
7) Try typing a sentence like "I'm excited to learn to code!" (in quotes!).
8) Try typing your name with the opening quote, but without the closing quote. Read the error message!
9) Now try typing your name without any quotes. Read the error message!
10) Explain what you understand about how strings work in this programming language.
Boolean-producing expressions are yes-or-no questions and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down your prediction in the blanks provided and then type the code into the interactions area to see what it returns.

<table>
<thead>
<tr>
<th>Prediction:</th>
<th>Computer Returns:</th>
<th>Prediction:</th>
<th>Computer Returns:</th>
</tr>
</thead>
<tbody>
<tr>
<td>1) (&lt;= 3 4)</td>
<td></td>
<td>2) (string&gt;? &quot;a&quot; &quot;b&quot;)</td>
<td></td>
</tr>
<tr>
<td>3) (= 3 2)</td>
<td></td>
<td>4) (string&lt; &quot;a&quot; &quot;b&quot;)</td>
<td></td>
</tr>
<tr>
<td>5) (&lt; 2 4)</td>
<td></td>
<td>6) (string= &quot;a&quot; &quot;b&quot;)</td>
<td></td>
</tr>
<tr>
<td>7) (&gt;= 5 5)</td>
<td></td>
<td>8) (string&lt;=? &quot;a&quot; &quot;a&quot;)</td>
<td></td>
</tr>
<tr>
<td>9) (&gt;= 4 6)</td>
<td></td>
<td>10) (string&gt;=? &quot;a&quot; &quot;a&quot;)</td>
<td></td>
</tr>
<tr>
<td>11) (&lt;&gt; 3 3)</td>
<td></td>
<td>12) (string&lt;&gt;? &quot;a&quot; &quot;b&quot;)</td>
<td></td>
</tr>
</tbody>
</table>

13) In your own words, describe what < does.

14) In your own words, describe what >= does.

15) In your own words, describe what <> does.

<table>
<thead>
<tr>
<th>Prediction:</th>
<th>Computer Returns:</th>
<th>Prediction:</th>
<th>Computer Returns:</th>
</tr>
</thead>
<tbody>
<tr>
<td>16) (string=? &quot;a tree&quot; &quot;trees&quot;)</td>
<td></td>
<td>17) (string=? &quot;tree&quot; &quot;tree&quot;)</td>
<td></td>
</tr>
<tr>
<td>18) (string-contains? &quot;catnap&quot; &quot;cat&quot;)</td>
<td></td>
<td>19) (string-contains? &quot;cat&quot; &quot;catnap&quot;)</td>
<td></td>
</tr>
</tbody>
</table>

20) How many Numbers are there in the entire universe? 
21) How many Strings are there in the entire universe? 
22) How many Images are there in the entire universe? 
23) How many Booleans are there in the entire universe?
Applying Functions

Type this line of code into the interactions area and hit "Enter":

(triangle 50 "solid" "red")

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>What is the name of this function?</td>
</tr>
<tr>
<td>2</td>
<td>What did the expression evaluate to?</td>
</tr>
<tr>
<td>3</td>
<td>How many arguments does triangle expect?</td>
</tr>
<tr>
<td>4</td>
<td>What data type does the triangle function produce? (Numbers? Strings? Booleans?)</td>
</tr>
</tbody>
</table>

Catching Bugs

5) (triangle 20 "solid")
   triangle: expects 3 arguments, but given 2: 20 solid at: line 1, column 0, in <interactions>
   Can you spot the mistake?

6) (triangle "solid" "red" 20)
   triangle: expects a non-negative number as 1st argument, but given: solid; other arguments were: red 20 at: line 1, column 0, in <interactions>
   Can you spot the mistake?

7) (triangle 20 40 "solid" "red")
   triangle: expects 3 arguments, but given 4: 20 40 solid red at: line 1, column 0, in <interactions>
   Can you spot the mistake?

8) (triangle 20 solid "red")
   solid: this variable is not defined at: line 1, column 0, in <interactions>
   Can you spot the mistake?

9) (triangle 20 "striped" "red")
   triangle: expects a style ("solid" / "outline") or an opacity value [0-255] as 2nd argument, but given: "striped"; other arguments were: 20 "red" at: line 1, column 0, in <interactions>
   Can you spot the mistake?
Consider the following contract:

\texttt{is-beach-weather :: Number, String -> Boolean}

1) What is the **Name** of this function? 
2) How many arguments are in this function's **Domain**? 
3) What is the **type** of this function's **first argument**? 
4) What is the **type** of this function's **second argument**? 
5) What is the **Range** of this function? 
6) Circle the expression below that shows the correct application of this function, based on its contract.

A. \texttt{(is-beach-weather 70 90)}
B. \texttt{(is-beach-weather 80 100 "cloudy")}
C. \texttt{(is-beach-weather "sunny" 90)}
D. \texttt{(is-beach-weather 90 "stormy weather")}

Consider the following contract:

\texttt{cylinder :: Number, Number, String -> Image}

7) What is the **Name** of this function? 
8) How many arguments are in this function's **Domain**? 
9) What is the **type** of this function's **first argument**? 
10) What is the **type** of this function's **second argument**? 
11) What is the **type** of this function's **third argument**? 
12) What is the **Range** of this function? 
13) Circle the expression below that shows the correct application of this function, based on its contract.

A. \texttt{(cylinder "red" 10 60)}
B. \texttt{(cylinder 30 "green")}
C. \texttt{(cylinder 10 25 "blue")}
D. \texttt{(cylinder 14 "orange" 25)}
Matching Expressions and Contracts

Match the contract (left) with the expression described by the function being used (right).

<table>
<thead>
<tr>
<th>Contract</th>
<th>Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>; make-id :: String, Number -&gt; Image</td>
<td>A (make-id &quot;Savannah&quot; &quot;Lopez&quot; 32)</td>
</tr>
<tr>
<td>; make-id :: String, Number, String -&gt; Image</td>
<td>B (make-id &quot;Pilar&quot; 17)</td>
</tr>
<tr>
<td>; make-id :: String -&gt; Image</td>
<td>C (make-id &quot;Akemi&quot; 39 &quot;red&quot;)</td>
</tr>
<tr>
<td>; make-id :: String, String -&gt; Image</td>
<td>D (make-id &quot;Raissa&quot; &quot;McCracken&quot;)</td>
</tr>
<tr>
<td>; make-id :: String, String, Number -&gt; Image</td>
<td>E (make-id &quot;von Einsiedel&quot;)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Contract</th>
<th>Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>; is-capital :: String, String -&gt; Boolean</td>
<td>A (show-pop &quot;Juneau&quot; &quot;AK&quot; 31848)</td>
</tr>
<tr>
<td>; is-capital :: String, String, String -&gt; Boolean</td>
<td>B (show-pop &quot;San Juan&quot; 395426)</td>
</tr>
<tr>
<td>; show-pop :: String, Number -&gt; Image</td>
<td>C (is-capital &quot;Accra&quot; &quot;Ghana&quot;)</td>
</tr>
<tr>
<td>; show-pop :: String, String, Number -&gt; Image</td>
<td>D (show-pop 3751351 &quot;Oklahoma&quot;)</td>
</tr>
<tr>
<td>; show-pop :: Number, String -&gt; Number</td>
<td>E (is-capital &quot;Albany&quot; &quot;NY&quot; &quot;USA&quot;)</td>
</tr>
</tbody>
</table>
Using Contracts

Use the contracts to write expressions to generate images similar to those pictured.

**ellipse**: Number, Number, String, String -> Image

What changes with the first number?

What about the shape changes with the second Number?

Write an expression using ellipse to produce a circle.

**regular-polygon**: Number, Number, String, String -> Image

What changes with the first Number?

What about the shape changes with the second Number?

Use regular-polygon to write an expression for a square!

How would you describe a regular polygon to a friend?
1) What kind of triangle does the triangle function produce?

There are lots of other kinds of triangles! And WeScheme has lots of other functions that make triangles!

```wescheme
triangle :: (size:: Number, style :: String, color :: String) -> Image
right-triangle :: (base::Number, height::Number, style::String, color::String) -> Image
isosceles-triangle :: (leg::Number, angle::Number, style::String, color::String) -> Image
```

2) Why do you think triangle only needs one number, while right-triangle and isosceles-triangle need two numbers and triangle/sas needs three?

3) Write right-triangle expressions for the images below. One argument for each should be 100.

```

```

4) What do you think the numbers in right-triangle represent?

5) Write isosceles-triangle expressions for the images below. 1 argument for each should be 100.

```

```

6) What do you think the numbers in isosceles-triangle represent?

7) Write 2 expressions that would build right-isosceles triangles. Use right-triangle for one expression and isosceles-triangle for the other expression.
Using the detailed contract above, match each image to the expression that describes it.

<table>
<thead>
<tr>
<th>Image</th>
<th>Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Image 1" /></td>
<td>(radial-star 5 50 200 &quot;solid&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image2.png" alt="Image 2" /></td>
<td>(radial-star 7 100 200 &quot;solid&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image3.png" alt="Image 3" /></td>
<td>(radial-star 7 100 200 &quot;outline&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image4.png" alt="Image 4" /></td>
<td>(radial-star 10 150 200 &quot;solid&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image5.png" alt="Image 5" /></td>
<td>(radial-star 10 20 200 &quot;solid&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image6.png" alt="Image 6" /></td>
<td>(radial-star 100 20 200 &quot;solid&quot; &quot;black&quot;)</td>
</tr>
<tr>
<td><img src="image7.png" alt="Image 7" /></td>
<td>(radial-star 100 100 200 &quot;outline&quot; &quot;black&quot;)</td>
</tr>
</tbody>
</table>
What's on your mind?
Diagramming Function Composition

For each function composition diagrammed below, translate it into the equivalent Circle of Evaluation for Order of Operations. Then write expressions for both versions of the Circles of Evaluation, and evaluate them for \( x = 4 \). The first one has been completed for you.

<table>
<thead>
<tr>
<th>Function Composition</th>
<th>Order of Operations</th>
<th>Translate &amp; Evaluate</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f(x) = 3x )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( g(x) = x + 6 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( h(x) = x - 1 )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

1)  

\[
\begin{align*}
\text{Composition:} & \quad (h \ (g \ (f \ x))) \\
\text{Operations:} & \quad (- \ (+ \ (* \ 3 \ x) \ 6) \ 1) \\
\text{Evaluate for } x = 4 & \quad h(g(f(4))) = 17
\end{align*}
\]

2)  

Composition: 

Operations: 

Evaluate for \( x = 4 \) 

3)  

Composition: 

Operations: 

Evaluate for \( x = 4 \) 

4)  

Composition: 

Operations: 

Evaluate for \( x = 4 \) 

\( f :: \text{Number} \rightarrow \text{Number} \) Consumes a number, multiplies by 3 to produce the result

\( g :: \text{Number} \rightarrow \text{Number} \) Consumes a number, adds six to produce the result

\( h :: \text{Number} \rightarrow \text{Number} \) Consumes a number, subtracts one to produce the result
1) Draw a Circle of Evaluation and write the Code for a **solid, green star, size 50**.  
**Circle of Evaluation:**

```
Code: ________________________________________________________________
```

Using the star described above as the **original**, draw the Circles of Evaluation and write the Code for each exercise below.

2) A solid, green star, that is triple the size of the original (using \textit{scale})  
**Circle of Evaluation:**

```
Code: ________________________________________________________________
```

3) A solid, green star, that is half the size of the original (using \textit{scale})  
**Circle of Evaluation:**

```
Code: ________________________________________________________________
```

4) A solid, green star of size 50 that has been rotated 45 degrees \textit{counter-clockwise}  
**Circle of Evaluation:**

```
Code: ________________________________________________________________
```

5) A solid, green star that is 3 times the size of the original \textit{and} has been rotated 45 degrees  
**Circle of Evaluation:**

```
Code: ________________________________________________________________
```
You’ll be investigating these functions with your partner:

; text :: String, Number, String -> Image
; flip-horizontal :: Image -> Image
; flip-vertical :: Image -> Image
; frame :: Image -> Image
; above :: Image, Image -> Image
; beside :: Image, Image -> Image

1) In the editor, write the code to make an image of your name in big letters in a color of your choosing using `text`. Then draw the Circle of Evaluation and write the Code that will create the image.

**Circle of Evaluation:**

**Code:**

Using the “image of your name” described above as the original, draw the Circles of Evaluation and write the Code for each exercise below. Test your ideas in the editor to make sure they work.

<table>
<thead>
<tr>
<th>Exercise</th>
<th>Original Description</th>
<th>Circles of Evaluation</th>
</tr>
</thead>
<tbody>
<tr>
<td>2)</td>
<td>The framed “image of your name”.</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td></td>
<td>Circle of Evaluation:</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td>3)</td>
<td>The “image of your name” flipped vertically.</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td></td>
<td>Circle of Evaluation:</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td>4)</td>
<td>The “image of your name” above “the image of your name” flipped vertically.</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td></td>
<td>Circle of Evaluation:</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td>5)</td>
<td>The “image of your name” flipped horizontally beside “the image of your name”.</td>
<td>Code: ____________________</td>
</tr>
<tr>
<td></td>
<td>Circle of Evaluation:</td>
<td>Code: ____________________</td>
</tr>
</tbody>
</table>
You'll be investigating these two functions with your partner:

\[
\text{scale/xy :: Number, Number, Image -> Image} \quad \text{overlay :: Image, Images -> Image}
\]

<table>
<thead>
<tr>
<th>The Image</th>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>□</td>
<td>rhombus 40 90 &quot;solid&quot; &quot;purple&quot;</td>
<td>(rhombus 40 90 &quot;solid&quot; &quot;purple&quot;)</td>
</tr>
</tbody>
</table>

Starting with the image described above, write the Circles of Evaluation and Code for each exercise below. Be sure to test your code in the editor!

1) A purple rhombus that is stretched 4 times as wide.
   Circle of Evaluation:

   Code: ___________________________________________________________________

2) A purple rhombus that is stretched 4 times as tall
   Circle of Evaluation:

   Code: ___________________________________________________________________

3) The tall rhombus overlayed on the wide rhombus.
   Circle of Evaluation:

   Code: ___________________________________________________________________

★: Overlay a red rhombus onto the last image you made.
   Circle of Evaluation:

   Code: ___________________________________________________________________
More than one way to Compose an Image!

Read through these 4 expressions and try to picture the images they are composing. If you're not sure what they'll look like, type them into the interactions area of your editor and see if you can figure out how the code connects to the image.

1

2

3

★

For each image below, identify 2 expressions that could be used to compose it. The bank of expressions at the top of the page includes one possible option for each image.
In math, we use **values** like $-98.1$, $2/3$ and $42$. In math, we also use **expressions** like $1 \times 3$, $\sqrt{16}$, and $5 - 2$. These evaluate to results, and typing any of them in as code produces some answer.

Math also has **definitions**. These are different from values and expressions, because they *do not produce results*. Instead, they simply create names for values, so that those names can be re-used to make the Math simpler and more efficient.

Definitions always have both a name and an expression. The name goes on the left and the value-producing expression goes on the right, separated by an equals sign:

\[
x = 4 \\
y = 9 + x
\]

The name is defined to be the result of evaluating the expression. Using the above examples, we get “$x$ is defined to be $4$, and $y$ is defined to be $13$”. **Important: there is no "answer" to a definition**, and typing in a definition as code will produce no result.

Notice that **definitions can refer to previous definitions**. In the example above, the definition of $y$ refers to $x$. But $x$, on the other hand, *cannot refer to $y$*. Once a value has been defined, it can be used in later expressions.

In WeScheme, these definitions are written a little differently, making it clear that we’re talking about definitions:

```scheme
(define x 4)
(define y (+ 9 x))
```

Just like in math, definitions in our programming language can only refer to previously-defined values.

Here are a few more value definitions. Feel free to type them in, and make sure you understand them.

```scheme
(define x (+ 5 1))
(define y (* x 7))
(define food "Pizza!"
(define dot (circle y "solid" "red"))
```
Defining Values - Explore

Open the [Defining Values Starter File](#) and click run.

1) What do you notice?

2) What do you wonder?

Look at the expressions listed below. Think about what you expect each of them to produce. Then, test them out one at a time in the Interactions Area.

- \(x\)
- \((+ \times 5)\)
- \((- y 9)\)
- \((\times y)\)
- \(z\)
- \(t\)
- \(\text{gold-star}\)
- \(\text{my-name}\)
- \(\text{swamp}\)
- \(5\pi\)

3) What have you learned about defining values?

4) Define at least 2 more variables in the definitions area, click run and test them out. Once you know they’re working, record the code you used below.
1) What image do you see repeated in the flag? ____________________________

2) Highlight or circle all instances of the structure that makes the repeated image in the code below.

3) In the code below, highlight or circle all instances of the expression for that image.

   (put-image
    (rotate 40 (star 15 "solid" "yellow"))
    120 175
   (put-image
    (rotate 80 (star 15 "solid" "yellow"))
    140 150
   (put-image
    (rotate 60 (star 15 "solid" "yellow"))
    140 120
   (put-image
    (rotate 40 (star 15 "solid" "yellow"))
    120 90
   (put-image
    (scale 3 (star 15 "solid" "yellow"))
    60 140
   (rectangle 300 200 "solid" "red"))))

4) Write the code to define a value for the repeated expression.

5) Open the Chinese flag starter file (Wescheme) and click Run. Then type china into the interactions area and click Enter.

6) Save a copy of the file, and simplify the flag code using the value you defined. Click Run, and confirm that you still get the same image as the original.

7) Now change the color of all of the stars to black, in both files. Then change the size of the stars.

8) Why is it helpful to define values for repeated images?

---

Challenge:

- This file uses a function we haven't seen before! What is it? ____________________________
- Can you figure out its contract? Hint: Focus on the last instance of the function.
Why Define Values?

1) Complete the table using the first row as an example.

2) Write the code to define the value of `sunny`.

<table>
<thead>
<tr>
<th>Original Circle of Evaluation &amp; Code</th>
<th>→</th>
<th>Use the defined value <code>sunny</code> to simplify!</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

```latex
scale
3
radial-star
30 20 50 "solid" "yellow"
```

→

```latex
scale
3
sunny
```

<table>
<thead>
<tr>
<th>Code:</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>(scale 3 (radial-star 30 20 50 &quot;solid&quot; &quot;yellow&quot;))</code></td>
</tr>
</tbody>
</table>

→

```latex
(scale 3 sunny)
```

| 

```latex
frame

radial-star
30 20 50 "solid" "yellow"
```

→

```latex
(frame (radial-star 30 20 50 "solid" "yellow"))
```

<table>
<thead>
<tr>
<th>Code:</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>(frame (radial-star 30 20 50 &quot;solid&quot; &quot;yellow&quot;))</code></td>
</tr>
</tbody>
</table>

→

```latex
(scale 3 sunny)
```

| 

```latex
overlay
text
"sun" 30 "black"
radial-star
30 20 50 "solid" "yellow"
```

→

```latex
(overlay (text "sun" 30 "black") (radial-star 30 20 50 "solid" "yellow"))
```

<table>
<thead>
<tr>
<th>Code:</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>(overlay (text &quot;sun&quot; 30 &quot;black&quot;) (radial-star 30 20 50 &quot;solid&quot; &quot;yellow&quot;))</code></td>
</tr>
</tbody>
</table>

→

```latex
(overlay (text "sun" 30 "black") (radial-star 30 20 50 "solid" "yellow"))
```

3) Test your code in the editor and make sure it produces what you would expect it to.
For each of the images below, identify which element(s) you would want to define before writing code to compose the image. Hint: what gets repeated?

<table>
<thead>
<tr>
<th>Philippines</th>
<th>St. Vincent &amp; the Grenadines</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1" alt="Philippines Flag" /></td>
<td><img src="image2" alt="St. Vincent &amp; the Grenadines Flag" /></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Liberia</th>
<th>Republic of Georgia</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image3" alt="Liberia Flag" /></td>
<td><img src="image4" alt="Republic of Georgia Flag" /></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Quebec</th>
<th>South Korea</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image5" alt="Quebec Flag" /></td>
<td><img src="image6" alt="South Korea Flag" /></td>
</tr>
</tbody>
</table>
1) On the line below, write the Code to define \texttt{PRIZE-STAR} as a pink, outline star of size 65.

Using the \texttt{PRIZE-STAR} definition from above, draw the Circle of Evaluation and write the Code for each of the exercises. One Circle of Evaluation has been done for you.

2) The outline of a pink star that is three times the size of the original (using \texttt{scale})
Circle of Evaluation:

3) The outline of a pink star that is half the size of the original (using \texttt{scale})
Circle of Evaluation:

Code:

Code:

4) The outline of a pink star that is rotated 45 degrees \textit{(It should be the same size as the original.)}
Circle of Evaluation:

5) The outline of a pink star that is three times as big as the original and has been rotated 45 degrees
Circle of Evaluation:

Code:

Code:

6) How does defining values help you as a programmer?
Think of the background image as a sheet of graph paper with the origin (0,0) in the bottom left corner. The numbers in `put-image` specify a point on that graph paper, where the center of the top image should be placed.

The width of the rectangle is 300 and the height is 200. The definitions for `dot` and `background` are:

```
(define dot (circle 50 "solid" "red"))
(define background (rectangle 300 200 "outline" "black"))
```

**Estimate:** What coordinates for the `dot` would create each of the following images?

A 

B

C 

D
Decomposing Flags

Each of the flags below is shown with their width and height. Identify the shapes that make up each flag. Use the flag’s dimensions to estimate the dimensions of the different shapes. Then estimate the x and y coordinates for the point at which the center of each shape should be located on the flag. *Hint: The bottom left corner of each flag is at (0,0) and the top right corner is given by the flag’s dimensions.*

<table>
<thead>
<tr>
<th>Flag</th>
<th>Dimensions</th>
<th>Shape</th>
<th>Color</th>
<th>Width</th>
<th>Height</th>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cameroon</td>
<td>(450 x 300)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Chile</td>
<td>(420 x 280)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Panama</td>
<td>(300 x 200)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Norway</td>
<td>(330 x 240)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Notice and Wonder

As you investigate the Game Starter File with your partner, record what you Notice, and then what you Wonder. Remember, “Notices” are statements, not questions.

<table>
<thead>
<tr>
<th>What do you Notice?</th>
<th>What do you Wonder?</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>


Defining Functions

Functions can be viewed in multiple representations. You already know one of them: Contracts, which specify the Name, Domain, and Range of a function. Contracts are a way of thinking of functions as a mapping between one set of data and another. For example, a mapping from Numbers to Strings:

```
f :: Number -> String
```

Another way to view functions is with Examples. Examples are essentially input-output tables, showing what the function would do for a specific input:

In our programming language, we focus on the last two columns and write them as code:

```lisp
(EXAMPLE (f 1) (+ 1 2))
(EXAMPLE (f 2) (+ 2 2))
(EXAMPLE (f 3) (+ 3 2))
(EXAMPLE (f 4) (+ 4 2))
```

Finally, we write a formal function definition ourselves. The pattern in the Examples becomes abstract (or "general"), replacing the inputs with variables. In the example below, the same definition is written in both math and code:

```
f(x) = x + 2
```

```
(define (f x) (+ x 2))
```

Look for connections between these three representations!

- The function name is always the same, whether looking at the Contract, Examples, or Definition.
- The number of inputs in the Examples is always the same as the number of types in the Domain, which is always the same as the number of variables in the Definition.
- The "what the function does" pattern in the Examples is almost the same in the Definition, but with specific inputs replaced by variables.
Look at each set of examples on the left and circle what is changing from one example to the next. Then, match the examples on the left to the definitions on the right.

<table>
<thead>
<tr>
<th>Examples:</th>
<th>Functions:</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x$</td>
<td>$f(x)$</td>
</tr>
<tr>
<td>1</td>
<td>$2 \times 1$</td>
</tr>
<tr>
<td>2</td>
<td>$2 \times 2$</td>
</tr>
<tr>
<td>3</td>
<td>$2 \times 3$</td>
</tr>
<tr>
<td>15</td>
<td>$15 - 3$</td>
</tr>
<tr>
<td>25</td>
<td>$25 - 3$</td>
</tr>
<tr>
<td>35</td>
<td>$35 - 3$</td>
</tr>
<tr>
<td>10</td>
<td>$10 + 2$</td>
</tr>
<tr>
<td>15</td>
<td>$15 + 2$</td>
</tr>
<tr>
<td>20</td>
<td>$20 + 2$</td>
</tr>
<tr>
<td>0</td>
<td>$3(0) - 2$</td>
</tr>
<tr>
<td>1</td>
<td>$3(1) - 2$</td>
</tr>
<tr>
<td>2</td>
<td>$3(2) - 2$</td>
</tr>
<tr>
<td>10</td>
<td>$2(10) + 1$</td>
</tr>
<tr>
<td>20</td>
<td>$2(20) + 1$</td>
</tr>
<tr>
<td>30</td>
<td>$2(30) + 1$</td>
</tr>
</tbody>
</table>
Matching Examples and Function Definitions

Highlight the variables in `gt` and label them with the word "size".

```
(EXAMPLE (gt 20)
  (triangle 20 "solid" "green"))
(EXAMPLE (gt 45)
  (triangle 45 "solid" "green"))
(define (gt size) (triangle size "solid" "green"))
```

Highlight and label the variables in the example lists below. Then, using `gt` as a model, match the examples to their corresponding function definitions.

<table>
<thead>
<tr>
<th>Examples</th>
<th>Definition</th>
</tr>
</thead>
</table>
| (EXAMPLE (f "solid")
  (circle 8 "solid" "red")) | 1 A (define (f s) (star s "outline" "red")) |
| (EXAMPLE (f "outline")
  (circle 8 "outline" "red")) | |

| EXAMPLE (f 2) (+ 2 2))
(EXAMPLE (f 4) (+ 4 4))
(EXAMPLE (f 5) (+ 5 5)) | 2 B (define (f num) (+ num num)) |

| EXAMPLE (f "red") (circle 7 "solid" "red")|
(EXAMPLE (f "teal")
  (circle 7 "solid" "teal")) | 3 C (define (f c) (star 9 "solid" c)) |

| EXAMPLE (f "red") (star 9 "solid" "red")|
(EXAMPLE (f "grey") (star 9 "solid" "grey"))
(EXAMPLE (f "pink") (star 9 "solid" "pink")) | 4 D (define (f s) (circle 8 s "red")) |

| EXAMPLE (f 3) (star 3 "outline" "red"))
(EXAMPLE (f 8) (star 8 "outline" "red")) | 5 E (define (f c) (circle 7 "solid" c)) |
<table>
<thead>
<tr>
<th>Contract</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>(EXAMPLE (f 1) (rectangle 1 1 &quot;outline&quot; &quot;red&quot;)) (EXAMPLE (f 6) (rectangle 6 6 &quot;outline&quot; &quot;red&quot;))</td>
</tr>
<tr>
<td>B</td>
<td>(EXAMPLE (f &quot;pink&quot; 5) (star 5 &quot;solid&quot; &quot;pink&quot;)) (EXAMPLE (f &quot;blue&quot; 8) (star 8 &quot;solid&quot; &quot;blue&quot;))</td>
</tr>
<tr>
<td>C</td>
<td>(EXAMPLE (f &quot;Hi!&quot;) (text &quot;Hi!&quot; 50 &quot;red&quot;)) (EXAMPLE (f &quot;Ciao!&quot;) (text &quot;Ciao!&quot; 50 &quot;red&quot;))</td>
</tr>
<tr>
<td>D</td>
<td>(EXAMPLE (f 5 &quot;outline&quot;) (star 5 &quot;outline&quot; &quot;yellow&quot;)) (EXAMPLE (f 5 &quot;solid&quot;) (star 5 &quot;solid&quot; &quot;yellow&quot;))</td>
</tr>
<tr>
<td>E</td>
<td>(EXAMPLE (f &quot;red&quot; 5) (rectangle 5 5 &quot;outline&quot; &quot;red&quot;)) (EXAMPLE (f &quot;blue&quot; 5) (rectangle 5 5 &quot;solid&quot; &quot;blue&quot;))</td>
</tr>
</tbody>
</table>
### gt

**Directions:** Define a function called \( \text{gt} \), which makes solid green triangles of whatever size we want.

**Every contract has three parts...**

\[
\begin{array}{ccc}
\text{function name} & \text{domain} & \rightarrow \text{Image} \\
\end{array}
\]

**Write some examples, then circle and label what changes...**

(\text{EXAMPLE} (\text{gt} 10) (\text{triangle} 10 \text{ "solid" "green"}))

(\text{EXAMPLE} (\text{gt} 20) (\text{triangle} 20 \text{ "solid" "green"}))

**Write the definition, giving variable names to all your input values...**

(\text{define} (\text{gt} \text{ size})

(triangle \text{ size} \text{ "solid" "green"}))

### bc

**Directions:** Define a function called \( \text{bc} \), which makes solid blue circles of whatever radius we want.

**Every contract has three parts...**

\[
\begin{array}{ccc}
\text{function name} & \text{domain} & \rightarrow \text{Image} \\
\end{array}
\]

**Write some examples, then circle and label what changes...**

(\text{EXAMPLE} (\text{bc} \text{ radius}) (\text{circle} \text{ radius} \text{ "solid" "blue"}))

(\text{EXAMPLE} (\text{bc} \text{ radius}) (\text{circle} \text{ radius} \text{ "solid" "blue"}))

**Write the definition, giving variable names to all your input values...**

(\text{define} (\text{bc} \text{ radius})

(circle \text{ radius} \text{ "solid" "blue"}))
What’s on your mind?
Solving Word Problems

Being able to see functions as Contracts, Examples or Definitions is like having three powerful tools. These representations can be used together to solve word problems!

1) When reading a word problem, the first step is to figure out the **Contract** for the function you want to build. Remember, a Contract must include the Name, Domain and Range for the function!

2) Then we write a **Purpose Statement**, which is a short note that tells us what the function *should do*. Professional programmers work hard to write good purpose statements, so that other people can understand the code they wrote!

3) Next, we write at least two **Examples**. These are lines of code that show what the function should do for a *specific* input. Once we see examples of at least two inputs, we can *find a pattern* and see which parts are changing and which parts aren’t.

4) To finish the Examples, we circle the parts that are changing, and label them with a short **variable name** that explains what they do.

5) Finally, we define the function itself! This is pretty easy after you have some examples to work from: we copy everything that didn’t change, and replace the changeable stuff with the variable name!
Creating Contracts From Examples

Write the contracts used to create each of the following collections of examples.

1)  
(EXAMPLE (big-triangle 100 "red")
(triangle 100 "solid" "red")
(EXAMPLE (big-triangle 200 "orange")
(triangle 200 "solid" "orange"))

2)  
(EXAMPLE (purple-square 15)
(rectangle 15 15 "outline" "purple")
(EXAMPLE (purple-square 6)
(rectangle 6 6 "outline" "purple"))

3)  
(EXAMPLE (banner "Game Today!"
(text "Game Today!" 50 "red")
(EXAMPLE (banner "Go Team!"
(text "Go Team!" 50 "red")
(EXAMPLE (banner "Exit"
(text "Exit" 50 "red"))

4)  
(EXAMPLE (twinkle "outline" "red")
(star 5 "outline" "red")
(EXAMPLE (twinkle "solid" "pink")
(star 5 "solid" "pink")
(EXAMPLE (twinkle "outline" "grey")
(star 5 "outline" "grey")

5)  
(EXAMPLE (half 5) (/ 5 2))
(EXAMPLE (half 8) (/ 8 2))
(EXAMPLE (half 900) (/ 900 2))
Writing Examples from Purpose Statements

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

**Contract and Purpose Statement**

Every contract has three parts...

- **Product-squared:**
  
  function name: product-squared
  
  domain: Number
  
  range: Number

  Consumes two numbers and squares their product

  what does the function do?

  (EXAMPLE (function name input(s)) what the function produces)

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

---

**Contract and Purpose Statement**

Every contract has three parts...

- **Upside-down:**
  
  function name: upside-down
  
  domain: Image
  
  range: Image

  Consumes an image, and flips it upside down by rotating it 180 degrees.

  what does the function do?

  (EXAMPLE (function name input(s)) what the function produces)

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)
Directions: A rocket blasts off, and is now traveling at a constant velocity of 7 meters per second. Use the Design Recipe to write a function `rocket-height`, which takes in a number of seconds and calculates the height.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function name variable(s))

what the function does with those variable(s))
<table>
<thead>
<tr>
<th>1st Read: What is this problem about?</th>
<th>2nd Read: What are the Quantities?</th>
<th>3rd Read: What is a good Purpose Statement?</th>
<th>Stronger &amp; Clearer</th>
<th>Purpose Statement 1st Revision:</th>
<th>Purpose Statement 2nd Revision:</th>
</tr>
</thead>
</table>
The Design Recipe - Direct Variation

Directions: Write a function `wage`, that takes in a number of hours worked and returns the amount a worker will get paid if their rate is $10.25/hr.

Contract and Purpose Statement
Every contract has three parts...

- function name: domain -> range
- what does the function do?

Examples
Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

Definition
Write the definition, giving variable names to all your input values...

(define (function name variable(s))
what the function does with those variable(s))

Directions: On average, people burn about 11 calories/minute riding a bike. Write a function `calories-burned` that takes in the number of minutes you bike and returns the number of calories burned.

Contract and Purpose Statement
Every contract has three parts...

- function name: domain -> range
- what does the function do?

Examples
Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

Definition
Write the definition, giving variable names to all your input values...

(define (function name variable(s))
what the function does with those variable(s))
Directions: Write a function **marquee** that takes in a message and returns that message in large gold letters.

**Contract and Purpose Statement**

Every contract has three parts...

- **function name**: domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function name variable(s))
  what the function does with those variable(s))

Directions: Write a function **num-cube** that takes in a number and returns the cube of that number.

**Contract and Purpose Statement**

Every contract has three parts...

- **function name**: domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function name variable(s))
  what the function does with those variable(s))
The Design Recipe (Practice 2)

Directions: Write a function `split-tab` that takes in a cost and the number of people sharing the bill and splits the cost equally.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function name variable(s)) what the function does with those variable(s))

Directions: Write a function `tip-calculator` that takes in the cost of a meal and returns the 15% tip for that meal.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function name variable(s)) what the function does with those variable(s))
The Design Recipe (Practice 3)

**Directions**: The Swamp in the City Festival is ordering t-shirts. The production cost is $75 to set up the silk screen and $9 per shirt. Write a function `min-shirt-price` that takes in the number of shirts to be ordered, `n`, and returns the minimum amount the festival should charge for the shirts in order to break even. (Assume that they will sell all of the shirts.)

<table>
<thead>
<tr>
<th>Contract and Purpose Statement</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Every contract has three parts...</strong></td>
</tr>
<tr>
<td>function name : domain -&gt; range</td>
</tr>
<tr>
<td>; what does the function do?</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Write some examples, then circle and label what changes...</td>
</tr>
</tbody>
</table>

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

<table>
<thead>
<tr>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>Write the definition, giving variable names to all your input values...</td>
</tr>
</tbody>
</table>

(define (function name variable(s))

what the function does with those variable(s))
**Directions**: For his birthday, James’ family decided to open a savings account for him. He started with $50 and committed to adding $10 a week from his afterschool job teaching basketball to kindergartners. Write a function `savings` that takes in the number of weeks since his birthday and calculates how much money he has saved.

### Contract and Purpose Statement

Every contract has three parts...

- function name: ____________
- domain: ____________
- range: ____________

- what does the function do?

### Examples

Write some examples, then circle and label what changes...

( EXAMPLE ( function name input(s) ) what the function produces )

( EXAMPLE ( function name input(s) ) what the function produces )

### Definition

Write the definition, giving variable names to all your input values...

( define ( function name variable(s) ) what the function does with those variable(s) )

### Directions: Write a function `moving` that takes in the days and number of miles driven and returns the cost of renting a truck. The truck is $45 per day and each driven mile is 15¢.

### Contract and Purpose Statement

Every contract has three parts...

- function name: ____________
- domain: ____________
- range: ____________

- what does the function do?

### Examples

Write some examples, then circle and label what changes...

( EXAMPLE ( function name input(s) ) what the function produces )

( EXAMPLE ( function name input(s) ) what the function produces )

### Definition

Write the definition, giving variable names to all your input values...

( define ( function name variable(s) ) what the function does with those variable(s) )
Directions: An Olympic pool holds 660,000 gallons of water. A fire hose can spray about 250 gallons per minute. Write a function pool that takes in the number of minutes that have passed and calculates how much water is still needed to fill it.

Contract and Purpose Statement

Every contract has three parts...

; function name : domain -> range ;

Examples

Write some examples, then circle and label what changes...

(EXAMPLE ( ; function name input(s) ; what the function produces ) )

Definition

Write the definition, giving variable names to all your input values...

(define ( ; function name variable(s) ; what the function does with those variable(s) ) )

Directions: The community arts fund awards a $1500 grant each month to support a new mural. They started with $50000 in their account. Write a function funds-available that takes in the number of months and calculates how much money they have left.

Contract and Purpose Statement

Every contract has three parts...

; function name : domain -> range ;

Examples

Write some examples, then circle and label what changes...

(EXAMPLE ( ; function name input(s) ; what the function produces ) )

Definition

Write the definition, giving variable names to all your input values...

(define ( ; function name variable(s) ; what the function does with those variable(s) ) )
Directions: Write a function `lawn-area` that takes in the length and width of a rectangular lawn and returns its area.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function variable input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function variable(s)) what the function does with those variable(s))

Directions: Write a function `rect-perimeter` that takes in the length and width of a rectangle and returns the perimeter of that rectangle.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function variable input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define (function variable(s)) what the function does with those variable(s))
The Design Recipe (Geometry - Rectangular Prisms)

Directions: Write a function `rectprism-vol` that takes in the length, width, and height of a rectangular prism and returns the Volume of a rectangular prism.

**Contract and Purpose Statement**
Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**
Write some examples, then circle and label what changes...

( EXAMPLE ( function name input(s) ) what the function produces )

( EXAMPLE ( function name input(s) ) what the function produces )

**Definition**
Write the definition, giving variable names to all your input values...

( define ( function name variable(s) ) what the function does with those variable(s) )

Directions: Write a function `rect-prism-sa` that takes in the width, length and height of a rectangular prism and calculates its surface area (the sum of the areas of each of its six faces)

**Contract and Purpose Statement**
Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**
Write some examples, then circle and label what changes...

( EXAMPLE ( function name input(s) ) what the function produces )

( EXAMPLE ( function name input(s) ) what the function produces )

**Definition**
Write the definition, giving variable names to all your input values...

( define ( function name variable(s) ) what the function does with those variable(s) )
Directions: Write a function `circle-area-dec` that takes in a radius and uses the decimal approximation of pi (3.14) to return the area of the circle.

**Contract and Purpose Statement**

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
<th>what does the function do?</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(\(define ( function name variable(s) )\)

what the function does with those variable(s))

Directions: Write a function `circumference` that takes in a radius and uses the decimal approximation of pi (3.14) to return the circumference of the circle.

**Contract and Purpose Statement**

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
<th>what does the function do?</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(\(define ( function name variable(s) )\)

what the function does with those variable(s))
The Design Recipe (Geometry - Cylinders)

**Directions**: Write a function `circle-area` that takes in a radius and uses the fraction approximation of \( \pi \) (\( \frac{22}{7} \)) to return the area of the circle.

**Contract and Purpose Statement**

Every contract has three parts…

- function name -> range

what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values…

(define (function name variable(s))

what the function does with those variable(s))

**Directions**: Write a function `cylinder` that takes in a cylinder’s radius and height and calculates its volume, making use of the function `circle-area`.

**Contract and Purpose Statement**

Every contract has three parts…

- function name -> range

what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values…

(define (function name variable(s))

what the function does with those variable(s))
Danger and Target Movement

**Directions:** Use the Design Recipe to write a function `update-danger`, which takes in the danger’s x-coordinate and produces the next x-coordinate, which is 50 pixels to the left.

**Contract and Purpose Statement**

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>-&gt;</th>
<th>range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )

what the function does with those variable(s))

**Directions:** Use the Design Recipe to write a function `update-target`, which takes in the target’s x-coordinate and produces the next x-coordinate, which is 50 pixels to the right.

**Contract and Purpose Statement**

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>-&gt;</th>
<th>range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )

what the function does with those variable(s))
Sometimes a problem is too complicated to solve all at once. Maybe there are too many variables, or there is just so much information that we can't get a handle on it!

We can use Problem Decomposition to break those problems down into simpler pieces, and then work with the pieces to solve the whole. There are two strategies we can use for decomposition:

- **Top-Down** - Start with the "big picture", writing functions or equations that describe the connections between parts of the problem. Then, work on defining those parts.

- **Bottom-Up** - Start with the smaller parts, writing functions or equations that describe the parts we understand. Then, connect those parts together to solve the whole problem.

You may find that one strategy works better for some types of problems than another, so make sure you're comfortable using either one!
The Design Recipe: Revenue & Cost

Directions: Use the Design Recipe to write a function `revenue`, which takes in the number of glasses sold at $1.75 apiece and calculates the total revenue.

**Contract and Purpose Statement**

Every contract has three parts...

- function name: ____________________________
  - domain: ____________________________
  - range: ____________________________

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )
  what the function does with those variable(s))

Directions: Use the Design Recipe to write a function `cost`, which takes in the number of glasses sold and calculates the total cost of materials if each glass costs $.30 to make.

**Contract and Purpose Statement**

Every contract has three parts...

- function name: ____________________________
  - domain: ____________________________
  - range: ____________________________

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )
  what the function does with those variable(s))
Directions: Use the Design Recipe to write a function profit that calculates total profit from glasses sold, which is computed by subtracting the total cost from the total revenue.

Contract and Purpose Statement

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
<th>what does the function do?</th>
</tr>
</thead>
</table>

Examples

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

Definition

Write the definition, giving variable names to all input values...

(define (function name variable(s))

what the function does with those variable(s))
Inequalities

- Sometimes we want to ask questions about data. For example, is \(x\) greater than \(y\)? Is one string equal to another? These questions can't be answered with a Numbers. Instead, they are answered with a new data type called a **Boolean**.

- Video games use Booleans for many things: asking when a player’s health is equal to zero, whether two characters are close enough to bump into one another, or if a character’s coordinates put it off the edge of the screen.

- A Boolean value is either **true** or **false**. Unlike Numbers, Strings, and Images, Booleans have only two possible values.

- You already know some functions that produce Booleans, such as \(<\) and \(\geq\)! Our programming language has them, too: \((< 3 4)\), \((\geq 10 2)\), and \((= -10 19)\).

- We also have ways of writing **Compound Inequalities**, so we can ask more complicated questions using the **and** and **or** functions.
  - \((\text{and} (> 3 4) (< 10 2))\) translates to "three is greater than four and ten is less than two". This will evaluate to **false**, since the **and** function requires that both sub-expressions be **true**.
  - \((\text{or} (> 3 4) (< 10 2))\), which translates to "three is greater than four or ten is less than two". This will evaluate to **true**, since the **or** function only requires that one sub-expression be **true**.

- The Circles of Evaluation work the same way with Booleans that they do with Numbers, Strings and Images:
Explore the functions in the Booleans Starter File. What characteristics define them as Booleans?

Fill in the blanks below so that each of the five functions returns true:
1) (is-odd [ ])
2) (is-even [ ])
3) (is-less-than-one [ ])
4) (is-continent [ ])
5) (is-primary-color [ ])

Fill in the blanks below so that each of the five functions returns false:
6) (is-odd [ ])
7) (is-even [ ])
8) (is-less-than-one [ ])
9) (is-continent [ ])
10) (is-primary-color [ ])
Simple Inequalities

Each inequality expression in the first column contains a number. Decide whether or not that number is a solution to the expression and place it in the appropriate column. Then identify 4 solution and 4 non-solution values for \( x \).

- **Solutions** will make the expression true.
- **Non-Solutions** will make the expression false.

Challenge yourself to use negatives, positives, fractions, decimals, etc. for your \( x \) values.

<table>
<thead>
<tr>
<th>Expression</th>
<th>4 solutions that evaluate to true</th>
<th>4 non-solutions that evaluate to false</th>
</tr>
</thead>
<tbody>
<tr>
<td>( &gt; x 2 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( &lt;= x -2 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( &lt; x 3.5 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( &gt;= x -1 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( &gt; x -4 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( &lt;&gt; x 2 )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

1) For which inequalities was the number from the expression part of the solution?

2) For which inequalities was the number from the expression not part of the solution?

3) For which inequalities were the solutions on the left end of the number line?

4) For which inequalities were the solutions on the right end of the number line?
### Converting Circles of Evaluation to Code

For each Circle of Evaluation on the left-hand side, write the code for the Circle on the right-hand side.

<table>
<thead>
<tr>
<th>Circle of Evaluation</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Circle 1" /></td>
<td>$&gt; \ 4 \ &lt; 5 \ &lt; 9$</td>
</tr>
<tr>
<td><img src="image2.png" alt="Circle 2" /></td>
<td>$\text{and} \ &lt; 5 \ 10 \ &lt; 10 \ 15$</td>
</tr>
<tr>
<td><img src="image3.png" alt="Circle 3" /></td>
<td>$\text{or} \ \text{string}=? \ \text{yum} \ &quot;apple&quot; \ \text{string}=? \ \text{yum} \ &quot;banana&quot;$</td>
</tr>
<tr>
<td><img src="image4.png" alt="Circle 4" /></td>
<td>$\geq \ \text{string-length} \ 6 \ \text{&quot;My Game&quot;}$</td>
</tr>
<tr>
<td><img src="image5.png" alt="Circle 5" /></td>
<td>$\text{or} \ \text{and} \ &lt; 1 \ x \ 5 \ \text{and} \ &lt; 8 \ x \ 10$</td>
</tr>
</tbody>
</table>
Create the Circles of Evaluation, then convert the expressions into code in the space provided.

1) 2 is less than 5, and 0 is equal to 6

What will this evaluate to? ________________

2) 6 is greater than 8, or -4 is less than 1

What will this evaluate to? ________________

3) The String "purple" is the same as the String "blue", and 3 plus 5 equals 8

What will this evaluate to? ________________

4) Write the contracts for and & or in your Contracts page.
### Compound Inequalities: Solutions & Non-Solutions

For each Compound Inequality listed below, identify 4 solutions and 4 non-solutions. If there are no solutions or the solution set includes all real numbers you can write that instead of making a list.

- Solutions for intersections, which use **and** will make both of the expressions **true**.
- Solutions for unions, which use **or** will make at least one of the expressions **true**.

Pay special attention to the numbers in the sample expression! Challenge yourself to use negatives, positives, fractions, decimals, etc. for your $x$ values.

The first two have been done for you - Answers will vary!

<table>
<thead>
<tr>
<th>Expression</th>
<th>4 solutions that evaluate to <strong>true</strong></th>
<th>4 non-solutions that evaluate to <strong>false</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td>$x &gt; 5 \text{ and } x &lt; 15$</td>
<td>6, 9.5, 12, 14.9</td>
<td>-2, 5, 15, 16.1</td>
</tr>
<tr>
<td>$x &gt; 5 \text{ or } x &lt; 15$</td>
<td>All real numbers</td>
<td>No non-solutions</td>
</tr>
<tr>
<td>$x \leq -2 \text{ and } x &gt; 7$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x \leq -2 \text{ or } x &gt; 7$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x &lt; 3.5 \text{ and } x &gt; -4$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x &lt; 3.5 \text{ or } x &gt; -4$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x \geq -1 \text{ and } x &gt; -5$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x \geq -1 \text{ or } x &gt; -5$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x &lt; -4 \text{ and } x &gt; 2$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

1) Could there ever be a union with no solutions? Explain your thinking.

2) Could there ever be an intersection whose solution is all real numbers? Explain your thinking.
Each of the plots below was generated using the code `inequality(comp-ineq, [list: -1, 0, 1.6, 3, 5.2, 7, 8.1, 9] ). With the exception of the example, each plot below was defined using the numbers 3 and 7. Write the code for how `comp-ineq` was defined for each plot in the space provided.

```scheme
(define (comp-ineq x) (and (> x 0) (<= x 8.1)))
```
Open the “Sam the Butterfly” starter file and press “Run”. (Hi, Sam!)
Move Sam around the screen using the arrow keys.

1) What do you notice about the program?

2) What do you wonder?

3) What do you see when Sam is at (0,0)? Why is that?

4) What changes as the butterfly moves left and right?

Sam is in a 640 × 480 yard. Sam's mom wants Sam to stay in sight.

How far to the left and right can Sam go and still remain visible?

Use the new inequality functions to answer the following questions with code:

5) Sam hasn't gone off the left edge of the screen as long as...

6) Sam hasn't gone off the right edge of the screen as long as...

7) Use the space below to draw Circles of Evaluation for these two expressions:
**Left and Right**

**Directions**: Use the Design Recipe to write a function `safe-left?`, which takes in an x-coordinate and checks to see if it is greater than -50.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE __________)

(EXAMPLE __________)

**Definition**

Write the definition, giving variable names to all your input values...

(define __________)

what the function produces

**Directions**: Use the Design Recipe to write a function `safe-right?`, which takes in an x-coordinate and checks to see if it is less than 690.

**Contract and Purpose Statement**

Every contract has three parts...

- function name : domain -> range
- what does the function do?

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE __________)

(EXAMPLE __________)

**Definition**

Write the definition, giving variable names to all your input values...

(define __________)

what the function produces
Word Problem: onscreen?

Directions: Use the Design Recipe to write a function `onscreen?`, which takes in an x-coordinate and checks to see if Sam is safe on the left while also being safe on the right.

Contract and Purpose Statement

Every contract has three parts...

- function name : domain -> range
- what does the function do?

Examples

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

Definition

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )

what the function does with those variable(s))
Sometimes we want to build functions that act differently for different inputs. For example, suppose a business charges $10/pizza, but only $5 for orders of six or more. How could we write a function that computes the total price based on the number of pizzas?

In math, **Piecewise Functions** are functions that can behave one way for part of their Domain, and another way for a different part. In our pizza example, our function would act like \( \text{cost(pizzas)} = 10 \times \text{pizzas} \) for anywhere from 1-5 pizzas. But after 5, it acts like \( \text{cost(pizzas)} = 5 \times \text{pizzas} \).

Piecewise functions are divided into “pieces”. Each piece is divided into two parts:

1. How the function should behave
2. The domain where it behaves that way

Our programming language can be used to write piecewise functions, too! Just as in math, each piece has two parts:

```scheme
(define (cost pizzas)
  (cond
    [(>= pizzas 6) (* 5 pizzas)]
    [else (* 10 pizzas)]
  ))
```

Piecewise functions are powerful, and let us solve more complex problems. We can use piecewise functions in a video game to add or subtract from a character’s x-coordinate, moving it left or right depending on which key was pressed.
Welcome to Alice’s Restaurant!

Alice has hired you to improve some code used at the restaurant. The code we’ll be improving on is shown below.

Read through the code line-by-line with your partner before writing down your observations in the tables below.

; cost :: String -> Number
; given a item, produce the cost of that item
(define (cost item)
  (cond
    [(string=? item "onion rings") 3.5]
    [(string=? item "fried tofu") 5.25]
    [(string=? item "pie") 2.25]
    [else "Sorry, that’s not on the menu!"]
))
Alice's code has some new elements we haven't seen before, so let's experiment a bit to figure out how it works! **Open the Alice's Restaurant starter file**, click “Run”, and try using the `cost` function in the Interactions window.

1) What does `(cost "hamburger")` evaluate to? ____________________________

2) What does `(cost "pie")` evaluate to? ____________________________

3) What if you ask for `(cost "fries")`? ____________________________

4) Explain what the function is doing in your own words.

5) What is the function's name? _________________ Domain? _________________ Range? _________________

6) What is the name of its variable? ____________________________

7) Alice says onion rings have gone up to $3.75. Change the `cost` function to reflect this.

8) Try adding menu items of your own. What's your favorite?

9) For an unknown food item, the function produces the String "That's not on the menu!" Is this a problem? Why or why not?

10) Suppose Alice wants to calculate the price of a hamburger, including a 5% sales tax. Draw a Circle of Evaluation for the expression below.
Directions: Alice's Restaurant has hired you as a programmer. They offer the following menu items: hamburger ($6.00), onion rings ($3.50), fried tofu ($5.25) and pie ($2.25). Write a function called \texttt{order} which takes in the name of a menu item and outputs the price of that item.

**Contract and Purpose Statement**

Every contract has three parts...

\[
\begin{array}{c|c|c}
\text{function name} & \text{domain} & \text{range} \\
\hline
\end{array}
\]

\text{: what does the function do?}

**Examples**

Write some examples, then circle and label what changes...

\[
\begin{array}{c|c|c}
\text{EXAMPLE} & \text{function name} & \text{input(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{what the function produces} \\
\hline
\end{array}
\]

**Definition**

Write the definition, giving variable names to all your input values...

\[
\begin{array}{c|c|c}
\text{define} & \text{function name} & \text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
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\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
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\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]

\[
\begin{array}{c|c|c}
\text{variable(s)} \\
\hline
\end{array}
\]
Word Problem: update-player

Directions: The player moves up and down by 20 pixels each time. Write a function called `update-player`, which takes in the player’s y-coordinate and the name of the key pressed ("up" or "down"), and returns the new y-coordinate.

Contract and Purpose Statement

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Examples

Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

Definition

Write the definition, giving variable names to all your input values...

(define (function name variable(s))
  (_________
    [_________]
    [_________]
    [_________] )

[_________]
[_________]
[_________])
Challenges for update-player

For each of the challenges below, see if you can come up with two EXAMPLEs of how it should work!

1) Warping - Program one key to "warp" the player to a set location, such as the center of the screen.

(EXAMPLE (update-player ____________________________ ) ________________ )

(EXAMPLE (update-player ____________________________ ) ________________ )

2) Boundaries - Change update-player such that PLAYER cannot move off the top or bottom of the screen.

(EXAMPLE (update-player ____________________________ ) ________________ )

(EXAMPLE (update-player ____________________________ ) ________________ )

3) Wrapping - Add code to update-player such that when PLAYER moves to the top of the screen, it reappears at the bottom, and vice versa.

(EXAMPLE (update-player ____________________________ ) ________________ )

(EXAMPLE (update-player ____________________________ ) ________________ )

4) Hiding - Add a key that will make PLAYER seem to disappear, and reappear when the same key is pressed again.

(EXAMPLE (update-player ____________________________ ) ________________ )

(EXAMPLE (update-player ____________________________ ) ________________ )

(EXAMPLE (update-player ____________________________ ) ________________ )
Word Problem: line-length

Directions: Write a function called 'line-length', which takes in two numbers and returns the positive difference between them. It should always subtract the smaller number from the bigger one. If they are equal, it should return zero.

Contract and Purpose Statement

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

what does the function do?

Examples

Write some examples, then circle and label what changes...

(EXAMPLE (line-length 10 5) (- 10 5))

(EXAMPLE (line-length 2 8) (- 2 8))

Definition

Write the definition, giving variable names to all your input values...

(define (line-length function name variable(s))

(_______

[_____________________________________]  
[_____________________________________]  
))
In each of the game screenshots below, one of the distance labels has been hidden. Write the code to generate the missing distance on the line below each image. *Hint: Remember the Pythagorean Theorem!*
Distance on the Coordinate Plane

Distance between the pyret and the boot:

$\sqrt{(\text{sqr}(\text{line-length} \ 9 \ -3)) \ + \ (\text{sqr}(\text{line-length} \ 3 \ -2)))}$

Explain how the code works.

Now write the code to find the distance between this boot and pyret.
The Distance Between \((0, 2)\) and \((4, 5)\)

The distance between \(x_1\) and \(x_2\) is computed by \((\text{line-length } \ x_1 \ x_2)\). The distance between \(y_1\) and \(y_2\) is computed by \((\text{line-length } \ y_1 \ y_2)\). Below is the equation to compute the hypotenuse of a right triangle with those amount for legs:

$$\sqrt{\text{line-length}(x_2, x_1)^2 + \text{line-length}(y_2, y_1)^2}$$

Suppose your player is at \((0, 2)\) and a character is at \((4, 5)\). What is the distance between them? With your pencil, label which numbers represent \(x_1\), \(y_1\), \(x_2\) and \(y_2\). The equation to compute the distance between these points is:

$$\sqrt{\text{line-length}(4, 0)^2 + \text{line-length}(5, 2)^2}$$

1. Translate the expression above, for \((0,2)\) and \((4,5)\) into a Circle of Evaluation below.

2. Convert the Circle of Evaluation to Code below.
Distance between (1, 3) and (5, 0)
Distance From Game Coordinates

For each of the game screenshots, write the code to calculate the distance between the indicated characters. The first one has been done for you.

\[
\sqrt{\left(\text{sqr}(600 - 150) + \text{sqr}(110 - 300)\right)}
\]

\[
(150, 300)
\]

\[
(600, 110)
\]
Directions: Use the Design Recipe to write a function \texttt{distance}, which takes in FOUR inputs: \texttt{px} and \texttt{py} (the x- and y-coordinate of the Player) and \texttt{cx} and \texttt{cy} (the x- and y-coordinates of another character), and produces the distance between them in pixels.

Contract and Purpose Statement

Every contract has three parts...

\begin{itemize}
  \item function name : domain \rightarrow range
  \item what does the function do?
\end{itemize}

Examples

Write some examples, then circle and label what changes...

\begin{itemize}
  \item (EXAMPLE )
\end{itemize}

Definition

Write the definition, giving variable names to all your input values...

\begin{itemize}
  \item (define )
\end{itemize}
Comparing Code: Finding Missing Distances

For each of the game screenshots below, the math and the code for computing the covered distance is shown. Notice what is similar and what is different about how the top and bottom distances are calculated. Think about why those similarities and differences exist and record your thinking.

\[ \sqrt{166^2 + 276^2} \]

\[ \sqrt{276^2 - 194^2} \]

\( \texttt{(sqrt (+ (sqr 166) (sqr 276)))} \)

\( \texttt{(sqrt (- (sqr 276) (sqr 194)))} \)
A retractable flag pole starts out 24 inches tall, and grows taller at a rate of 0.6in/sec. An elastic is anchored 200 inches from the base and attached to the top of the pole, forming a right triangle. Using a top-down or bottom-up strategy, define functions that compute the height of the pole and the area of the triangle after a given number of seconds.

**Directions**: Define your first function (height or area) here.

**Contract and Purpose Statement**
Every contract has three parts...

- function name : domain -> range

- what does the function do?

**Examples**
Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**
Write the definition, giving variable names to all your input values...

(define (function name variable(s))
what the function does with those variable(s))

**Directions**: Define your second function (height or area) here.

**Contract and Purpose Statement**
Every contract has three parts...

- function name : domain -> range

- what does the function do?

**Examples**
Write some examples, then circle and label what changes...

(EXAMPLE (function name input(s)) what the function produces)

(EXAMPLE (function name input(s)) what the function produces)

**Definition**
Write the definition, giving variable names to all your input values...

(define (function name variable(s))
what the function does with those variable(s))
**Word Problem: collide?**

**Directions**: Use the Design Recipe to write a function `collide?`, which takes in the coordinates of two objects and checks if they are close enough to collide.

**Contract and Purpose Statement**

Every contract has three parts...

<table>
<thead>
<tr>
<th>function name</th>
<th>domain</th>
<th>range</th>
<th>what does the function do?</th>
</tr>
</thead>
</table>

**Examples**

Write some examples, then circle and label what changes...

(EXAMPLE ( function name input(s) ) what the function produces)

(EXAMPLE ( function name input(s) ) what the function produces)

**Definition**

Write the definition, giving variable names to all your input values...

(define ( function name variable(s) )

what the function does with those variable(s))
**Contracts**

Contracts tell us how to use a function. For example, `ellipse :: Number, Number, String, String -> Image` tells us that the name of the function is `ellipse`, and that it takes four inputs (two Numbers and two Strings). From the contract, we know that `(ellipse 100 50 "outline" "red")` will evaluate to an Image.
Contracts tell us how to use a function. e.g. `ellipse :: Number, Number, String, String -> Image` tells us that the name of the function is `ellipse`, and that it takes four inputs (two Numbers and two Strings). From the contract, we know `(ellipse 100 50 "outline" "fuchsia")` will evaluate to an Image.

<table>
<thead>
<tr>
<th>Name</th>
<th>Domain</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>; =</td>
<td>:: Number, Number</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(= 3 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; &lt;=</td>
<td>:: Number, Number</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(&lt;= 3 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; &gt;=</td>
<td>:: Number, Number</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(&gt;= 3 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; &lt;&gt;</td>
<td>:: Number, Number</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(&lt;&gt; 3 2)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; string=?</td>
<td>:: String, String</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(string=? &quot;cat&quot; &quot;kitten&quot;)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; string=&gt;?</td>
<td>:: String, String</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(string=&gt;? &quot;ape&quot; &quot;zebra&quot;)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; string&lt;=?</td>
<td>:: String, String</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(string&lt;=? &quot;Abena&quot; &quot;Zoe&quot;)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; string&lt;&gt;?</td>
<td>:: String, String</td>
<td>-&gt; Boolean</td>
</tr>
<tr>
<td>(string&lt;&gt;? &quot;crab&quot; &quot;crawfish&quot;)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>; string-append</td>
<td>:: String, String</td>
<td>-&gt; String</td>
</tr>
<tr>
<td>(string-append &quot;sun&quot; &quot;shine&quot;)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Contracts tell us how to use a function. e.g. ellipse :: Number, Number, String, String -> Image tells us that the name of the function is ellipse, and that it takes four inputs (two numbers and two strings). From the contract we know (ellipse 100 50 "outline" "teal") will evaluate to an Image.

<table>
<thead>
<tr>
<th>Name</th>
<th>Domain</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>triangle</td>
<td>Number, String, String</td>
<td>Image</td>
</tr>
<tr>
<td>rectangle</td>
<td></td>
<td></td>
</tr>
<tr>
<td>square</td>
<td></td>
<td></td>
</tr>
<tr>
<td>circle</td>
<td></td>
<td></td>
</tr>
<tr>
<td>text</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ellipse</td>
<td></td>
<td></td>
</tr>
<tr>
<td>regular-polygon</td>
<td></td>
<td></td>
</tr>
<tr>
<td>rhombus</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Contracts tell us how to use a function. e.g. `ellipse :: Number, Number, String, String -> Image` tells us that the name of the function is `ellipse`, and that it takes four inputs (two Numbers and two Strings). From the contract, we know `(ellipse 100 50 "solid" "darkgreen")` will evaluate to an Image.

<table>
<thead>
<tr>
<th>Name</th>
<th>Domain</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>right-triangle</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>isosceles-triangle</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>radial-star</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>star-polygon</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>triangle/sas</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>triangle/asa</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>image-url</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>(image-url &quot;<a href="https://www.bootstrapworld.org/images/icon.png">https://www.bootstrapworld.org/images/icon.png</a>&quot;)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>scale</td>
<td>:</td>
<td>-&gt;</td>
</tr>
<tr>
<td>rotate</td>
<td>:</td>
<td>-&gt;</td>
</tr>
</tbody>
</table>
Contracts tell us how to use a function. E.g. `ellipse :: Number, Number, String, String -> Image` tells us that the name of the function is `ellipse`, and that it takes four inputs (two Numbers and two Strings). From the contract, we know `(ellipse 100 50 "solid" "lightblue")` will evaluate to an Image.

<table>
<thead>
<tr>
<th>Name</th>
<th>Domain</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>overlay</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>flip-horizontal</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>flip-vertical</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>above</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>beside</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>or</code></td>
<td></td>
<td></td>
</tr>
<tr>
<td><code>and</code></td>
<td></td>
<td>Boolean</td>
</tr>
<tr>
<td><code>or-boolean</code></td>
<td></td>
<td>Boolean</td>
</tr>
<tr>
<td><code>and-boolean</code></td>
<td></td>
<td>Boolean</td>
</tr>
</tbody>
</table>

Both (two Numbers and two Strings) if the contract we know (`ellipse 100 50 "solid" "lightblue"`) will evaluate to an Image.