

Name: \_\_\_\_\_



# Data Science

Fall 2025 Student Workbook - Pyret Edition



# BOOTSTRAP

Equity • Scale • Rigor

Workbook v3.1

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# Pioneers in Computing and Mathematics

The pioneers pictured below are featured in our Computing Needs All Voices lesson. To learn more about them and their contributions, visit <https://bit.ly/bootstrap-pioneers>.



We are in the process of expanding our collection of pioneers. If there's someone else whose work inspires you, please let us know at <https://bit.ly/pioneer-suggestion>.



# Notice and Wonder

Write down what you Notice and Wonder from the [What Most Schools Don't Teach](#) video.  
"Notices" should be statements, not questions. What stood out to you? What do you remember? "Wonders" are questions.

What do you Notice?	What do you Wonder?

# Windows and Mirrors

1) Think about the stories you've just encountered. Identify something(s) from the film and/or posters that served as a mirror for you, connecting you with your own identity and experience of the world. Write about who or what you connected with and why.

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2) Identify something(s) from the film or the posters that served as a window for you, giving you insight into other people's experiences or expanding your thinking in some way.

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# Reflection: Try Thinking About Ketchup

This reflection is designed to follow reading [LA Times Perspective: A solution to tech's lingering diversity problem? Try thinking about ketchup](#)

1) Think of a time when someone else had a strategy or idea that you would never have thought of, but was interesting to you and/or pushed your thinking to a new level.

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2) Think of a time when you had an idea that felt "out of the box". Did you share your idea? Why or why not?

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3) The author argues that tech companies with diverse teams have an advantage. Why?

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4) What suggestions did the article offer for tech companies looking to diversify their teams?

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5) What is one thing of interest to you in the author's bio?

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6) Based on your experience of exceptions to mainstream assumptions, propose another pair of questions that could be used in place of "Where do you keep your ketchup?" and "What would you reach for instead?"

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# Perspective: A solution to tech's lingering diversity problem?

## Try thinking about ketchup

By Dexter Thomas • Published March 16, 2016 6:24 PM PT in the [Los Angeles Times](#)

Diversity is a hot, and controversial, topic in Silicon Valley. But why do so many people care about it?

At first glance, the answer may seem simple: Improving minorities' access to tech jobs is the right thing to do.

But when I moderated a panel Monday at SXSW on diversity in the tech industry, I was surprised none of the panelists talked much about what was "right."

Instead, they talked about what was right for business.

Sarah Wagener, vice president of talent acquisition and diversity at Pandora, agreed during the panel that pushing to hire more diverse candidates is the "right thing" to do.

"But," she said, "it's been the 'right thing to do' for a long time, and we're still having this conversation."

If you're trying to make the case at your company for diversifying your workforce, she said, your argument needs to be focused on "real business outcomes."

In other words, recruiting people from underrepresented backgrounds should be understood not as an obligation that could lower the bar and weigh your company down, but as an opportunity that could raise the bar, and lift your company above the competition.

Instantly, Wagener's statements reminded me of ketchup.

If you haven't heard it yet, the "ketchup question" is a thought experiment that's become something of a meme in some corners of the tech community thanks to a popular episode of the Reply All podcast. It starts as an innocent question:

Where do you keep your ketchup?

If you're like most people in the United States, odds are that you keep your ketchup in the refrigerator. But depending on where you grew up, you might keep it in the cupboard.

Imagine that you reach for the ketchup bottle and find it empty. You need a substitute sauce, and grab whatever is nearby. If that bottle is in the refrigerator, you may opt for mayo. But if it's in the cupboard, the seasoning closest at hand might be malt vinegar, or Tabasco, or salt and pepper.

Start-up culture is often centered around new ways of solving "problems" — ride-sharing apps such as Lyft and Uber solve the problem of getting around town without a car, for example. The "ketchup question" shows how a slight difference in perspective can lead a coworker toward a completely different solution that might never occur to you. That extra perspective could lead to a fresh new idea that could take your company to the top.

But without a diverse team? It's gonna be mayo every time.

What do we do about it?

Most people aren't chief executives of a major company, and may feel like they have no sway in the hiring process.

So I asked two of the panelists to give some suggestions that could be useful for employees of all levels, regardless of the industry in which they work.

Karla Monterroso, vice president of programs at Code 2040, an organization that works to place black and Latino students in engineering internships at tech companies, said that job listings could be an unexpected barrier to attracting diverse talent.

Using seemingly innocent words like "hacker" or "rockstar" in job listings could unintentionally give the impression to some women that the company would not be a hospitable place to work, said Monterroso. She recommended reading articles on the topic of bias and having informal conversations with coworkers.

More directly, she said, using these articles as "evidence" to suggest small changes in recruitment practices could be an easy first step in attracting new talent.

James Talbot, a software engineer at San Francisco web publishing startup Medium, was concerned with what happens after a new recruit is hired. He suggested using social media to follow people who have different perspectives than you, for 30 days. The key, he said, is to listen to what they have to say, simply exposing yourself to their conversations — not commenting or arguing with them.

This is important, he said, because even after a recruiter hires a person from an underrepresented community, adapting to the workplace environment can be another challenge. If people get into a job but have to deal with racist or sexist comments and insensitive treatment, they may simply leave — and take their unique perspectives and talent elsewhere.

People often say that the cause of the lack of diversity in many tech companies is the lack of an easy way to find available candidates.

"People always give excuses, saying the problem is the 'pipeline,'" Talbot said.

"But who wants to be on a pipeline into a sewer?"

*Dexter Thomas is from San Bernardino and is a PhD candidate in East Asian studies at Cornell University. He has taught media studies and Japanese and is writing a book about Japanese hip-hop. Thomas began working in new media as a student director of programming at KUCR-FM (88.3), independently producing podcasts as well as music and news programs. He has written for several outlets internationally on topics as diverse as Internet and youth culture, social justice and video games. He left The Times in 2016.*

(handout)

# Case Study: Ethics, Privacy, and Bias

These questions are designed to accompany one of the case studies provided in the [Ethics, Privacy, and Bias](#)

My Case Study is \_\_\_\_\_

1) Read the case study you were assigned, and write your summary here.

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2) Is this a good thing or a bad thing? Why?

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3) What are the arguments on *each* side?

*Data Science used for this purpose is good because...*

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*Data Science used for this purpose is bad because...*

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# Categorical and Quantitative Data in a Nutshell

Many important questions (“What’s the best restaurant in town?”, “Is this law good for citizens?”, etc.) are answered with *data*. Data Scientists try to answer these questions by writing *programs that ask questions about data*.

Data of all types can be organized into **Tables**.

- Every Table has a **header row** and some number of **data rows**.
- **Quantitative data** is numeric and measures *an amount*, such as a person’s height, a score on a test, distance, etc. A list of quantitative data can be ordered from smallest to largest.
- **Categorical data** is data that specifies *qualities*, such as sex, eye color, country of origin, etc. Categorical data is not subject to the laws of arithmetic — for example, we cannot take the “average” of a list of colors.



# Categorical or Quantitative?

- **Quantitative data** measures an *amount* and can be ordered from smallest to largest.
- **Categorical data** specifies *qualities* and is not subject to the laws of arithmetic — for example, we cannot take the “average” of a list of colors. *Note: Numbers can sometimes be categorical rather than quantitative!*

For each piece of data below, circle whether it is **Categorical** or **Quantitative**.

1)	Hair color	categorical	quantitative
2)	Age	categorical	quantitative
3)	ZIP Code	categorical	quantitative
4)	Date	categorical	quantitative
5)	Height	categorical	quantitative
6)	Sex	categorical	quantitative
7)	Street Name	categorical	quantitative

For each question below, circle whether it will be answered by **Categorical** or **Quantitative** data.

8)	We'd like to find out the average price of cars in a lot.	categorical	quantitative
9)	We'd like to find out the most popular color for cars.	categorical	quantitative
10)	We'd like to find out which puppy is the youngest.	categorical	quantitative
11)	We'd like to find out which cats have been fixed.	categorical	quantitative
12)	We want to know which people have a ZIP code of 02907.	categorical	quantitative

★ We can sort the animals in *ascending order* (smallest-to-largest) by age and then sort the table in *alphabetical order* (A-to-Z) by name.

Does that mean name is a quantitative column? Why or why not? \_\_\_\_\_

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# Questions and Column Descriptions

1) Take some time to look through the Animals Dataset. What stands out to you? Which animals are interesting? What patterns do you notice? Put your observations in the **Notice** column below.

2) Do any of these observations make you wonder? If so, write your question next to the observation in the **Wonder** column. If not, think of another question to write down.

Notice	Wonder	Answered by this dataset?
I notice that <i>Kujo took a long time to be adopted</i>	<i>Is it because he was so big?</i>	Yes No
I notice that		Yes No
I notice that		Yes No
I notice that		Yes No
I notice that		Yes No
I notice that		Yes No
I notice that		Yes No
I notice that		Yes No

Describe the table, and two of the columns, by filling in the blanks below.

1. This dataset is about \_\_\_\_\_; it contains \_\_\_\_\_ data rows.

2. Some of the columns are:

a. \_\_\_\_\_, which contains \_\_\_\_\_ data. Some example values are:  
column name categorical or quantitative

\_\_\_\_\_.

b. \_\_\_\_\_, which contains \_\_\_\_\_ data. Some example values are:  
column name categorical or quantitative

\_\_\_\_\_.

# Opening Questions

## Sports

- Who is the best quarterback of all time?
- Are baseball pitchers throwing harder than ever?
- How much more do male soccer players earn than females?
- How common is it for former Olympic athletes to become coaches?
- How much does an extra inch of height help a basketball player?

## Pop Culture

- What percentage of people have seen the movie that won last year's Best Picture Award?
- Who tends to be more popular: bands or solo singers?
- Are younger actors paid more than older actors?
- Are movies with female leads as profitable as movies with male leads?
- Does winning a Grammy increase sales?

## Politics

- Is "Stop and Frisk" a racist policy?
- Do Republican politicians tend to come from different states than Democratic ones?
- Do people in countries that have universal healthcare live longer than people in countries that don't?
- Was press coverage slanted for or against a particular candidate?

## Education

- Do small schools perform better than large ones?
- Which has a stronger correlation with student achievement: race or wealth?
- Do bilingual classes result in better outcomes for ESL/ELL students?
- How does quality of education differ in various regions of the United States?

# What Questions Can You Answer with the Given Data?

The following is a dataset of a bicycle rider's training rides.

date	miles	time (w/stops)	weather	average speed	max speed
04/10/2018	10	44	"cloudy"	13	30
05/30/2018	15	66	"sunny"	13.5	22
06/12/2018	12	61	"rainy"	11.2	25
07/04/2018	24	103	"sunny"	14	26
07/12/2018	24	120	"windy"	12.5	26

1) Decide whether each questions below *can* or *cannot* be answered with the given data and circle your selection.

Question	Answered by this dataset?	
How many miles did the cyclist ride June 12th?	Yes	No
What tire pressure produces the highest average speed?	Yes	No
What is the average time it takes this cyclist to ride 1 mi?	Yes	No
Does this cyclist ride slower when it is snowing?	Yes	No
Does this cyclist ride faster when they are late to an appointment?	Yes	No
How many miles has the cyclist ridden in total as part of their training?	Yes	No

2) In the space provided below each question, explain *how* you could answer the question using the data or *why you cannot* answer the question.

★ Are there any questions that you could find the answers to more than one way?

(optional)

# Introduction to Programming in a Nutshell

The **Editor** is a software program we use to write Code. Our Editor allows us to experiment with Code on the right-hand side, in the **Interactions Area**. For Code that we want to *keep*, we can put it on the left-hand side in the **Definitions Area**. Clicking the "Run" button causes the computer to re-read everything in the Definitions Area and erase anything that was typed into the Interactions Area.

## Data Types

Programming languages involve different *data types*, such as Numbers, Strings, Booleans, and even Images.

- Numbers are values like `1`, `0.4`, `1/3`, and `-8261.003`.
  - Numbers are *usually* used for quantitative data and other values are *usually* used as categorical data.
  - In Pyret, decimals *must* start with a zero. For example, `0.22` is valid, but `.22` is not.
- Strings are values like `"Emma"`, `"Rosanna"`, `"Jen and Ed"`, or even `"08/28/1980"`.
  - All strings *must* be surrounded by quotation marks.
- Booleans are either `true` or `false`.

All values evaluate to themselves. The program `42` will evaluate to `42`, the String `"Hello"` will evaluate to `"Hello"`, and the Boolean `false` will evaluate to `false`.

## Operators

Operators (like `+`, `-`, `*`, `<`, etc.) work the same way in Pyret that they do in math.

- Operators are written between values, for example: `4 + 2`.
- In Pyret, operators must always have spaces around them. `4 + 2` is valid, but `4+2` is not.
- If an expression has different operators, parentheses must be used to show order of operations. `4 + 2 + 6` and `4 + (2 * 6)` are valid, but `4 + 2 * 6` is not.

## Applying Functions

Functions work much the way they do in math. Every function has a name, takes some inputs, and produces some output. The function name is written first, followed by a list of *arguments* in parentheses.

- In math this could look like  $f(5)$  or  $g(10, 4)$ .
- In Pyret, these examples would be written as `f(5)` and `g(10, 4)`.
- Applying a function to make images would look like `star(50, "solid", "red")`.
- There are many other functions in Pyret, for example `sqr`, `sqrt`, `triangle`, `square`, `string-repeat`, etc.

Functions have *contracts*, which help explain how a function should be used. Every Contract has three parts:

- The *Name* of the function - literally, what it's called.
- The *Domain* of the function - what *type(s) of value(s)* the function consumes, and in what order.
- The *Range* of the function - what *type of value* the function produces.

# Strings and Numbers

Make sure you've loaded [code.pyret.org](http://code.pyret.org) (CPO), clicked "Run", and are working in the **Interactions Area** on the right. Hit Enter/return to evaluate expressions you test out.

## Strings

String values are always in quotes.

- Try typing your name (in quotes!).
- Try typing a sentence like "I'm excited to learn to code!" (in quotes!).
- Try typing your name with the opening quote, but *without the closing quote*. Read the error message!
- Now try typing your name *without any quotes*. Read the error message!

1) Explain what you understand about how strings work in this programming language. \_\_\_\_\_

## Numbers

2) Try typing 42 into the Interactions Area and hitting "Enter". Is 42 the same as "42"? Why or why not?

\_\_\_\_\_

3) What is the largest number the editor can handle?

\_\_\_\_\_

4) Try typing 0.5. Then try typing .5. Then try clicking on the answer. Experiment with other decimals.

Explain what you understand about how decimals work in this programming language. \_\_\_\_\_

\_\_\_\_\_

5) What happens if you try a fraction like 1/3? \_\_\_\_\_

\_\_\_\_\_

6) Try writing **negative** integers, fractions and decimals. What do you learn? \_\_\_\_\_

\_\_\_\_\_

## Operators

7) Just like math, Pyret has **operators** like +, -, \* and /.

Try typing in 4 + 2 and then 4+2 (without the spaces). What can you conclude from this?

\_\_\_\_\_

8) Type in the following expressions, **one at a time**: 4 + 2 \* 6   (4 + 2) \* 6   4 + (2 \* 6)   What do you notice?

\_\_\_\_\_

9) Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this?

\_\_\_\_\_

\_\_\_\_\_



# Booleans

Boolean-producing expressions are yes-or-no questions, and will always evaluate to either **true** ("yes") or **false** ("no").

What will the expressions below evaluate to? Write down your prediction, then type the code into the Interactions Area to see what it returns.

Prediction	Result	Prediction	Result
1) <code>3 &lt;= 4</code>		2) <code>"a" &gt; "b"</code>	
3) <code>3 == 2</code>		4) <code>"a" &lt; "b"</code>	
5) <code>2 &lt; 4</code>		6) <code>"a" == "b"</code>	
7) <code>5 &gt;= 5</code>		8) <code>"a" &lt;&gt; "a"</code>	
9) <code>4 &gt;= 6</code>		10) <code>"a" &gt;= "a"</code>	
11) <code>3 &lt;&gt; 3</code>		12) <code>"a" &lt;&gt; "b"</code>	
13) <code>4 &lt;&gt; 3</code>		14) <code>"a" &gt;= "b"</code>	

15) In your own words, describe what `<` does.

16) In your own words, describe what `>=` does.

17) In your own words, describe what `<>` does.

Prediction:	Result:
18) <code>string-contains("catnap", "cat")</code>	
19) <code>string-contains("cat", "catnap")</code>	

20) In your own words, describe what `string-contains` does. Can you generate another expression using `string-contains` that returns true?

★ There are infinite string values ("a", "aa", "aaa" ...) and infinite number values out there (...-2,-1,0,-1,2...). But how many different *Boolean* values are there?

# Applying Functions

Open [\(code.pyret.org \(CPO\)\)](https://code.pyret.org) and click "Run". We will be working in the Interactions Area on the right.

Test out these two expressions and record what you learn below:

- `regular-polygon(40, 6, "solid", "green")`
- `regular-polygon(80, 5, "outline", "dark-green")`

1) You've seen data types like Numbers, Strings, and Booleans. What data type did the `regular-polygon` function produce? \_\_\_\_\_

2) How would you describe what a regular polygon is? \_\_\_\_\_

3) The `regular-polygon` function takes in four pieces of information (called arguments). Record what you know about them below.

	Data Type	Information it Contains
Argument 1		
Argument 2		
Argument 3		
Argument 4		

There are many other functions available to us in Pyret. We can describe them using **contracts**. The Contract for `regular-polygon` is:

```
# regular-polygon :: Number, Number, String, String -> Image
```

- Each Contract begins with the function name: *in this case* `regular-polygon`
- Lists the data types required to satisfy its Domain: *in this case* `Number, Number, String, String`
- And then declares the data type of the Range it will return: *in this case* `Image`

Contracts can also be written with more detail, by annotating the Domain with *variable names*:

```
# regular-polygon :: ( Number , Number , String , String ) -> Image
                     size   number-of-sides fill-style color
```

4) We know that a square is a regular polygon because \_\_\_\_\_

5) What code would you write to make a big, blue square using the `regular-polygon` function?

```
_____ ( _____ , _____ , _____ , _____ )
      function-name  size :: Number  number-of-sides :: Number  fill-style :: String  color :: String
```

6) Pyret also has a `square` function whose contract is: `# square :: ( Number , String , String ) -> Image`

What code would you write to make a big blue square using the `square` function?

```
_____ ( _____ , _____ , _____ )
      function-name  size :: Number  fill-style :: String  color :: String
```

7) Why does `square` need fewer arguments to make a square than `regular-polygon`? \_\_\_\_\_

★ Where else have you heard the word **contract** used before?

# Practicing Contracts: Domain & Range

Note: The contracts on this page are not defined in Pyret and cannot be tested in the editor.

## is-beach-weather

Consider the following Contract:

```
# is-beach-weather :: Number, String -> Boolean
```

- 1) What is the **Name** of this function? \_\_\_\_\_
- 2) How many arguments are in this function's **Domain**? \_\_\_\_\_
- 3) What is the **Type** of this function's **first argument**? \_\_\_\_\_
- 4) What is the **Type** of this function's **second argument**? \_\_\_\_\_
- 5) What is the **Range** of this function? \_\_\_\_\_

6) Circle the expression below that shows the correct application of this function, based on its Contract.

- A. is-beach-weather(70, 90)
- B. is-beach-weather(80, 100, "cloudy")
- C. is-beach-weather("sunny", 90)
- D. is-beach-weather(90, "stormy weather")

## cylinder

Consider the following Contract:

```
# cylinder :: Number, Number, String -> Image
```

- 7) What is the **Name** of this function? \_\_\_\_\_
- 8) How many arguments are in this function's **Domain**? \_\_\_\_\_
- 9) What is the **Type** of this function's **first argument**? \_\_\_\_\_
- 10) What is the **Type** of this function's **second argument**? \_\_\_\_\_
- 11) What is the **Type** of this function's **third argument**? \_\_\_\_\_
- 12) What is the **Range** of this function? \_\_\_\_\_

13) Circle the expression below that shows the correct application of this function, based on its Contract.

- A. cylinder("red", 10, 60)
- B. cylinder(30, "green")
- C. cylinder(10, 25, "blue")
- D. cylinder(14, "orange", 25)

# Matching Expressions and Contracts

Match the Contract (left) with the expression that uses it correctly (right).

Note: The contracts on this page are not defined in Pyret and cannot be tested in the editor.

Contract		Expression
# make-id :: String, Number -> Image	1	A make-id("Savannah", "Lopez", 32)
# make-id :: String, Number, String -> Image	2	B make-id("Pilar", 17)
# make-id :: String -> Image	3	C make-id("Akemi", 39, "red")
# make-id :: String, String -> Image	4	D make-id("Raissa", "McCracken")
# make-id :: String, String, Number -> Image	5	E make-id("von Einsiedel")

Contract		Expression
# is-capital :: String, String -> Boolean	6	A show-pop("Juneau", "AK", 31848)
# is-capital :: String, String, String -> Boolean	7	B show-pop("San Juan", 395426)
# show-pop :: String, Number -> Image	8	C is-capital("Accra", "Ghana")
# show-pop :: String, String, Number -> Image	9	D show-pop(3751351, "Oklahoma")
# show-pop :: Number, String -> Number	10	E is-capital("Albany", "NY", "USA")

# Contracts for Image-Producing Functions

Log into [code.pyret.org](https://code.pyret.org) (CPO) and click "Run". Experiment with each of the functions listed below in the interactions area. Try to find an expression that produces an image. Record the contract and example code for each function you are able to use!

Name	Domain	Range
# triangle	:: Number, String, String	-> Image
triangle(80, "solid", "darkgreen")		
# star	::	->
# circle	::	->
# rectangle	::	->
# text	::	->
# square	::	->
# rhombus	::	->
# ellipse	::	->
# regular-polygon	::	->
# right-triangle	::	->
# isosceles-triangle	::	->
# radial-star	::	->
# star-polygon	::	->
# triangle-sas	::	->
# triangle-asa	::	->

# Catching Bugs when Making Triangles

## Learning about a Function through Error Messages

- 1) Type `triangle` into the Interactions Area of [code.pyret.org\(CPO\)](http://code.pyret.org(CPO)) and hit "Enter". What do you learn? \_\_\_\_\_
- 2) We know that all functions will need an open parenthesis and at least one input! Type `triangle(80)` in the Interactions Area and hit Enter/return. Read the error message. What hint does it give us about how to use this function?  
\_\_\_\_\_
- 3) Using the hint from the error message, experiment until you can make a triangle. What is the contract for `triangle`?  
\_\_\_\_\_
- 4) Read the explanation below. Then explain the difference in your own words.  
**syntax errors** - when the computer cannot make sense of the code because of unclosed strings, missing commas or parentheses, etc.  
**contract errors** - when the function isn't given what it needs (the wrong type or number of arguments are used)  
The difference between **syntax errors** and **contract errors** is: \_\_\_\_\_  
\_\_\_\_\_

## Finding Mistakes with Error Messages

The following lines of code are all BUGGY! Read the code and the error messages below. See if you can find the mistake WITHOUT typing it into Pyret.



- 5) `triangle(20, "solid" "red")`  
Pyret didn't understand your program around  
`triangle(20, "solid" "red")`  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 6) `triangle(20, "solid")`  
This application expression errored:  
`triangle(20, "solid")`  
2 arguments were passed to the **operator**. The **operator** evaluated to a function accepting 3 parameters. An application expression expects the number of parameters and arguments to be the same.  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 7) `triangle(20, 10, "solid", "red")`  
This application expression errored:  
`triangle(20, 10, "solid", "red")`  
4 arguments were passed to the **operator**. The **operator** evaluated to a function accepting 3 parameters. An application expression expects the number of parameters and arguments to be the same.  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 8) `triangle (20, "solid", "red")`  
Pyret thinks this code is probably a function call:  
`triangle (20, "solid", "red")`  
Function calls must not have space between the **function expression** and the arguments.  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax




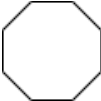
# Using Contracts

For questions 1,2,4,5,8 & 9, use the contracts provided to find expressions that will generate images similar to the ones pictured.  
Test your code in [code.pyret.org\(CPO\)](http://code.pyret.org(CPO)) before recording it.



```
# ellipse :: ( Number  
               width      , Number  
                           height , String  
                               fill-style , String  
                                       color ) -> Image
```

1)		
2)		
3)	Write an expression using <code>ellipse</code> to produce a circle.	

```
# regular-polygon :: ( Number  
                      side-length , Number  
                                number-of-sides , String  
                                                    fill-style , String  
                                                            color ) -> Image
```

4)		
5)		
6)	Use <code>regular-polygon</code> to write an expression for a square!	
7)	How would you describe a <b>regular polygon</b> to a friend?	

```
# rhombus :: ( Number  
              size , Number  
                  top-angle , String  
                              fill-style , String  
                                      color ) -> Image
```

8)		
9)		
10)	Write an expression to generate a <code>rhombus</code> that is a square!	

# Triangle Contracts

Respond to the questions. Go to [code.pyret.org\(CPO\)](http://code.pyret.org(CPO)) to test your code.

1) What kind of triangle does the `triangle` function produce? \_\_\_\_\_  
There are lots of other kinds of triangles! And Pyret has lots of other functions that make triangles!

```
# triangle :: (Number, String, String) -> Image
               size      fill-style  color
# right-triangle :: (Number, Number, String, String) -> Image
                   base    height   fill-style  color
# isosceles-triangle :: (Number, Number, String, String) -> Image
                       leg     angle  fill-style  color
```

2) Why do you think `triangle` only needs one number, while `right-triangle` and `isosceles-triangle` need two numbers?

---

---

3) Write `right-triangle` expressions for the images below using `100` as one argument for each.



---



---

4) Write `isosceles-triangle` expressions for the images below using `100` as one argument for each.



---



---

5) Write 2 expressions that would build **right-isosceles** triangles. Use `right-triangle` for one expression and `isosceles-triangle` for the other expression.



---

---

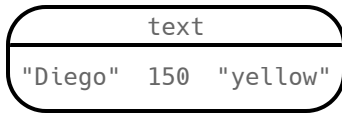
6) Which do you like better? Why? \_\_\_\_\_

# Composing with Circles of Evaluation

## Notice and Wonder

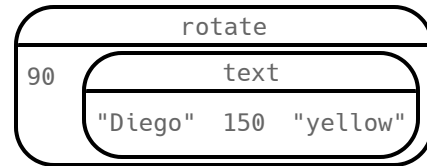
Suppose we want to see the `text` "Diego" written vertically in yellow letters of size 150. Let's use Circles of Evaluation to look at the structure:

We can start by generating the Diego image.



```
text("Diego", 150, "yellow")
```

And then use the `rotate` function to rotate it 90 degrees.



```
rotate(90, text("Diego", 150, "yellow"))
```

1) What do you Notice? \_\_\_\_\_

2) What do you Wonder? \_\_\_\_\_

## Let's Rotate an Image of Your Name!

Suppose you wanted the computer to show your name in your favorite color and rotate it so that it's diagonal...

Write your name (any size), in your favorite color

3) Draw the circle of evaluation:

`rotate` the image so that it's diagonal

4) Draw the circle of evaluation:

5) Convert the Circle of Evaluation to code:

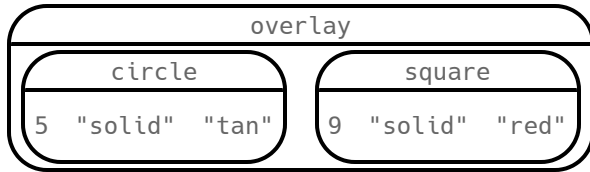
6) Convert the Circle of Evaluation to code:

# Circle of Evaluation to Code (Scaffolded)

## Complete the Code by Filling in the Blanks!

Finish the Code by filling in the blanks.

1)

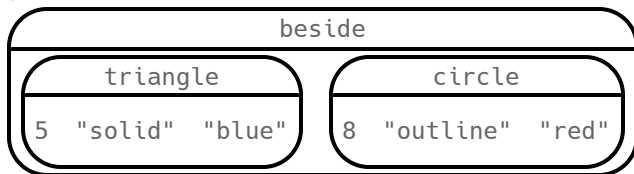


overlay(circle(\_\_\_\_, "solid", \_\_\_\_\_), \_\_\_\_\_(9, \_\_\_\_\_, "red"))

## Complete the Code by adding Parentheses

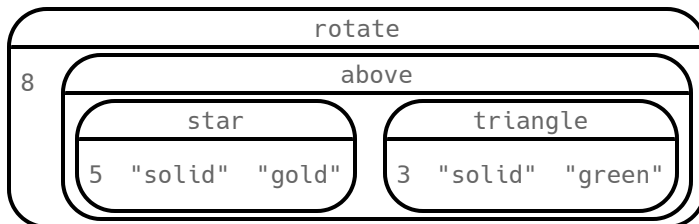
For each Circle of Evaluation, finish the Code by adding parentheses and commas.

2)



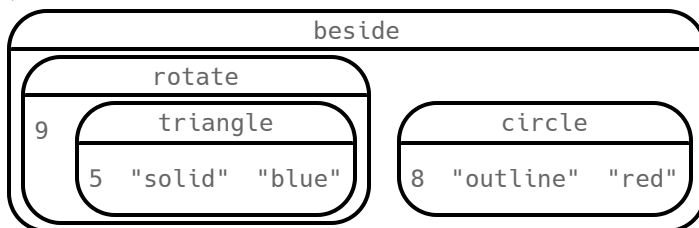
beside triangle 5 "solid" "blue" circle 8 "outline" "red"

3)



rotate 8 above star 5 "solid" "gold" triangle 3 "solid" "green"

4)



beside rotate 9 triangle 5 "solid" "blue" circle 8 "outline" "red"

# Frayer Model: Domain and Range

My Definition			Facts and Characteristics
<b>Domain</b>			
Examples			Non-Examples
My Definition			Facts and Characteristics
<b>Range</b>			
Examples			Non-Examples

(optional)

# Frayer Model: Function and Variable

My Definition		Facts and Characteristics
<b>Function</b>		
Examples		Non-Examples
<b>Variable</b>		
My Definition		Facts and Characteristics
Examples		Non-Examples

(optional)



# Radial Star

# radial-star :: ( Number  
points, Number  
outer-radius, Number  
inner-radius, String  
fill-style, String  
color ) -> Image

Using the Contract above, match the images on the left to the expressions on the right. Test the code at [code.pyret.org\(CPO\)](https://code.pyret.org/CPO).



1

A

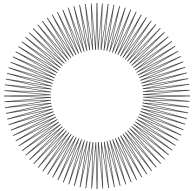
```
radial-star(5, 200, 50, "solid", "black")
```



2

B

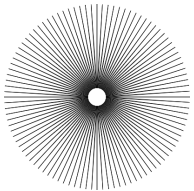
```
radial-star(7, 200, 100, "solid", "black")
```



3

C

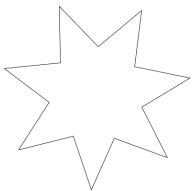
```
radial-star(7, 200, 100, "outline", "black")
```



4

D

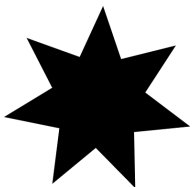
```
radial-star(10, 200, 150, "solid", "black")
```



5

E

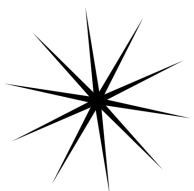
```
radial-star(10, 200, 20, "solid", "black")
```



6

F

```
radial-star(100, 200, 20, "outline", "black")
```



7

G

```
radial-star(100, 200, 100, "outline", "black")
```

(optional)

# Triangle Contracts (SAS & ASA)

Type each expression (left) below into the [code.pyret.org \(CPO\)](https://code.pyret.org/CPO/), and match it to the image it creates (right).

Expression			Image
<code>triangle-sas(120, 45, 70, "solid", "black")</code>	1	A	
<code>triangle-sas(120, 90, 70, "solid", "black")</code>	2	B	
<code>triangle-sas(120, 135, 70, "solid", "black")</code>	3	C	
<code>triangle-sas(70, 135, 120, "solid", "black")</code>	4	D	

## Contracts

Think about how you would describe each `triangle-sas` argument to someone who'd never used the function before.

5) Annotate the Contract below using descriptive variable names.

```
triangle-sas :: ( Number , Number , Number , String , String ) -> Image
```

*If you have a printed workbook, add examples of each of the triangle functions we've explored to your contracts pages.*

★ If you have time, experiment with the `triangle-asa` function.

```
# triangle-asa :: ( Number , Number , Number , String , String ) -> Image
                  top-left-angle left-side bottom-angle fill-style color
```

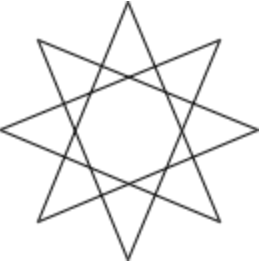
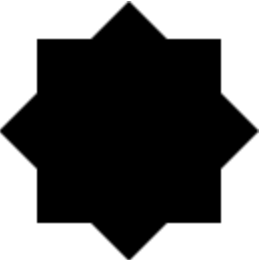
★ Why did these two functions need to take in one more Number than `right-triangle` did?

---

# Star Polygon

```
# star-polygon :: ( Number  
side-length , Number  
points-on-polygon , Number  
points-to-skip-for-star , String  
fill-style , String  
color ) -> Image
```

1. Using the Contract above, write expressions to create images like those pictured below.
2. Go to [\(CPO\)](http://code.pyret.org) to test your code.
3. Then write expressions to generate two more star polygons of your choosing.  
Sketch them and record your working code.

1		<hr/>
2		<hr/>
3		<hr/>
4		<hr/>

(optional)

# Rubric: Create Your Own Logo

Important: Students, be sure to submit all three components of this project, including (1) Sample Logo Study worksheet, (2) Designing Your Logo worksheet, (3) Coding Your Logo worksheet and (4) your published Pyret program link.

	❑ Wow!	❑ Getting There	❑ Needs Improvement
Sample Logo Study	I described my favorite logo fully, and explained why I like it. I listed each and every specific color, image-producing function, and transformation function that the programmer used. I did not leave out any details.	I described my favorite logo and explained why I like it. When I listed the functions that the programmer used, however, I missed one or two.	My description of why I like a certain logo was brief. My list of the functions used by the programmer left out three or more functions.
Drawing my Logo	My logo sketch is attractive and creative. I've annotated the shapes and colors I plan to use.	My logo sketch is attractive and creative, when I annotated, I forgot to label one or two shape and color names.	My logo sketch looks nice, but I forgot to annotate three or more shape or color names.
Circle of Evaluation	My Circle of Evaluation shows my very best attempt to compose the functions in my logo. Every Circle has a function at the top and the order in which the functions are to be combined is clear and logical.	My Circle of Evaluation shows a solid attempt to compose the functions in my logo but some logic, organization or details could be clearer.	My Circle of Evaluation is hard for the reader to interpret.
My Logo Program Submission	Running my code produces no errors. The logo that appears after typing in my - Logo looks very close to my drawing. I've commented thoughtfully on the thinking behind my logo.	Running my code produces no errors. The logo that appears after typing in my - Logo sort of looks like my drawing. My explanation is brief.	Running my code produces errors. The logo that appears after typing in my - Logo doesn't really look like my drawing. I forgot to include responses to the reflection question.

(handout)

# Logo Study

We're going to look at three logos made by Bootstrap students in San Diego. Open the [Logos Starter File](#) and click "Run". Type `sample-logo-1` in the Interactions Area (right side) and hit enter, then repeat for the other sample logos.

1) Which logo's **picture** looks the most complex to you? \_\_\_\_\_

2) Which logo's **code** looks the most complex to you? \_\_\_\_\_

3) Which logo was your favorite? \_\_\_\_\_ What did you like about it? \_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

4) Look at the code for the logo you chose in the previous question. List all of the *colors* that the programmer used to create this logo.

\_\_\_\_\_

\_\_\_\_\_

5) List all of the *image-producing functions* (`triangle`, `rectangle`, etc.) that the programmer used to create this logo.

\_\_\_\_\_

\_\_\_\_\_

6) List all of the *image-transforming functions* (`above`, `rotate`, etc.) that the programmer used to create this logo.

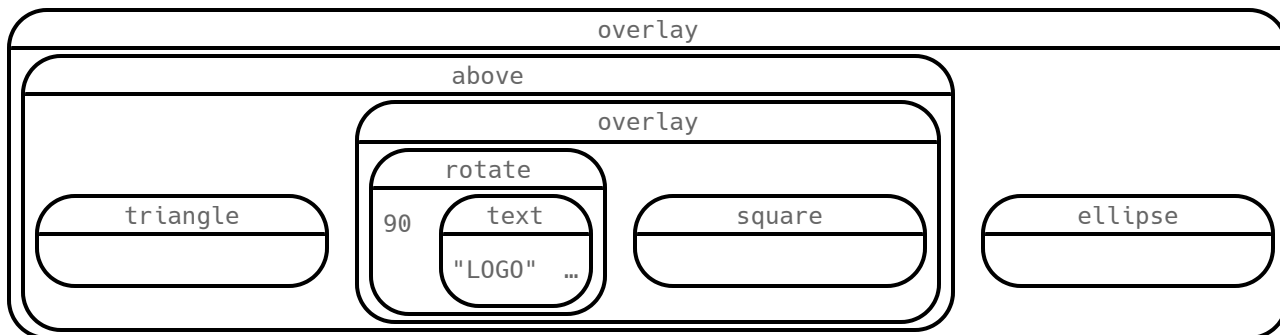
\_\_\_\_\_

\_\_\_\_\_

7) How many layers does this logo have? ( *Note: When 2 images sit beside each other, they are in the same layer.* ) \_\_\_\_\_

8) When thinking through complex code, it can be helpful to use simplified versions of Circles of Evaluation that show the structure but not the nitty gritty details of colors and sizes of shapes.

Make a rough sketch of a logo that would satisfy the vision represented by the Circle of Evaluation below.



# Designing Your Logo

## Design Your Logo

1) It's your turn! Think about what makes the logos you discussed memorable. In the space below (or on a separate page), draw a logo or design to represent yourself, a friend, an activity - it's up to you.

2) Choose specific [colors](#) for your logo! If something is "tomato" or "chocolate", draw an arrow to the appropriate region and label it with the color's name.

## Plan Your Logo's Code

Let's think more deeply about the logo we are going to create. Refer to your logo drawing in order to respond to the prompts below.

3) Put a check mark by each of the **shape functions** that you are going to include in your logo. **You must choose at least two!** If you plan to use a function multiple times, you can add additional check marks next to it.

<input type="checkbox"/> circle	<input type="checkbox"/> ellipse	<input type="checkbox"/> square	<input type="checkbox"/> rectangle
<input type="checkbox"/> text	<input type="checkbox"/> rhombus	<input type="checkbox"/> triangle	<input type="checkbox"/> radial-star

4) Put a check mark by each of the **transformation functions** that you are going to use in your logo. **You must choose at least two!** If you plan to use a function multiple times, you can add additional check marks next to it.

<input type="checkbox"/> above	<input type="checkbox"/> beside	<input type="checkbox"/> flip-horizontal	<input type="checkbox"/> flip-vertical
<input type="checkbox"/> rotate	<input type="checkbox"/> scale	<input type="checkbox"/> overlay	

## Peer Review - Swap Papers with a Partner!

5) Write your name on the line so that your teacher knows who is reviewing this design. \_\_\_\_\_

6) What do you like about this logo? \_\_\_\_\_

7) What suggestions do you have to make the logo even better? \_\_\_\_\_

8) Did your partner correctly label all colors and shapes? If no, explain what they missed. \_\_\_\_\_

9) Did your partner correctly choose their shape functions? How about their transformation functions? \_\_\_\_\_

10) Return this paper to its owner! Verbally share any additional feedback.

# Coding Your Logo

## Represent Your Logo with a Circle of Evaluation

1) Draw a Circle of Evaluation to show how you will compose the functions you selected in order to create your logo. If you need more space, use a separate sheet of paper.

## Peer Review - Swap papers with a partner! ( *Trade this page and your logo sketch.* )

2) Write your name on the line so that your teacher knows who is reviewing this design. \_\_\_\_\_

3) Did your partner put a function at the top of each Circle? If no, explain what the problem is. \_\_\_\_\_

4) When you compare the Circles of Evaluation to your partner's logo sketch, do they match up? Or would the Circle produce an image different than the sketch? \_\_\_\_\_  
\_\_\_\_\_

5) Are there any syntax errors (strings missing quotation marks, decimals without at least one number before the decimal point, etc.)? If so, where? \_\_\_\_\_  
\_\_\_\_\_

## Put Your Logo's Code in Pyret

You'll need the [Logos Starter File](#) open on your computer.

6) In the Definitions Area (left side), type `my-logo = ...`, replacing the `...` with the code represented by your Circles of Evaluation. This defines the variable name `my-logo` to be *your logo image* !

7) Test it out! Click "Run" and type `my-logo` into the *Interactions Area* . If you get an error, read the message and resolve it. If the logo doesn't look like the one you drew, try again until it works. Describe one adjustment that you made to your code. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

8) Add a comment to the Definitions Area describing why you designed your logo the way you did.

9) What did you learn from completing this project? \_\_\_\_\_  
\_\_\_\_\_

10) **Save your program!** Select "File", then "Save a Copy." Go to "Publish", and copy the link that appears. Follow your teacher's instructions and submit the link.

## Sorting and Summarizing Tables

Open the [Animals Starter File](#) and click "Run". In the Interactions Area (right), type `animals-table`. Hit "Enter" to see the default view of the table.

## Ordering a Table with `sort`

1) Mabel Lee wants to sort this table by **age** (youngest-to-oldest). Juan Carlos wants to sort the table by **pounds** (heaviest-to-lightest). What are some other ways we could sort the table?

- a. \_\_\_\_\_
- b. \_\_\_\_\_

Pyret has a function called `sort` that will produce sorted Tables!

2) Test out `sort(animals-table, "age", true)` in the Interactions Area. Try using `false` instead of `true`. Complete the sentences below by **circling** the behavior you observed for each Boolean.

- |                                     |  |   |
|-------------------------------------|--|---|
| (a) <b>true</b> sorts the table...  | in <b>ascending order</b> (from least to greatest) | in <b>descending order</b> (from largest to smallest) |
| (b) <b>false</b> sorts the table... | in <b>ascending order</b> (from least to greatest) | in <b>descending order</b> (from largest to smallest) |

3) The Domain of `sort` has three inputs. One of them is the table itself. Can you identify the data types of the other two?

```
# sort :: ( Table, column-name, order ) -> Table
```

4) What code will sort the animals by alphabetical order of their *names*? \_\_\_\_\_

5) Did you use **true** or **false**? Explain why. \_\_\_\_\_

## Summarizing a Column with count

Let's explore another table function, beginning with its contract:

```
# count :: Table, String -> Table
```

6) What do you expect the code `count(animals-table, "legs")` to produce? \_\_\_\_\_

Type the code into the Interactions Area and click "Enter" to test it out.

7) How many animals had 4 legs? \_\_\_\_\_

8) Think of another question you might be able to answer by making a different table using the `count` function.

9) Fill in the blanks with the code to make the table: \_\_\_\_\_ ( \_\_\_\_\_, \_\_\_\_\_ )

function-name                      table-name :: Table                      column-name :: String

10) Try using the `count` function to summarize the `pounds` column. Is the resulting summary useful? Why or why not?

11) Tables that summarize data with a count are commonly used in the real world. Write an example of where you've seen them before:

12) Newspapers often incorporate data into their reporting. How else might they display this information, besides using a table?



# Functions for Tables (continued)

## Grabbing a Single Row

In addition to Numbers, Strings, Booleans, Images and Tables, Pyret has a **data type** for an individual **Row**.

Open the [Animals Starter File](#) and click "Run". In the Interactions Area (right), type `animals-table`. Hit "Enter" to see the default view of the table. Then type `row-n(animals-table, 2)` and compare the result to the table.

- 1) Write the code that generates the first row of the table. \_\_\_\_\_
- 2) Explain what the second input to `row-n` means, in as much detail as possible. \_\_\_\_\_  
\_\_\_\_\_

## Grabbing Multiple Rows

- 3) Type `first-n-rows(animals-table, 5)`. What happens? \_\_\_\_\_
- 4) If we wanted a table of the first 3 rows of the `animals-table`, what code would we write? \_\_\_\_\_
- 5) What is the Contract for `first-n-rows`? \_\_\_\_\_

## Defining Values

Pyret lets us **define** values that we want to use later. We can define any kind of values we like!

- 6) If we tell Pyret that `x = 4 * 2`, what would you expect to get back when you type `x + 1`? \_\_\_\_\_  
Test it out by typing `x = 4 * 2` into the Interactions Area, hitting "Enter" and then typing `x + 1`.
  - 7) Try typing `gt = triangle(50, "solid", "green")` and hitting "Enter".  
What happens? \_\_\_\_\_  
Now type `gt`. What do you get back? \_\_\_\_\_
  - 8) Explain what is happening on Line 14 of the [Animals Starter File](#). \_\_\_\_\_  
\_\_\_\_\_
  - 9) On line 16 of the Definitions Area, add a new definition called `my-pet`, which is defined to be your favorite animal.  
code: \_\_\_\_\_
  - 10) Add a new line at the bottom of the Definitions Area, define `first-3` to be a subset of the first 3 rows of the `animals-table`.  
code: \_\_\_\_\_
- ★ What happens when you type `first-n-rows(sort(animals-table, "pounds", true), 5)`? \_\_\_\_\_  
\_\_\_\_\_

*Note: In this case, the output of `sort(animals-table, "pounds", true)` is the Table `first-n-rows` is taking in!*

- ★★ See if you can figure out how to compose the code that would generate a table of the 10 oldest animals!

\_\_\_\_\_ ( \_\_\_\_\_ , \_\_\_\_\_ )  
function-name Table Number

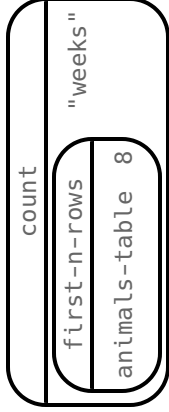
# Matching Descriptions to Circles of Evaluation: sort, count, first-n-rows

Match each prompt on the left to the Circle of Evaluation used to answer it.

We want to see the 8 lightest animals.

1

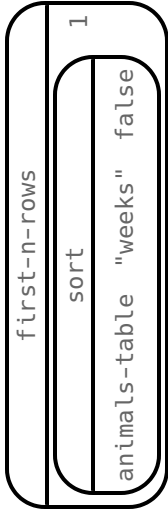
A



We want to see the animal who was adopted the quickest.

2

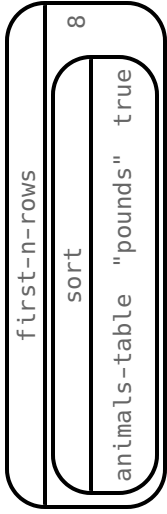
B



We want to take the first 8 animals from the table and order them from heaviest to lightest.

3

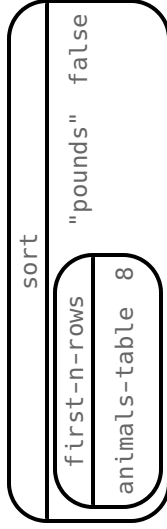
C



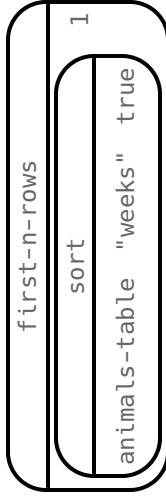
We want to know the count by weeks to adoption of the first 8 animals.

4

D



E



★ Translate each Circle of Evaluation into code and test it out in the [Animals Starter File](#) to confirm it does what you'd expect it to.

Hint: The Code for A is `count(first-n-rows(animals-table, 8), "weeks")`

# Circles of Evaluation: Count, Sort, First-n-rows

For each scenario below, draw the Circle of Evaluation and then use it to write the code.

When you're done, test your code out in the [Animals Starter File](#) and make sure it does what you'd expect it to.

```
# count :: Table, String -> Table
```

```
# first-n-rows :: Table, Number -> Table
```

```
# sort :: Table, String, Boolean -> Table
```

1) We want to see the 10 animals who were adopted the quickest.

Circle of Evaluation:

code: \_\_\_\_\_

2) We want to see the heaviest animal.

Circle of Evaluation:

code: \_\_\_\_\_

3) We want to take the first 8 animals from the table and put them in alphabetical order (by name).

Circle of Evaluation:

code: \_\_\_\_\_

4) You notice that the lightest 16 animals weigh under 10 pounds and you want to know the count (*by species*) of those animals.

Circle of Evaluation:

code: \_\_\_\_\_

# Catching Bugs when Sorting Tables

## Learning about a Function through Error Messages

- 1) Type `sort` into the Interactions Area of the [Animals Starter File](#) and hit "Enter". What do you learn? \_\_\_\_\_
- 2) We know that all functions need an open parenthesis and at least one input! Type `sort(animals-table)` in the Interactions Area and hit Enter. Read the error message. What hint does it give us about how to use this function?  
\_\_\_\_\_
- 3) Read the explanations below. Then explain the difference in your own words.  
**syntax errors** - when the computer cannot make sense of the code because of unclosed strings, missing commas or parentheses, etc.  
**contract errors** - when the function isn't given what it needs (the wrong type or number of arguments are used)

The difference between **syntax errors** and **contract errors** is: \_\_\_\_\_

## Finding Mistakes with Error Messages

The code below is **BUGGY!** Read the code and the error messages, and see if you can catch the mistake **WITHOUT** typing the code into Pyret.

- 4) `sort(animals-table, "name", true)`  
Pyret didn't expect your program to end as soon as it did:  
`sort(animals-table, "name", true`  
You may be missing an "end", or closing punctuation like ")" or "]" somewhere in your program.  
  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 5) `sort(animals-table "name" true)`  
Pyret didn't understand your program around:  
`sort(animals-table "name" true)`  
You may need to add or remove some text to fix your program. Look carefully before **the highlighted text**. Is there a missing colon (:), comma (,), string marker ("), or keyword? Is there something there that shouldn't be?  
  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 6) `sort(animals-table, "name" , "true")`  
The **Boolean annotation**:  
`fun sort(t :: Table, col :: String, asc :: Boolean)`  
was not satisfied by the value  
"true"  
  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 7) `sort(animals-table, name , true)`  
The name **name** is unbound:  
`sort(animals-table, name , true)`  
It is **used** but not previously defined.  
  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax
- 8) `sort (animals-table, "name", true)`  
Pyret thinks this code is probably a function call:  
`sort (animals-table, "name", true)`  
Function calls must not have space between the **function expression** and the arguments.  
  
This is a \_\_\_\_\_ error. The problem is that \_\_\_\_\_  
contract / syntax

# Exploring Data Visualizations

Use the contracts provided below to make each type of display in the [Animals Starter File](#). Then answer the questions about each display.

<b>Bar Charts:</b> <b># bar-chart :: Table, String -&gt; Image</b>	
<div style="border-bottom: 1px solid black; margin-bottom: 5px;"> <span style="float: left;">_____</span> <span style="float: right;">_____</span> <span style="clear: both;">function-name ( table-name :: Table , column-name :: String )</span> </div>	
Sketch a bar chart below.	Bar charts summarize 1 column of _____ data. This kind of display tells us... <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div> <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div>
<b>Pie Charts:</b> <b># pie-chart :: Table, String -&gt; Image</b>	
<div style="border-bottom: 1px solid black; margin-bottom: 5px;"> <span style="float: left;">_____</span> <span style="float: right;">_____</span> <span style="clear: both;">function-name ( table-name :: Table , column-name :: String )</span> </div>	
Sketch a pie chart below.	Pie charts summarize 1 column of _____ data. This kind of display tells us... <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div> <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div>
<b>Dot Plots:</b> <b># dot-plot :: Table, String, String -&gt; Image</b>	
<div style="border-bottom: 1px solid black; margin-bottom: 5px;"> <span style="float: left;">_____</span> <span style="float: right;">_____</span> <span style="clear: both;">function-name ( table-name :: Table , labels :: String , values :: String )</span> </div>	
Sketch a dot plot below.	Dot plots summarize 1 column of _____ data. This kind of display tells us... <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div> <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div>
<b>Histograms:</b> <b># histogram :: Table, String, String, Number -&gt; Image</b>	
<div style="border-bottom: 1px solid black; margin-bottom: 5px;"> <span style="float: left;">_____</span> <span style="float: right;">_____</span> <span style="clear: both;">function-name ( table-name :: Table , labels :: String , values :: String , bin-width :: Number )</span> </div>	
Sketch a histogram below.	Histograms summarize 1 column of _____ data. This kind of display tells us... <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div> <div style="border-bottom: 1px solid black; height: 20px; margin-top: 10px;"></div>

# Composing Functions: Match Descriptions to Circles of Evaluation

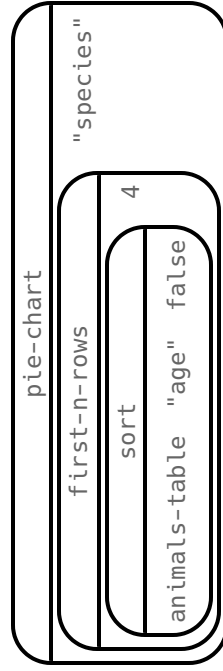
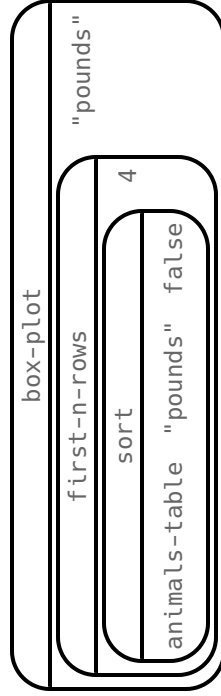
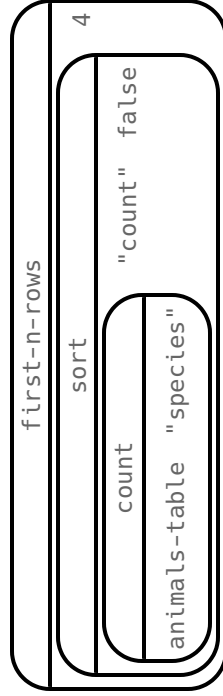
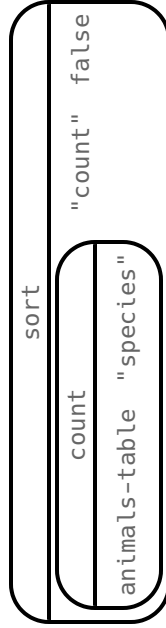
Match each prompt on the left to the Circle of Evaluation used to answer it.

1 Make a pie-chart, showing the species of the 4 oldest animals.

2 Take the 4 heaviest animals and make a box plot of their weight.

3 Make a table showing the count of the species in this dataset, sorted from most to least.

4 Make a table showing the count of the 4 species with the most animals



# Circles of Evaluation: Composing Functions to Make Visualizations

Using the Contracts below as a reference, draw the Circle of Evaluation for each prompt.

# pie-chart :: Table, String -> Image

# bar-chart :: Table, String -> Image

# dot-plot :: Table, String -> Image

# box-plot :: Table, String -> Image

# first-n-rows :: Table, Number -> Table

# sort :: Table, String, Boolean -> Table

1) Make a bar-chart of the lightest 16 animals by sex.

★ What other bar chart might you want to compare this to? \_\_\_\_\_

2) Take the heaviest 20 animals and make a dot plot of weeks to adoption.

★ What other histogram might you want to compare this to? \_\_\_\_\_

3) Make a box-plot of age for the 11 animals who spent the most weeks in the shelter.

★ What other box plot might you want to compare this to? \_\_\_\_\_

4) Make a pie-chart of species for the 18 animals who spent the fewest weeks in the shelter.

★ What other pie chart might you want to compare this to? \_\_\_\_\_

# Exploring Data Visualizations (2)

Use the contracts provided below to make each type of display in the [Animals Starter File](#). Then answer the questions about each display.

Line Graphs: # line-graph :: Table, String, String, String -> Image	
<div><div>function-name</div><div>(</div><div>table-name :: Table</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>)</div></div>	
Sketch a line graph below.	<div>Line Graphs summarize 2 columns of <div>categorical/quantitative</div> data.</div> <div>This kind of display tells us...</div> <div></div> <div></div> <div></div>

Scatter Plots: # scatter-plot :: Table, String, String, String -> Image	
<div><div>function-name</div><div>(</div><div>table-name :: Table</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>)</div></div>	
Sketch a scatter plot below.	<div>Scatter Plots summarize 2 columns of <div>categorical/quantitative</div> data.</div> <div>This kind of display tells us...</div> <div></div> <div></div> <div></div>

LR Plots: # lr-plot :: Table, String, String, String -> Image	
<div><div>function-name</div><div>(</div><div>table-name :: Table</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>,</div><div>column-name :: String</div><div>)</div></div>	
Sketch an Linear Regression Plot below.	<div>LR Plots summarize 2 columns of <div>categorical/quantitative</div> data.</div> <div>This kind of display tells us...</div> <div></div> <div></div> <div></div>



# Circles of Evaluation: Composing Functions to Make Visualizations (2)

Using the Contracts below as a reference, draw the Circle of Evaluation for each prompt.

# pie-chart :: Table, String -> Image

# bar-chart :: Table, String -> Image

# histogram :: Table, String, String, Number -> Image

# box-plot :: Table, String -> Image

# first-n-rows :: Table, Number -> Table

# sort :: Table, String, Boolean -> Table

1) Take the youngest 12 animals and make a box-plot of pounds.

What other box plot might you want to compare this to? \_\_\_\_\_

2) Make a pie-chart of legs for the 10 oldest animals.

What other pie chart might you want to compare this to? \_\_\_\_\_

★ Take the 20 lightest animals, then take the 10 youngest of *those* animals and make a bar-chart of species

What other pie chart might you want to compare this to? \_\_\_\_\_

(optional)

# Displaying Categorical Data in a Nutshell

Data Scientists use **data visualizations** to interpret data. You've probably seen some of these charts, graphs and plots yourselves!

When it comes to displaying **Categorical Data**, there are two visualizations that are especially useful:

1. **Bar charts** show the *count or percentage* of rows in each category.

- Bar charts provide a visual representation of the frequency of values in a categorical column.
- Bar charts have a bar for every category in a column.
- The more rows in a category, the taller the bar.
- Bars in a bar chart can be shown in *any order*, without changing the meaning of the chart. However, bars are usually shown in some sensible order (bars for the number of orders for different t-shirt sizes might be presented in order of smallest to largest shirt).

2. **Pie charts** show the *percentage* of rows in each category.

- Pie charts provide a visual representation of the relative frequency of values in a categorical column.
- Pie charts have a slice for every category in a column.
- The more rows in a category, the larger the slice.
- Slices in a pie chart can be shown in *any order*, without changing the meaning of the chart. However, slices are usually shown in some sensible order (e.g. slices might be shown in alphabetical order or from the smallest to largest slice).

# Frequency Tables, Bar Charts and Pie Charts

Open the [Expanded Animals Starter File](#) and click "Run".

## Part 1 - Visualizations for Categorical Data

Test the following expressions in the Interactions Area:

- `count(more-animals, "species")`
- `bar-chart(more-animals, "species")`

1) How are they similar? \_\_\_\_\_

2) Which do you like better: the bar chart or the frequency table? Why? \_\_\_\_\_

Now test out the expression `pie-chart(more-animals, "species")`

3) How does the pie chart connect to the bar chart you just made?

Note: When you first build a bar chart or pie chart in Pyret, they are interactive visualizations. That means that you can mouse over them for more information. Hit the up arrow in the interactions area to reload your last expression and test it out!

## Part 2 - Comparing Bar and Pie Charts

Best completed after [Bar & Pie Chart - Notice and Wonder](#) and [Matching Bar and Pie Charts](#).

4) How are pie charts similar to bar charts?

5) How are pie charts and bar charts different?

6) What information is provided in bar charts that is hidden in pie charts?

7) Why might this sometimes be problematic?

8) When would you want to use one chart instead of another?

## C - Bar and Pie Charts for Quantitative Data?

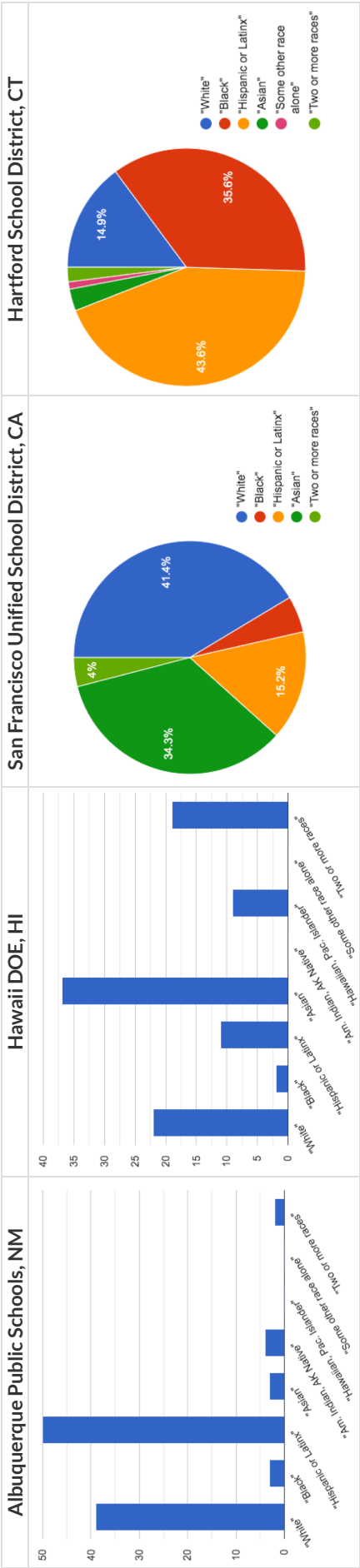
9) Make a `pie-chart` and `bar-chart` for the `pounds` column. Why isn't grouping the `pounds` column very useful?

10) Look at the list of columns in the Definitions Area. For which columns do you expect pie charts to be most useful?

★ What questions about the dataset are you curious to investigate using these visualizations?

# Bar & Pie Chart - Notice and Wonder

What do you Notice and Wonder about the visualizations below?



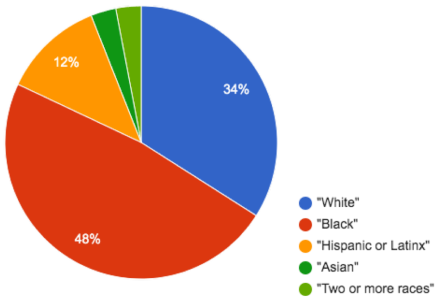
What do you Notice?

What do you Wonder?

# Matching Bar and Pie Charts

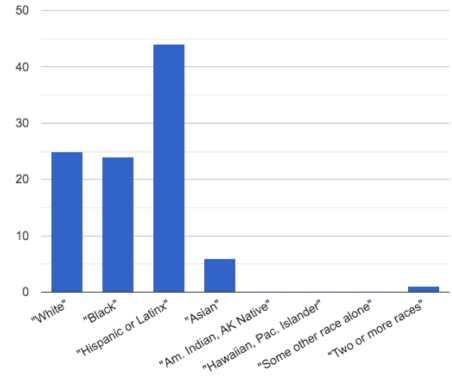
Match each bar chart below to the pie chart that visualizes the racial demographic data from the same school district.

Cleveland Municipal School District

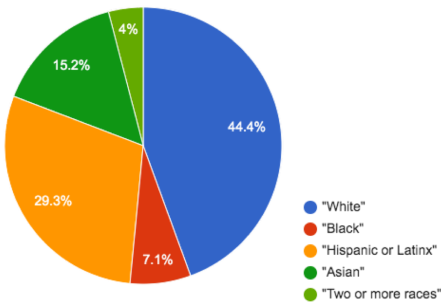


1

A

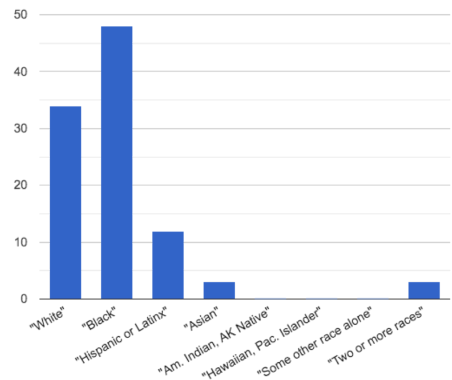


San Diego City Unified School District

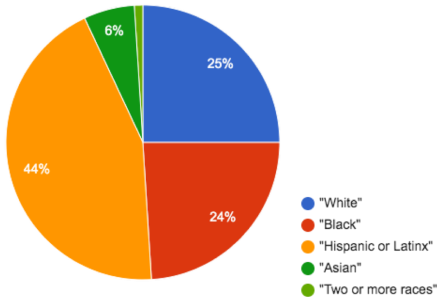


2

B

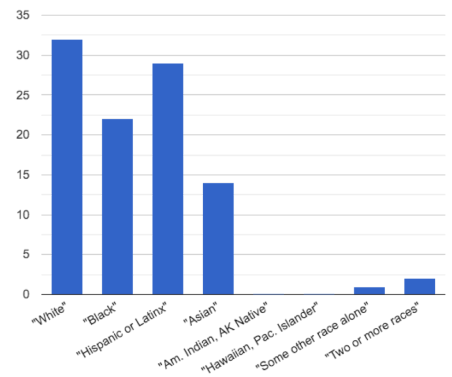


Houston Independent School District

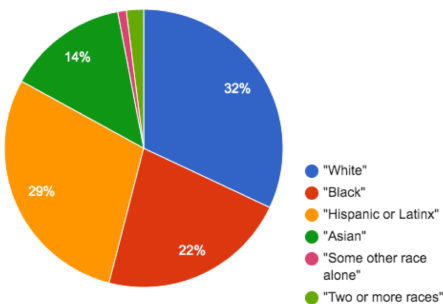


3

C

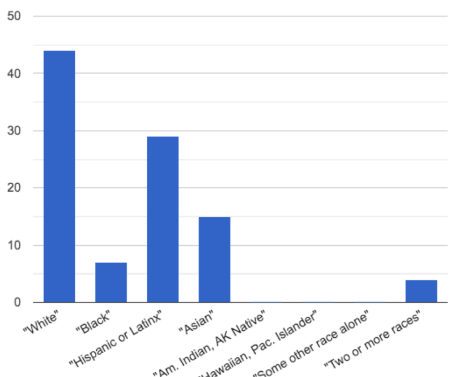


New York City Dept of Education



4

D



# Introducing Visualizations for Subgroups

This page is designed to be used with the [Expanded Animals Starter File](#).

## Part A

1) How many tarantulas are male? \_\_\_\_\_

*Hint: Sort the table by species!*

2) How many tarantulas are female? \_\_\_\_\_

3) Would you imagine that the distribution of male and female animals will be similar for every species at the shelter? Why or why not?

---

---

## Part B

Sometimes we want to compare *sub-groups across groups*. In this example, we want to compare the distribution of sexes across each species.

Fortunately, Pyret has two functions that let us specify both a group and a subgroup:

```
# stacked-bar-chart :: ( Table , String , String ) -> Image
                        table-name  group      subgroup
# multi-bar-chart  :: ( Table , String , String ) -> Image
                        table-name  group      subgroup
```

4) Make a stacked-bar-chart showing the distribution of sexes across species in our shelter.

5) Make a multi-bar-chart showing the distribution of sexes across species in our shelter.

6) What do you notice? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

7) What do you wonder? \_\_\_\_\_  
\_\_\_\_\_

8) Which display would be most efficient for answering the question: "What percentage of cats are female?" Why?

---

9) Which display would be most efficient for answering the question: "Are there more cats or dogs?" Why?

---

10) Write a question of your own that involves comparing subgroups across groups. \_\_\_\_\_  
\_\_\_\_\_

Which display would be most efficient for answering your question? \_\_\_\_\_ Make the display.

What did you learn? \_\_\_\_\_

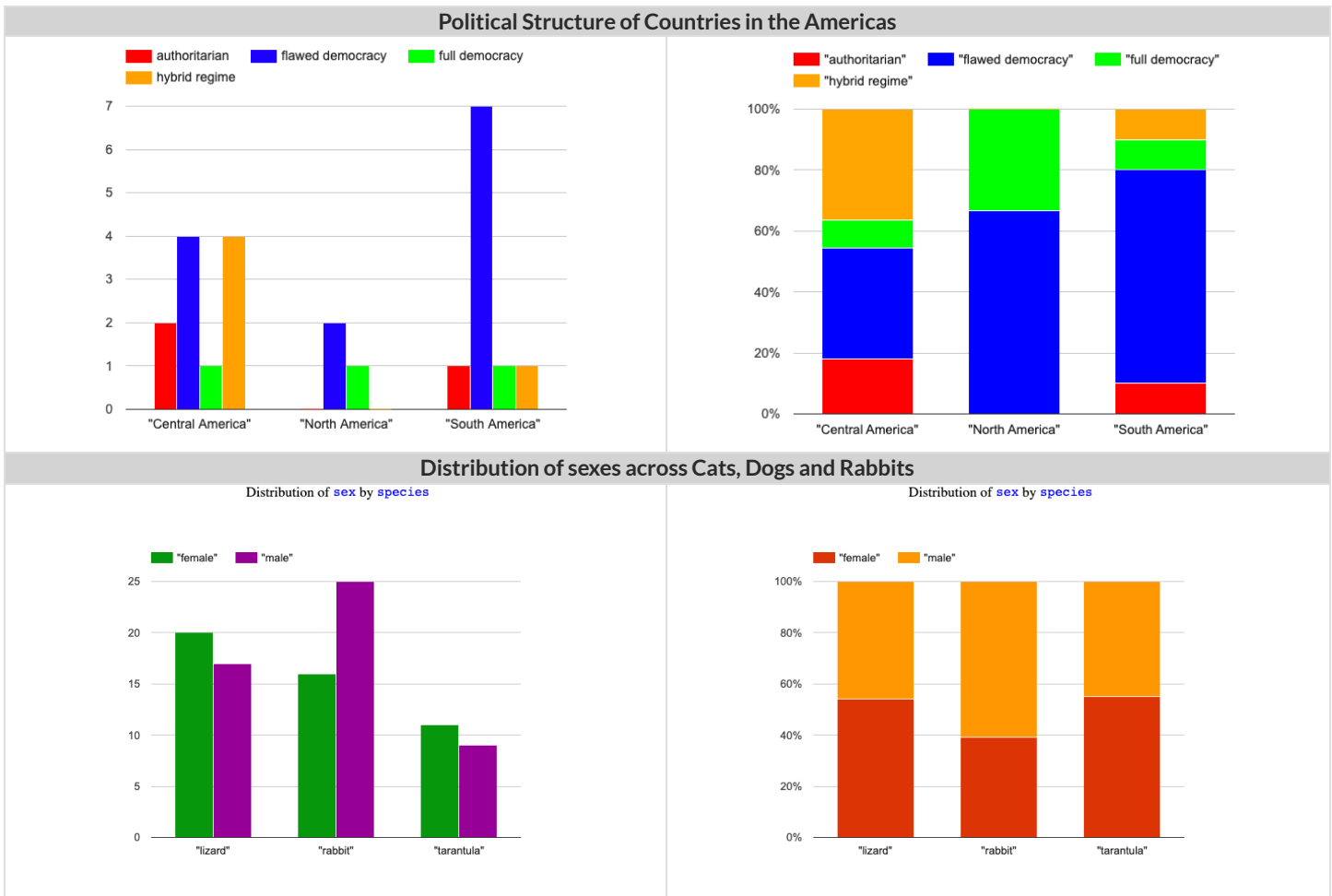
11) Write a different question that would be more efficient to answer with the other kind of display. \_\_\_\_\_  
\_\_\_\_\_

What did you learn from making this display? \_\_\_\_\_

# Multi Bar & Stacked Bar Charts - Notice and Wonder

The visualizations on the left are called **multi bar charts**.

The visualizations on the right are called **stacked bar charts**.



**What do you Notice?**

**What do you Wonder?**

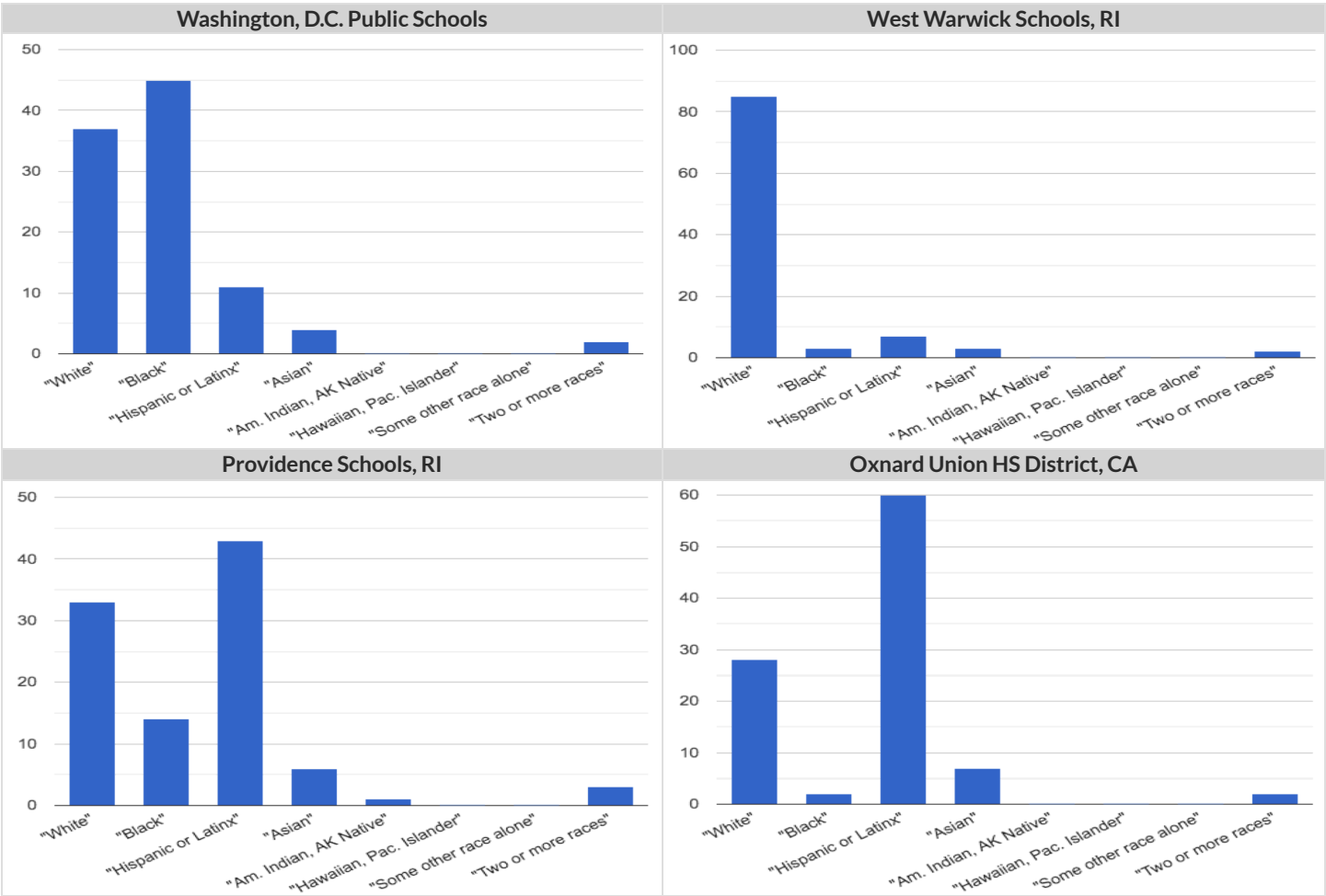
1) Is it possible that the same data was used for the multi bar charts as for the stacked bar charts? How do you know?

2) Write a question that it would be easiest to answer by looking at one of the multi bar charts.

3) Write a question that it would be easiest to answer by looking at one of the stacked bar charts.

# Bar Chart - Notice and Wonder

What do you Notice and Wonder about the pie charts below?

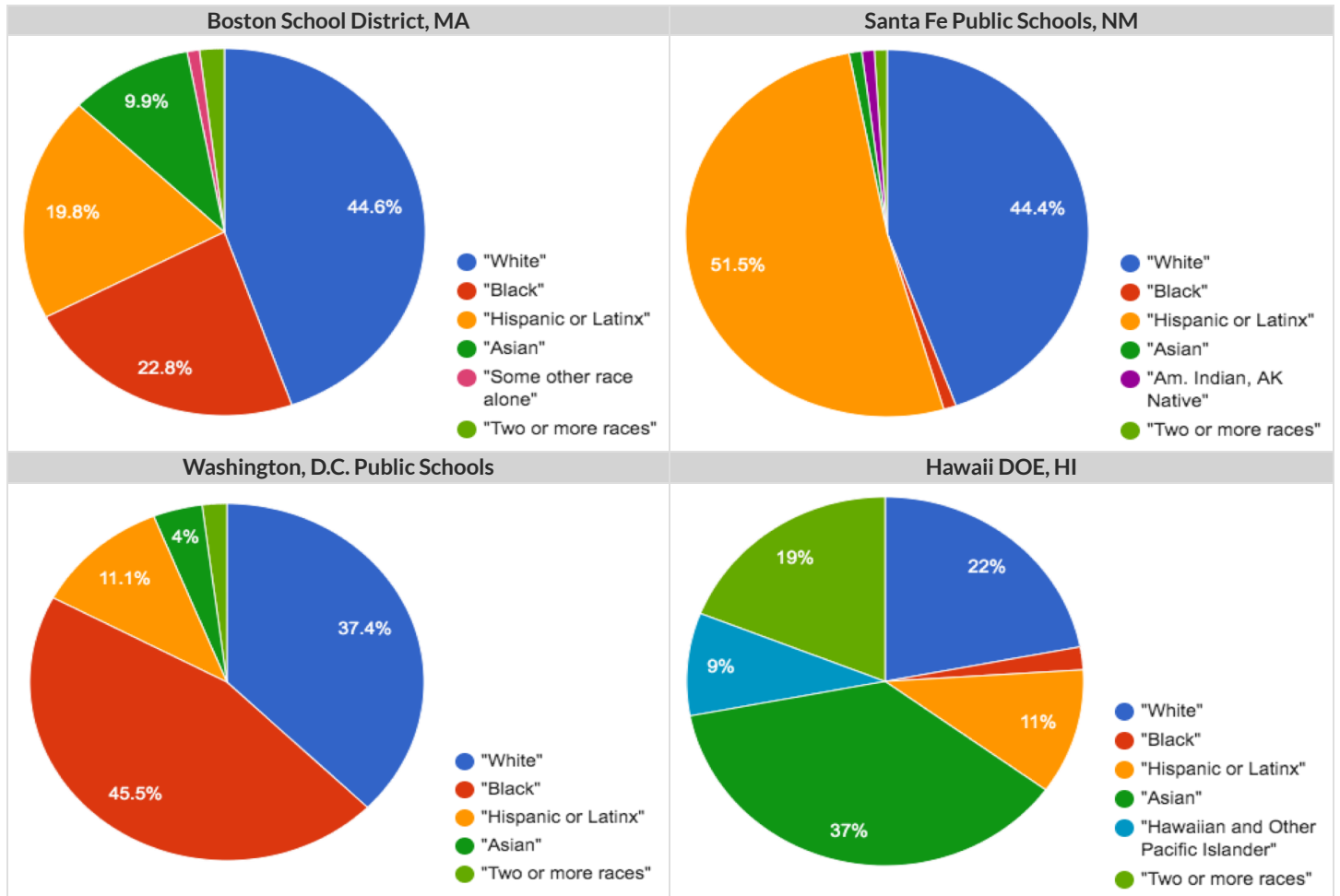


What do you Notice?	What do you Wonder?
<div></div>	<div></div>



# Pie Chart - Notice and Wonder

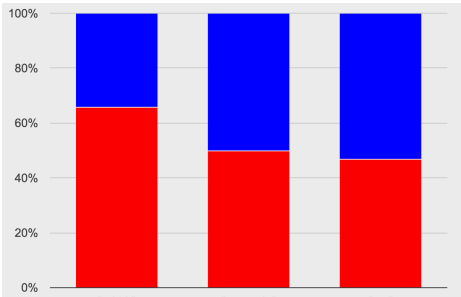
What do you Notice and Wonder about the pie charts below?



What do you Notice?	What do you Wonder?

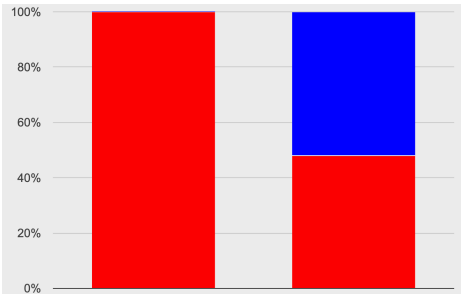
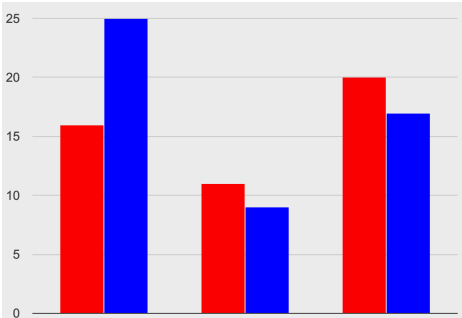
# Matching Stacked and Multi Bar Charts

Match each stacked bar chart below to the multi bar chart that visualizes the same information.



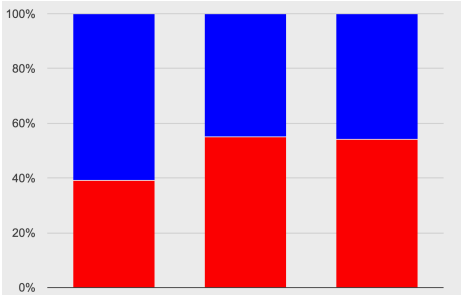
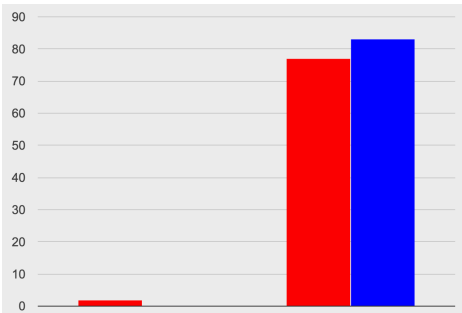
1

A



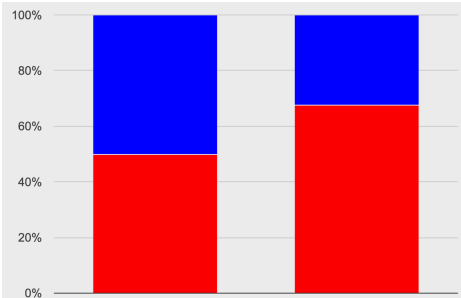
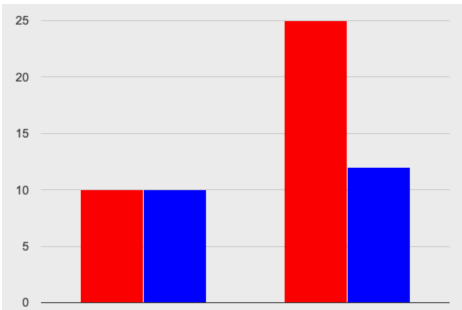
2

B



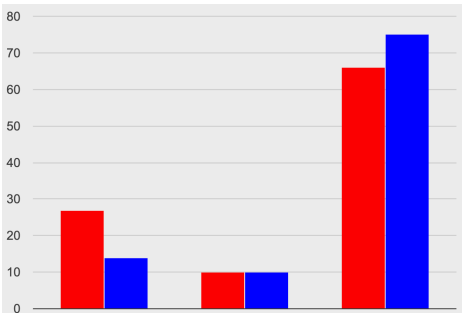
3

C



4

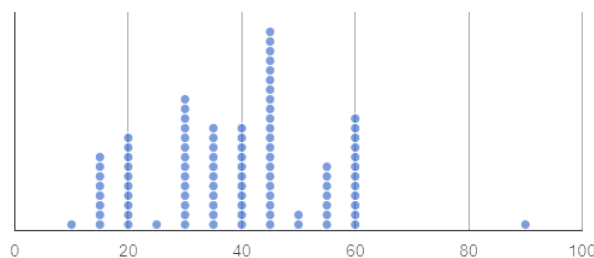
D



(optional)

# Dot Plots: Distribution, Typicality, Variability in a Nutshell

A **dot plot** (below) is a data visualization consisting of data points plotted along a number line.



On the dot plot (above), each data point represents one student in a sample.

The position of the data point indicates how many minutes it takes for that student to get ready for school. We see, for example, that there is only one student who gets ready in 10 minutes and there are 8 students who take 15 minutes to get ready.

**Distribution of Data.** To describe the distribution of data—the way that it is spread out on a number line—it is helpful to locate any outliers, clusters, peaks, and gaps.

- A **cluster** is a group of data points that are close together. *Most of the data in the dot plot above is clustered from 10-60, meaning that most students spend between 10 minutes and an hour getting ready for school in the morning.*
- A **gap** is an interval where there are no data points. *On the dot plot above, there is a gap from 60 to 90. In this sample, no one takes between 60 and 90 minutes to get ready.*
- An **outlier** occurs when one data point is much larger or smaller than the other data points. *There is an outlier on the above dot plot at 90. One student requires much more time to get ready in the morning.*
- A **peak** is the value(s) with the most data. *In this sample, 45 minutes is the most common amount of time spent getting ready for school.*

## Typicality of Data

- Typicality in a dataset is what we expect from a dataset. We can estimate typicality by looking for peaks and clusters in a dataset.
- In looking at the dot plot above, we might estimate that students typically spend 40 or 45 minutes getting ready for school.

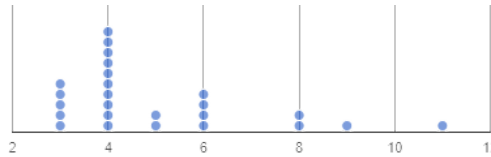
## Variability of Data

- **Variability** is how different or alike the data points are. In a quantitative dataset we can measure and describe the variability using range, interquartile range, and standard deviation.
- **Statistical questions** are questions that anticipate variability.
- "In general, how tall are the students in your class?" does anticipate variability.
- "How many inches are in a foot?" does not anticipate variability. The answer is always 12.

# Interpreting Dot Plots

## Reading a Dot Plot (Group A)

The dot plot below is a name length data visualization created by a group of 25 students (Group A).



- 1) What is the difference (in letters) between the longest and shortest name? \_\_\_\_\_
- 2) What is the most common name length? \_\_\_\_\_
- 3) What fraction of students have first names that are 5 letters long? \_\_\_\_\_

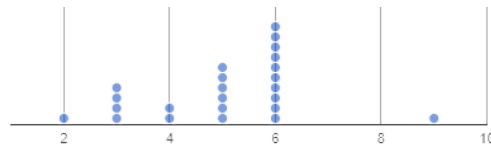
## Interpreting Peaks, Clusters, Gaps, and Outliers

4) The distribution of the data is the way that it is spread out on the number line. One way to describe distribution is by identifying peaks, clusters, gaps, and outliers. As a class, label any peaks, clusters, gaps, or outliers on the dot plot **above**.

5) Let's think about what those peaks, clusters, gaps and outliers **tell** us about the dataset. In the dot plot above:

- the peak indicates that \_\_\_\_\_ letters is the most common name length
- the cluster indicates that many students' names are \_\_\_\_\_ letters
- the gaps tell us that, in this sample, no students have names that are \_\_\_\_\_ letters or \_\_\_\_\_ letters
- the outlier is \_\_\_\_\_ letters, telling us that longer names are uncommon in this sample.

## Reading a Dot Plot (Group B)



- 6) Label the peaks, clusters, gaps, and outliers of this new dot plot representing the name lengths of a different group of 25 students (Group B).
- 7) What do the peaks, clusters, gaps, and outliers tell you about the dataset?

## Typicality of Name Length Data

- 8) What do you think is a typical value in Group A? \_\_\_\_\_ (There is more than one correct response.) Explain your reasoning. \_\_\_\_\_
- 9) Identify another value someone else might claim is typical of Group A. \_\_\_\_\_ Why would they choose that value? \_\_\_\_\_
- 10) Would 6 letters be a good description of the typical number of letters in students' names for Group B? \_\_\_\_\_ Explain. \_\_\_\_\_

# Our Class' Name Length Data

## Create a Dot Plot: Length of First Names in My Class

1) Your class just created a communal dot plot. Copy all of its dots onto the number line below.



## Reading a Dot Plot

2) What is the difference (in letters) between the longest name and the shortest name? \_\_\_\_\_

3) What is/are the most common name length(s)? \_\_\_\_\_

4) What fraction of students have first names that are 5 letters long? \_\_\_\_\_

## Peaks, Clusters, Gaps, and Outliers in Name Length Data

5) Label any peaks, clusters, gaps, and outliers on the class dot plot (above).

6) Describe what you can conclude about students' name lengths in your class, based on those peaks, clusters, gaps, and outliers. \_\_\_\_\_

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## Typicality of Name Length Data

7) What is one possible typical value for class name length? \_\_\_\_\_ Explain. \_\_\_\_\_

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8) Give another possible typical value: \_\_\_\_\_. Explain why it is appropriate. \_\_\_\_\_

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## Compare

9) Compare and contrast your class dataset with either Group A or Group B from [Interpreting Dot Plots](#). Give at least one way that the distributions are alike, and at least one way that they are different. \_\_\_\_\_

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# Two Ways of Thinking about Variability

## Variability of Categorical Data

Sana's Groceries	Juliette's Groceries
12 apples and 1 banana	4 peaches, 4 kiwis, 4 oranges, and 1 lime

1) Which dataset has greater variability - Sana's groceries or Juliette's groceries? Explain. \_\_\_\_\_

---

---

2) You ask a group of sixth grade students to respond to two different statements with either "true" or "false."

- Statement A: *I am in sixth grade.*
- Statement B: *I am wearing blue today.*

Which statement do you predict will produce greater variability? Explain. \_\_\_\_\_

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## Variability of Quantitative Data

3) Someone looks at your class roster and says, "*In general, students in our class have the same number of letters in their first names.*"

Do you agree or disagree? Explain your reasoning. \_\_\_\_\_

---

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4) Which dataset do you predict will have greater variability for a group of ninth graders who attend the same school - wake-up times on

Wednesday or Saturday? Explain. \_\_\_\_\_

---

---

5) Below are the students' responses for their wake-up times on Wednesday versus Saturday. Was your prediction correct? Explain.

- Wednesday: 6:30, 6:15, 6, 6:45, 6:30, 5:45, 6:45, 6:30, 6:30, 6:15
- Saturday: 7:00, 8:00, 8:30, 6:30, 9:45, 10:30, 6:00, 5:45, 10:15, 9:30

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## Designing Datasets with High and Low Variability

6) Make up two **categorical** datasets with 5 items, each.

Dataset with Low Variability	Dataset with High Variability

7) Make up two **quantitative** datasets with ten quantities, each.

Dataset with Low Variability	Dataset with High Variability

# Variability of Dot Plots

The person who created the dot plots below forgot to label them. For each row, decide which description matches which dot plot. Then explain your choice.

	Which dot plot corresponds, A or B?	Dot Plot A	Dot Plot B	Explain your choice
1)	Students' hours of sleep: <ul style="list-style-type: none"> <li>on Monday night: _____</li> <li>on Saturday night: _____</li> </ul>			<div></div> <div></div> <div></div> <div></div>
2)	Ages: <ul style="list-style-type: none"> <li>of all sixth graders at a K-12 school: _____</li> <li>of all students at a K-12 school: _____</li> </ul>			<div></div> <div></div> <div></div> <div></div>
3)	Weights: <ul style="list-style-type: none"> <li>of cats in the shelter: _____</li> <li>of dogs in a shelter: _____</li> </ul>			<div></div> <div></div> <div></div> <div></div>
4)	Number of minutes: <ul style="list-style-type: none"> <li>spent brushing teeth in a day: _____</li> <li>spent getting ready for school: _____</li> </ul>			<div></div> <div></div> <div></div> <div></div>
5)	Number of televisions: <ul style="list-style-type: none"> <li>per household: _____</li> <li>per bedroom: _____</li> </ul>			<div></div> <div></div> <div></div> <div></div>

# Variability of Animals' Weights

## Make Your Predictions

The staff at the shelter know there is a relationship between how much an animal weighs and how much it eats. They're about to order food for the month, and need some help analyzing the distribution of animals' weights!

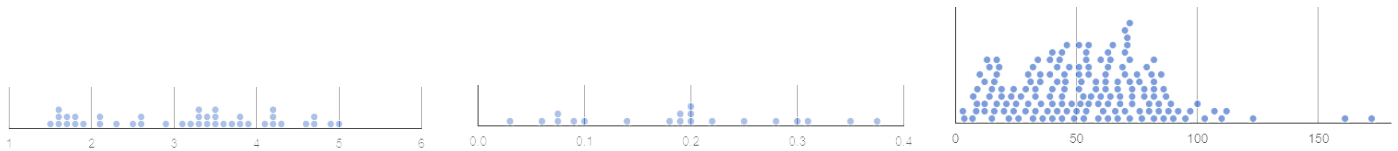
1) Imagine a *typical* animal from each of these four species. Rank the animals from lightest (1) to heaviest (4).

dog: \_\_\_\_\_ rabbit: \_\_\_\_\_ cat: \_\_\_\_\_ tarantula: \_\_\_\_\_

2) Circle the species you expect to have the *greatest* variability in weight:      dog                  rabbit                  cat                  tarantula

3) Circle the species you expect to have the *least* variability in weight:      dog                  rabbit                  cat                  tarantula

4) The dot plots below display the weight distributions of dogs, rabbits, and tarantulas. Identify the species of each plot.



species: \_\_\_\_\_ species: \_\_\_\_\_ species: \_\_\_\_\_

5) Explain how you made your decisions. \_\_\_\_\_

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## Test Your Predictions Using Pyret

6) Using the [Dogs, Rabbits, Cats & Tarantulas Starter File](#), build a dot plot for each species. In your code, use the tables defined on lines 22-25. Use information from your dot plots to fill in the cells. You can hover your mouse over specific points on the dot plot for additional information on an individual animal. Some cells have been completed for you.

	dogs	cats	rabbits	tarantula
Range/variability	3-172 lbs			
Gaps	123-161 lbs		No significant gaps	No significant gaps
Outliers	Kujo (172 lbs) Mr. PB (161 lbs)		No significant outliers	No significant outliers
Peak(s)	72 pounds			

7) Purchasing dog food would be easier if every dog ate roughly the *same amount of food*! But is that true for dogs? What about rabbits, or *any* of the four species in the [Dogs, Rabbits, Cats & Tarantulas Starter File](#)? Can you make any recommendations about quantity of food to

purchase? \_\_\_\_\_

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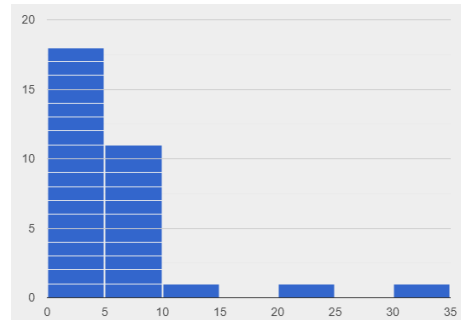
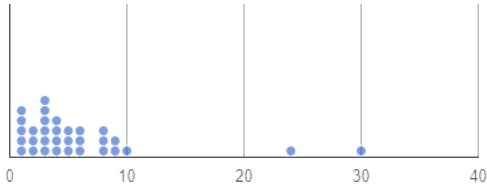
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# Comparing Dot Plots and Histograms

The displays below both show the distribution of weeks that animals spend at the shelter.

## Notice and Wonder



1) What do you Notice about the dot plot (left) and the histogram (right)? What do you Wonder? \_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

## Dot Plots versus Histograms

Answer the questions below using only the dot plot, and then only the histogram. If you cannot answer a question precisely, write "X".

Question	Dot Plot	Histogram
2) How many animals were in the shelter for fewer than 10 weeks?		
3) How many animals were in the shelter for exactly 30 weeks?		
4) What is the longest amount of time that an animal stayed in the shelter?		
5) How many animals were in the shelter for at least 5 weeks but not more than 25?		
6) Are there any gaps in the data?		
7) Are there any peaks in the data?		

## Reflect

8) When you answered the questions using the dot plot:

i. Which questions were **easy** to answer? \_\_\_\_\_

ii. Which questions were **hard** to answer? \_\_\_\_\_

iii. Which questions were **impossible** to answer? \_\_\_\_\_

9) When you answered the questions using the histogram:

i. Which questions were **easy** to answer? \_\_\_\_\_

ii. Which questions were **hard** to answer? \_\_\_\_\_

iii. Which questions were **impossible** to answer? \_\_\_\_\_

10) When might a histogram be more useful than a dot plot?

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

11) When might a dot plot be more useful than a histogram?

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

# Matching Dot Plots and Histograms

Draw a line from each dot plot on the left to the corresponding histogram on the right.

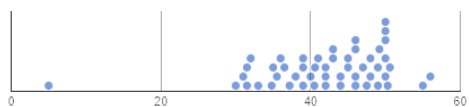
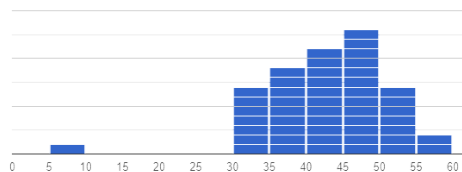
Dot Plot

Histogram



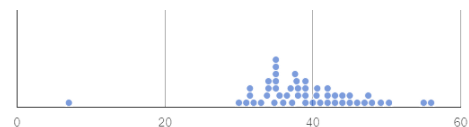
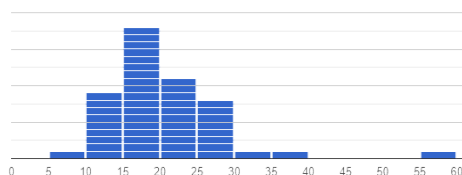
1

A



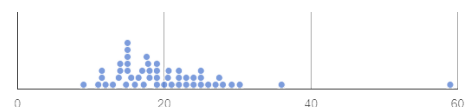
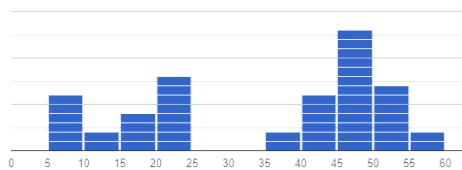
2

B



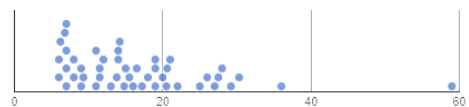
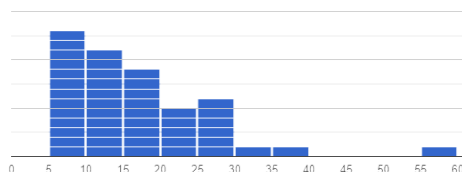
3

C



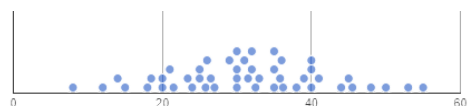
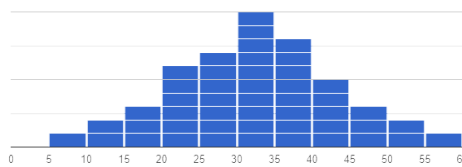
4

D



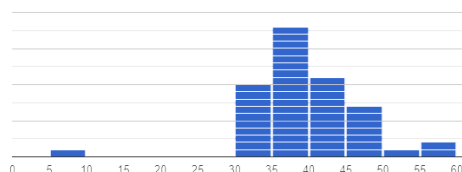
5

E



6

F



## Making Histograms

## By Hand

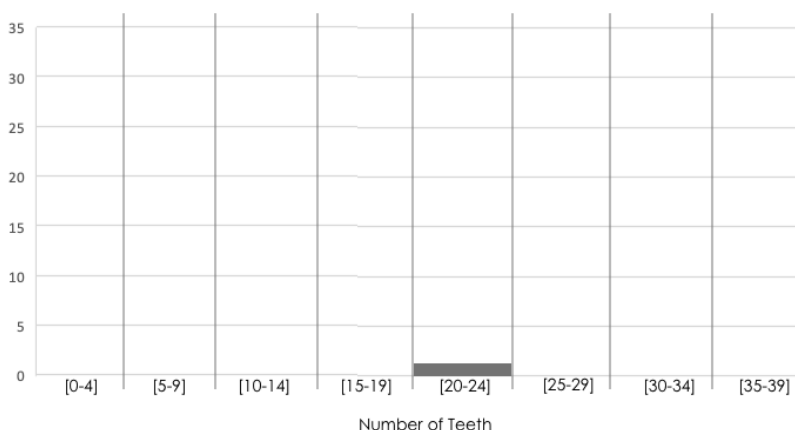
Suppose we have a dataset for a group of 50 adults, showing the number of teeth each person has...

0, 0, 0, 0, 0, 22, 26, 27, 28, 28, 28, 28, 29, 29, 29, 30, 30, 30, 30, 30, 31, 31, 31, 32, 32, 32, 32, 32, 32, 32, 32, 32,  
32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32, 32

1) Use the data to complete the frequency table below. (The last cell has been completed for you.)

number of teeth	0-4	5-9	10-14	15-19	20-24	25-29	30-34
frequency							35

2) Use the frequency table to draw a histogram below, filling in each interval so that its height is equal to the frequency.



## In Pyret

Open the **Tooth Data Starter File**. Make a copy, and click "Run".

3) Type `tooth-table` in the Interactions window. Press enter. What do you see?

4) Type `count( tooth-table, "num-teeth" )` in the Interactions window and press enter. How is the frequency table created in Pyret different from the one that you created, above?

5) What bin sized was used for the Tooth Data frequency table and the histogram above?

6) Build `tooth-table`. Does this data appear to be the same or different from the tooth data that appeared in the first section?

7) Use the contract below to build a histogram in Pyret of the distribution of teeth.

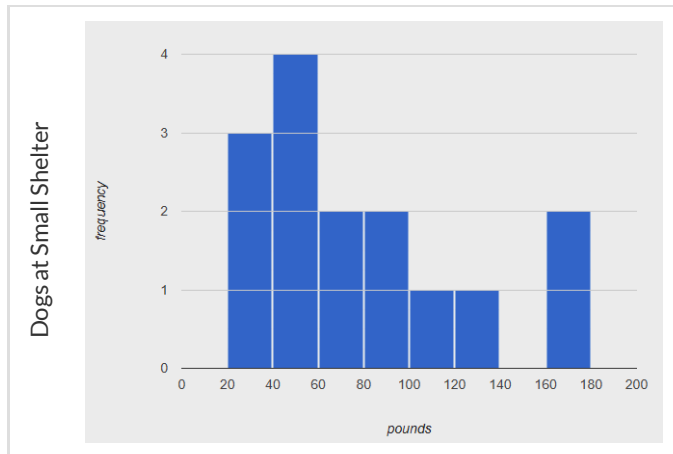
```
# histogram :: ( Table , String , String , Number ) -> Image
```

8) How does the histogram you created in Pyret look *similar* to the one that you drew? Are there any ways in which the histogram you created in Pyret is *different* than the one you created by hand?

# Reading Histograms

## Small Local Animal Shelter

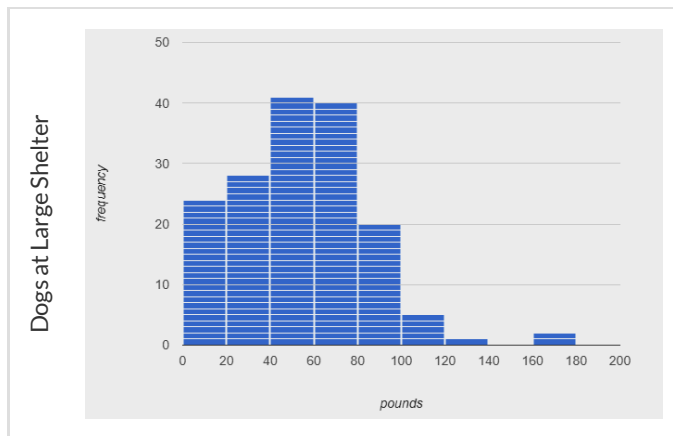
Using the histogram below, respond to the questions about the distribution of dogs' weights at a small local animal shelter.



- 1) How many dogs are represented on the histogram? \_\_\_\_\_
- 2) How many dogs weigh less than 100 pounds? \_\_\_\_\_
- 3) True or False: The majority of dogs weigh between 40 and 60 pounds.
- 4) True or False: The dogs weigh between 20 and 180 pounds.
- 5) True or False: The heaviest dog weighs between 40 and 60 pounds.
- 6) True or False: The histogram shows us that one dog weighs exactly 140 pounds.

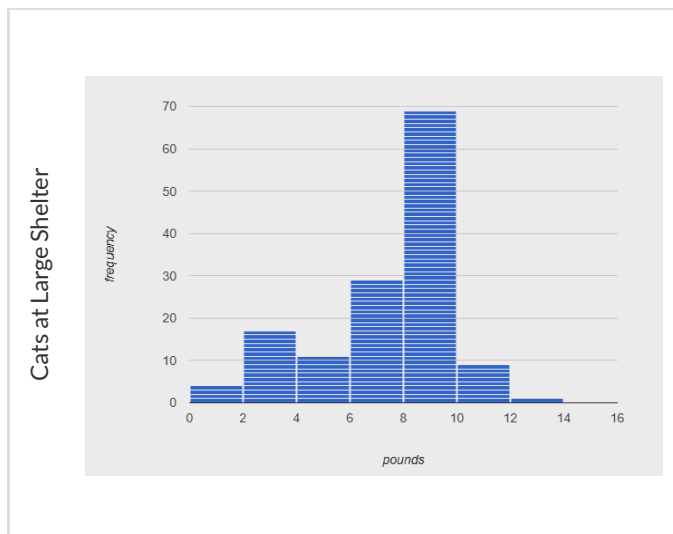
## Larger Animal Shelter

Using the histogram below, respond to the questions about **dogs'** weights at a different (much larger) animal shelter.



- 7) True or False: There are two dogs that weigh at least 160 pounds.
- 8) True or False: The majority of the dogs weigh between 40 and 60 pounds.
- 9) True or False: The lightest dog weighs zero pounds.
- 10) True or False: Most commonly, dogs at this shelter weigh 40-60 pounds.
- 11) True or False: There are 180 dogs at this animal shelter.
- 12) True or False: There are more than 150 dogs at this animal shelter.

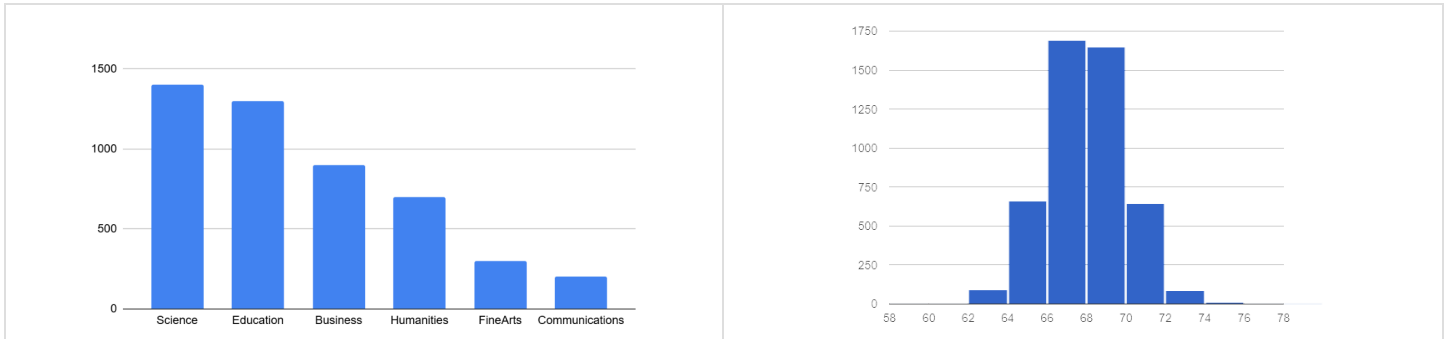
Using the histogram below, write three statements about the **cats'** weights and their distribution at the large animal shelter.



- 13) \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
- 14) \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
- 15) \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_

# Bar Charts Versus Histograms

A university consists of six colleges. Each student in the university has chosen to enroll in one of these colleges. The **bar chart** below shows the distribution of college choice. The **histogram** below shows the distribution of students by height in inches.



## Differences and Similarities

Respond to the prompts to complete the table below.

	Bar Chart	Histogram
Displays frequency: yes or no?		
Type of data: categorical or quantitative?		
Bars touch: yes or no?		
Bars can be reordered: yes or no?		
The shape of the data matters: yes or no?		

1) What are some of the ways that bar charts and histograms are **alike**? *Summarize your conclusions from the table.* \_\_\_\_\_

\_\_\_\_\_

2) What are some of the ways that bar charts and histograms are **different**? *Summarize your conclusions from the table.* \_\_\_\_\_

\_\_\_\_\_

## Distribution of College Choice

Four different students share their conclusions about the **bar graph** displayed above. Only **one** of those conclusions is correct. Respond whether you agree or not, and then explain your stance.

Student A: "The distribution is skewed to the left." \_\_\_\_\_

\_\_\_\_\_

Student B: "The distribution is skewed to the right." \_\_\_\_\_

\_\_\_\_\_

Student C: "The majority of students are enrolled in the college of science." \_\_\_\_\_

\_\_\_\_\_

Student D: "After science and education, there is a large drop in enrollments for the other colleges." \_\_\_\_\_

\_\_\_\_\_

# Choosing the Right Bin Size

Open your saved [Animals Starter File](#), or make a new copy, and click "Run".

```
# histogram :: ( Table, String, String, Number ) -> Image
                table-name  labels    column-name  bin-size
```

Make a histogram for the "weeks" column in the animals-table, using a bin size of 10 and the "name" column for your labels.

1) How many animals took between 0 and 10 weeks to be adopted? \_\_\_\_\_

2) How many animals took between 10 and 20 weeks to be adopted? \_\_\_\_\_

Try some other bin sizes (be sure to experiment with bigger and smaller bins!)

3) What shape emerges? \_\_\_\_\_

4) What bin size gives you a picture of the distribution with between 5 and 10 bins. \_\_\_\_\_

5) Are there any outliers? If so, are they high or low? \_\_\_\_\_

6) How many animals took between 0 and 5 weeks to be adopted? \_\_\_\_\_

7) How many animals took between 5 and 10 weeks to be adopted? \_\_\_\_\_

8) What else do you Notice? What do you Wonder?

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9) What was a typical time to adoption?

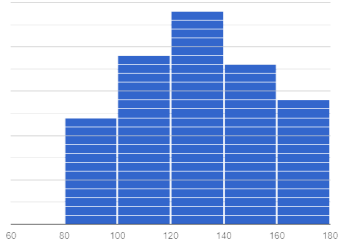
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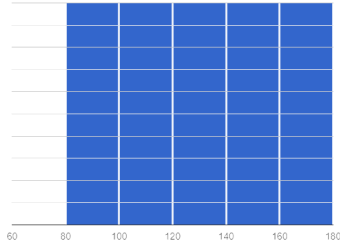
# Histograms Card Sort

Cut out one set of cards for every pair of students. Instructions for this sorting activity can be found on [Sorting Histograms](#).

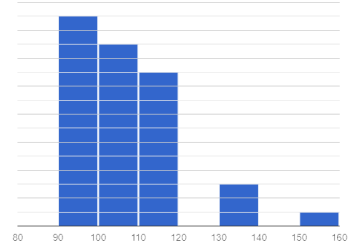
A



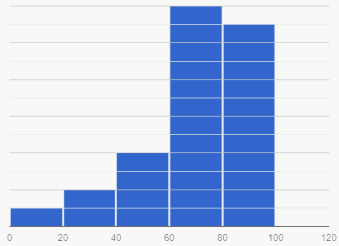
B



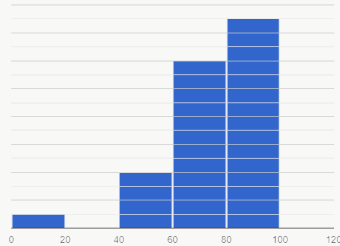
C



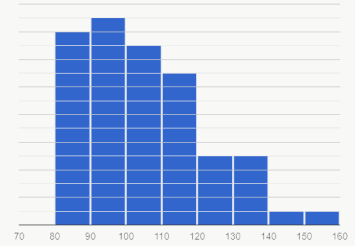
D



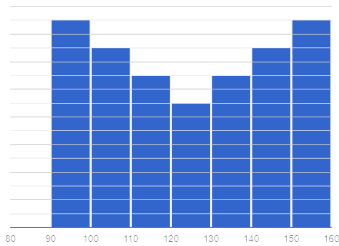
E



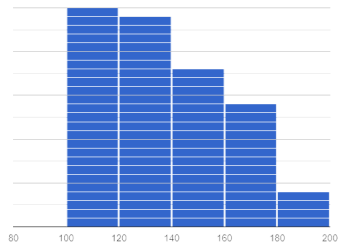
F



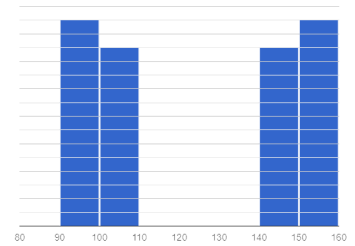
G



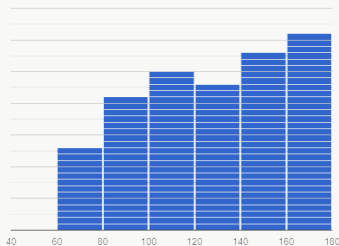
H



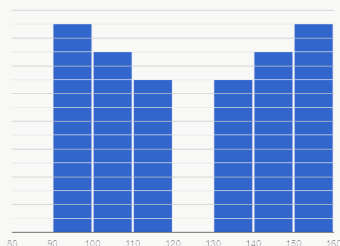
I



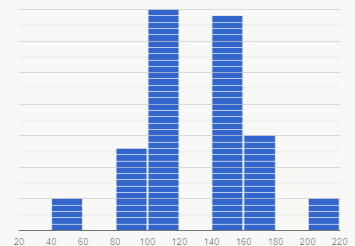
J



K



L



# Sorting Histograms

With your partner, sort the histograms into two piles: approximately symmetrical and definitely not symmetrical. Then, follow the prompts and respond to the questions below.

## Symmetrical Histograms

*Put your asymmetrical cards aside (or back in their envelope).*

- 1) List out the letters of the histograms that were symmetrical: \_\_\_\_\_
- 2) Sort the symmetrical cards into two or three logical groups. *Hint: It may be useful to think about peaks, gaps, clusters, center, and spread!* What do the cards in your first group have in common? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 3) What do the cards in your second group have in common? (Describe your third group as well, if you have a third group.) \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 4) Can you think of a different way of grouping these histograms? Explain. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 5) Describe how you can determine what's typical of a symmetrical histogram. \_\_\_\_\_  
\_\_\_\_\_

## Asymmetrical Histograms

*Put the symmetrical histograms away, and take out the asymmetrical histograms.*

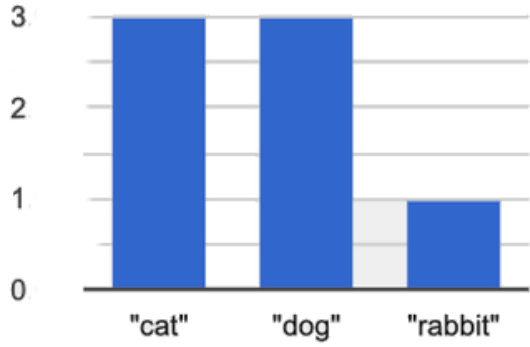
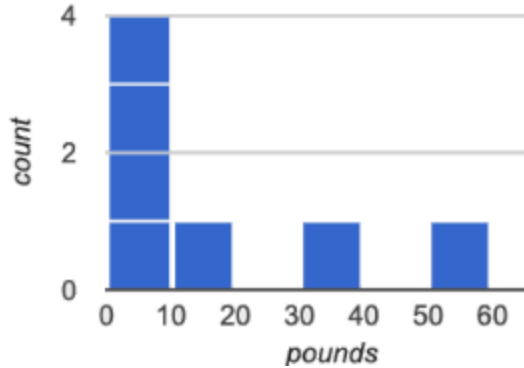
- 6) List out the letters of the histograms that were asymmetrical: \_\_\_\_\_
- 7) Sort the asymmetrical histograms into two or three logical groups. What do the cards in your first group have in common? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 8) What do the cards in your second group have in common? (Describe your third group as well, if you have a third group.) \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 9) Can you think of a different way of grouping these histograms? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_
- 10) Describe how you can determine where the outliers are on an asymmetrical histogram. \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_



# Summarizing Columns with Bar Charts & Histograms

name	species	age	pounds
"Sasha"	"cat"	1	6.5
"Boo-boo"	"dog"	11	12.3
"Felix"	"cat"	16	9.2
"Nori"	"dog"	6	35.3
"Wade"	"cat"	1	3.2
"Nibblet"	"rabbit"	6	4.3
"Maple"	"dog"	3	51.6

The two data visualizations below both summarize columns of this table. In some ways they are similar. In other ways they are quite different!

	Bar Chart	Histogram
		
1) What type of data is displayed?		
2) Could we rearrange the order of the bars?		
3) Does having a sense that the bars are taller on the left than the right tell us anything about the dataset as a whole?		

What else do you Notice?	What else do you Wonder?

# Data Collection in a Nutshell

## With Great Power Comes Great Responsibility

Politicians pass laws, shoppers choose brands, and countries go to war based on studies that sound reliable. But sometimes the data those decisions are made on is unreliable and misleading!

There are many ways for a study and its analysis to be flawed, whether by accident, by incompetence or by intent.

Being an ethical data scientist means making sure that every element of your study is designed to minimize bias in the data and analysis.

It is also best practice to acknowledge any limitations of datasets we create by writing a Datasheet for the Dataset that describes how the data was collected, what efforts were made to avoid bias, and what data may have been left out, so that people who are trying to make sense of studies that use the dataset don't have to wonder about how reliable it is for the purposes they want to use it for.

## Data Cleaning

In order to process data, it needs to be clean. Four ways that data can be dirty include:

- 1) **Missing Data** - A column containing some cells with data, but some cells left blank.
- 2) **Inconsistent Types** - A column where some values have one data type and some cells have another. For example, a years column where almost every cell is a Number, but one cell contains the string "5 years old".
- 3) **Inconsistent Units** - A column where the data types are the same, but they represent different units. For example, a weight column where some entries are in pounds but others are in kilograms.
- 4) **Inconsistent Naming** - Inconsistent spelling and capitalization for entries lead to them being counted as different. For example, a species column where some entries are "cat" and others are "Cat" will not give us a full picture of the cats.

Once the data is dirty, we have to make careful choices about how to clean it. It's never as simple as just deleting dirty rows! That might, for example, lead us to draw conclusions about the world in general based on a dataset the underrepresents the reality for developing countries.

## Survey Validation

We can design a survey to improve the odds of getting clean data. A few design features that improve results include:

- 1) **Required Questions** - By making a question "required", we can eliminate missing data and blank cells.
- 2) **Question Format** - When you have a fixed number of categories, a drop-down can ensure that everyone selects one - and only one! - category.
- 3) **Descriptive Instructions** - Sometimes it's helpful to just add instructions! This can remind respondents to use inches instead of centimeters, for example, or give them extra guidance to answer accurately.
- 4) **Adding Validation** - Most survey tools allow you to specify whether some data should be a number or a string, which helps guard against inconsistent types. Often, you can even specify parameters for the data as well, such as "strings that are email addresses", or "numbers between 24 and 96".

# Analyzing Survey Results When Data is Dirty

These questions are designed to accompany the [Survey of Eighth Graders and their Favorite Desserts Starter File](#).

1) Paolo made a pie-chart of the dessert column and was surprised to discover that **Fruit** was the most popular dessert among 8th graders!

Make the pie-chart in Pyret to see what he's looking at. Why is this display misleading? How is the data "dirty"?

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2) What ideas do you have for how the survey designer could have made sure that the data in the dessert column would have been cleaner?

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3) Make a data visualization showing the ages of the 8th graders surveyed. What "dirty" data problems do you spot and how are they misleading?

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4) What ideas do you have for how the survey designer could have made sure that the data in the age column would have been cleaner?

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5) Experiment with making data visualizations for other columns. What other issues can you spot? What other suggestions do you have for how the survey could have been improved?

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# Dirty Data!

Open the [New Animals Spreadsheet](#) and take a careful look. A bunch of new animals are coming to the shelter, and that means more data!

What do you Notice?	What do you Wonder?

There are many different ways that data can be dirty!

- a. **Missing Data** - A column containing some cells with data, but some cells left blank.
- b. **Inconsistent Types** - A column with inconsistent data types. For example, a **years** column where almost every cell is a Number, but one cell contains the string "5 years old".
- c. **Inconsistent Units** - A column with consistent data types, but inconsistent units. For example, a **weight** column where some entries are in pounds but others are in kilograms.
- d. **Inconsistent Naming** - Inconsistent spelling and capitalization for entries lead to them being counted as different. For example, a **species** column where some entries are "cat" and others are "Cat" will not give us a full picture of the cats.

1) Which animals' row(s) have **missing data**? \_\_\_\_\_

2) Which column(s) have **inconsistent types**? \_\_\_\_\_

3) Which column(s) have **inconsistent units**? \_\_\_\_\_

4) Which column(s) have **inconsistent naming**? \_\_\_\_\_

5) If we want to analyze this data, what should we do with the rows for Tanner, Toni, and Lizzy? \_\_\_\_\_

6) If we want to analyze this data, what should we do with the rows for Chanel and Bibbles? \_\_\_\_\_

7) If we want to analyze this data, what should we do with the rows for Porche and Boss? \_\_\_\_\_

8) If we want to analyze this data, what should we do with the row for Niko? \_\_\_\_\_

9) If we want to analyze this data, what should we do with rows for Mona, Rover, Susie Q, and Happy? \_\_\_\_\_

10) Sometimes data cleaning is straightforward. Sometimes the problem is evident but the solution is less certain. For which questions were you certain of your data cleaning suggestion? For which were you less certain? Why? \_\_\_\_\_

# Bad Questions Make Dirty Data

The **Height v Wingspan Survey** has *lots* of problems, which can lead to many kinds of dirty data: Missing Data, Inconsistent Types, Inconsistent Units and Inconsistent Language! Using the link provided by your teacher to your class' copy of the survey, try filling it out with bad data. Record the problems for each question and make some recommendations for how to improve the survey!

	What examples of bad data were you able to submit?	How could the survey be improved to avoid bad data?
A Age		
B Grade		
C Height		
D Wingspan		

# Probability, Inference, and Sample Size in a Nutshell

How can you tell if a coin is fair, or designed to cheat you? Statisticians know that a fair coin should turn up "heads" about as often as "tails", so they begin with the **null hypothesis**: they assume the coin is fair, and start flipping it over and over to record the results.

A coin that comes up "heads" three times in a row could still be fair! The odds are 1-in-8, so it's totally possible that the null hypothesis is still true. But what if it comes up "heads" five times in a row? Ten times in a row?

Eventually, the chances of the coin being fair get smaller and smaller, and a Data Scientist can say "this coin is a cheat! The chances of it being fair are one in a million!"

By sampling the flips of a coin, we can *infer* whether the coin itself is fair or not.

Using information from a sample to draw conclusions about the larger population from which the sample was taken is called **Inference** and it plays a major role in Data Science and Statistics! For example:

- If we survey pet owners about whether they prefer cats or dogs, the **null hypothesis** is that the odds of someone preferring dogs are about the same as them preferring cats. And if the first three people we ask vote for dogs (a 1-in-8 chance), the null hypothesis could still be true! But after five people? Ten?
- If we're looking for gender bias in hiring, we might start with the null hypothesis that no such bias exists. If the first three people hired are all men, that doesn't necessarily mean there's a bias! But if 30 out of 35 hires are male, this is evidence that undermines the null hypothesis and suggests a real problem.
- If we poll voters for the next election, the **null hypothesis** is that the odds of voting for one candidate are the same as voting for the other. But if 80 out of 100 people say they'll vote for the same candidate, we might reject the null hypothesis and infer that the population as a whole is biased towards that candidate!

**Sample size matters!** The more bias there is, the smaller the sample we need to detect it. Major biases might need only a small sample, but subtle ones might need a huge sample to be found. However, choosing a **good sample** can be tricky!

**Random Samples** are a subset of a population in which each member of the subset has an equal chance of being chosen. A random sample is intended to be a representative subset of the population. The larger the random sample, the more closely it will represent the population and the better our inferences about the population will tend to be.

**Grouped Samples** are a subset of a population in which each member of the subset was chosen for a specific reason. For example, we might want to look at the difference in trends between two groups ("Is the age of a dog a bigger factor in adoption time v. the age of a cat?"). This would require making grouped samples of *just the dogs* and *just the cats*.

# Finding the Trick Coin

Open the [Fair Coins Starter File](#), which defines coin1, coin2, and coin3. Click "Run".

You can flip each coin by evaluating `flip(coin1)` in the Interactions Area (repeat for coins 2 and 3).

One of these coins is fair, one will land on "heads" 75% of the time, and one will land on "heads" 90% of the time. \*Which one is which?\*

1) Complete the table below by recording the results for five flips of each coin and *totalling* the number of "heads" you saw. Convert the ratio of heads to flips into a *percentage*. Finally, decide whether or not you think each coin is *fair* based on your sample.

Sample	coin1		coin2		coin3	
1	H	T	H	T	H	T
2	H	T	H	T	H	T
3	H	T	H	T	H	T
4	H	T	H	T	H	T
5	H	T	H	T	H	T
#heads	/5		/5		/5	
% heads	%		%		%	
fair?	Y	N	Y	N	Y	N

2) Record 15 more flips of each coin in the table below and *total* the number of "heads" you saw *in all 20 flips of each coin*. Convert the ratio of total heads to total flips into a *percentage*. Finally, decide whether you think each coin is fair based on this larger sample.

Sample	coin1		coin2		coin3	
6	H	T	H	T	H	T
7	H	T	H	T	H	T
8	H	T	H	T	H	T
9	H	T	H	T	H	T
10	H	T	H	T	H	T
11	H	T	H	T	H	T
12	H	T	H	T	H	T
13	H	T	H	T	H	T
14	H	T	H	T	H	T
15	H	T	H	T	H	T
16	H	T	H	T	H	T
17	H	T	H	T	H	T
18	H	T	H	T	H	T
19	H	T	H	T	H	T
20	H	T	H	T	H	T
#heads	/20		/20		/20	
% heads	%		%		%	
fair?	Y	N	Y	N	Y	N

3) Which coin was the easiest to identify?      fair?      75%?      90%?

4) Why was that coin the easiest to identify? \_\_\_\_\_

# Sampling and Inference

Open the [Expanded Animals Starter File](#), and save a copy.

1) Evaluate the `more-animals` table in the Interactions Area. This is the *complete* population of animals from the shelter!

Here is a true statement about that population: *The population is 47.7% fixed and 52.3% unfixed.*

Type each of the following lines into the Interactions Area and hit "Enter".

```
random-rows(more-animals, 10)
random-rows(more-animals, 40)
```

2) What do you get? \_\_\_\_\_

3) What is the Contract for `random-rows`? \_\_\_\_\_

4) What does the `random-rows` function do? \_\_\_\_\_

5) In the Definitions Area,

- define `small-sample` to be `random-rows(more-animals, 10)`
- define `large-sample` to be `random-rows(more-animals, 40)`

6) Make a `pie-chart` for the animals in each sample, showing percentages of fixed and unfixed.

- The percentage of fixed animals in the entire population is 47.2%
- The percentage of fixed animals in `small-sample` is \_\_\_\_\_
- The percentage of fixed animals in `large-sample` is \_\_\_\_\_

7) Make a `pie-chart` for the animals in each sample, showing percentages for each species.

- The percentage of tarantulas in the entire population is roughly 5%
- The percentage of tarantulas in `small-sample` is \_\_\_\_\_
- The percentage of tarantulas in `large-sample` is \_\_\_\_\_

8) Click "Run" to direct the computer to generate a different set of random samples of these sizes. Make a new `pie-chart` for each sample, showing percentages for each species.

- The percentage of tarantulas in the entire population is roughly 4.9%
- The percentage of tarantulas in `small-sample` is \_\_\_\_\_
- The percentage of tarantulas in `large-sample` is \_\_\_\_\_

9) Which sample size gave us a more accurate inference about the whole population? Why?

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---

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# Predictions from Samples

1) In the Definitions Area of the [Expanded Animals Starter File](#), define the following samples:

```
tiny-sample = random-rows(more-animals, 10)
small-sample = random-rows(more-animals, 20)
medium-sample = random-rows(more-animals, 40)
large-sample = random-rows(more-animals, 80)
```

2) Click "Run" and make a `pie-chart` of the species in the `tiny-sample`. What animals are in the sample? \_\_\_\_\_

- Click "Run" for a *new* random `tiny-sample`, and make *another* pie-chart for species. What animals are in this sample? \_\_\_\_\_

- Click "Run" for a *new* random sample, and make *yet another* pie-chart for species. Based on these 3 samples, how many species do you think are at the shelter? \_\_\_\_\_

- Which is the *most common* species at the shelter? \_\_\_\_\_

3) What did you learn from taking multiple samples that you wouldn't have known if you'd only taken one? \_\_\_\_\_

4) Repeat the steps above, but for `small-sample`. What animals are in the sample? \_\_\_\_\_

5) Now that you've seen `small-sample`, how has your sense of the distribution of the species changed? \_\_\_\_\_

6) Now use `medium-sample` to make a `pie-chart` of the species. If there are about 400 animals at the shelter, how many of each species would you predict there to be? \_\_\_\_\_

7) Now use `large-sample` to make a `pie-chart` of the species. If there's anything you'd like to change about your prediction now that you've seen `large-sample`, record it here. \_\_\_\_\_

8) Let's see how accurate your prediction is... *feel free to click "Run" and build a few more pie charts from your samples if you want to collect more information first!* When you're ready, make a `pie-chart` of `more-animals`.

- Which predictions were closest? \_\_\_\_\_
- Which predictions were off? \_\_\_\_\_
- Were there any surprises? \_\_\_\_\_

9) In the real world, we usually don't have access to a whole dataset to check predictions against! How could we test...

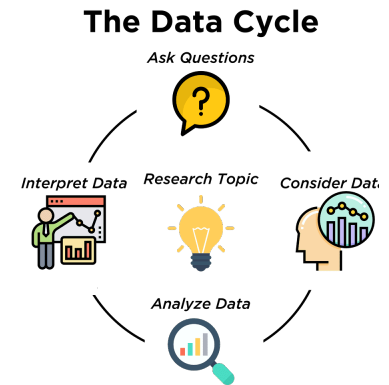
- Every giraffe on the planet?*
- Everyone who has ever come in contact with a covid-positive person?*
- What strategies can we use to make sure that predictions from samples are as close to accurate as possible?**

# The Data Cycle in a Nutshell

Data Science is all about *asking questions of data*.

- Sometimes the answer is easy to compute.
- Sometimes the answer to a question is *already in the dataset* - no computation needed.
- Sometimes the answer just sparks more questions!

Each question a Data Scientist asks adds a chapter to the story of their research. Even if a question is a "dead-end", it's valuable to share what the question was and what work you did to answer it!



1) We start by **Asking Questions** after reviewing and closely observing the data. These questions can come from initial wonderings, or as a result of previous data cycle. Most questions can be broken down into one of four categories:

- **Lookup questions** - Answered by only reading the table, no further calculations are necessary! Once you find the value, you're done! Examples of lookup questions might be "How many legs does Felix have?" or "What species is Sheba?"
- **Arithmetic questions** - Answered by doing calculations (comparing, averaging, totaling, etc.) with values from one single column. Examples of arithmetic questions might be "How much does the heaviest animal weigh?" or "What is the average age of animals from the shelter?"
- **Statistical questions** - These are questions that both *expect some variability in the data* related to the question and *account for it in the answers*. Statistical questions often involve multiple steps to answer, and the answers aren't black and white. When we compare two statistics we are actually comparing two datasets. If we ask "are dogs heavier than cats?", we know that not every dog is heavier than every cat! We just want to know if it is *generally* true or *generally* false!
- **Questions we can't answer** - We might wonder where the animal shelter is located, or what time of year the data was gathered! But the data in the table won't help us answer that question, so as Data Scientists we might need to do some research beyond the data. And if nothing turns up, we simply recognize that there are limits to what we can analyze.

2) Next, we **Consider Data**, by determining which parts of the dataset we need to answer our question. Sometimes we don't have the data we need, so we conduct a survey, observe and record data, or find another existing dataset. Since our data is contained in a table, it's useful to start by asking two questions:

- What rows do we care about? - Is it all the animals? Just the lizards?
- What columns do we need? - Are we examining the ages of the animals? Their weights?

3) Then, we **Analyze the Data**, by completing calculations, creating data visualizations, creating new tables, or filtering existing tables. The results of this step are calculations, patterns, and relationships.

- Are we making a pie chart? A bar chart? Something else?

4) Finally, we **Interpret the Data**, by answering our original question and summarizing the process we took and the results we found.

Sometimes the data cycle ends once we've interpreted the data... but often our interpretations lead to new questions... and the cycle begins again!

# Which Question Type?

name	type1	hitpoint	attack	defense	speed
Bulbasaur	Grass	45	49	49	45
Ivysaur	Grass	60	62	63	60
Venusaur	Grass	80	82	83	80
Mega Venusaur	Grass	80	100	123	80
Charmander	Fire	39	52	43	65
Charmeleon	Fire	58	64	58	80
Charizard	Fire	78	84	78	100
Mega Charizard X	Fire	78	130	111	100
Mega Charizard Y	Fire	78	104	78	100
Squirtle	Water	44	48	65	43
Wartortle	Water	59	63	80	58

Start by filling out **ONLY** the "Question Type" column of the table below.



Based on the Pokemon data above, decide whether each question is best described as:



- **Lookup** - Answered by only reading the table, no further calculations are necessary!
- **Arithmetic** - Answered by doing calculations (comparing, averaging, totalling, etc.) with values from one single column.
- **Statistical** - Best asked with "in general" attached, because the answer isn't black and white. If we ask "are dogs heavier than cats?", we know that not every dog is heavier than every cat! We just want to know if it is *generally true* or *generally false* !

	Question	Question Type	Which Rows?	Which Column(s)?
1	What type is Charizard?			
2	Which Pokemon is the fastest?			
3	What is Wartortle's attack score?			
4	What is the mean defense score?			
5	What is a typical defense score?			
6	Is Ivysaur faster than Venusaur?			
7	Is speed related to attack score?			
8	What is the most common type?			
9	Does one type tend to be faster than others?			
10	Are hitpoints (hp) similar for all Pokemon in the table?			
11	How many Fire-type Pokemon have a speed of 78?			



# Data Cycle: Consider Data



Part 1: For each question below, identify the type of question and fill in the Rows and Columns needed to answer the question.

<b>Ask Questions</b> 	<i>How old is Boo-boo?</i> What question do you have? _____ _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	

<b>Ask Questions</b> 	<i>Are there more cats than dogs in the shelter?</i> What question do you have? _____ _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	





Part 2: Think of 2 questions of your own and follow the same process for them.

<b>Ask Questions</b> 	What question do you have? _____ _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	





<b>Ask Questions</b> 	What question do you have? _____ _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	

## Data Cycle: Categorical Distributions (Animals)

Using the [Expanded Animals Starter File](#), let's make a **pie-chart** to see what we can learn about the distribution of fixed animals and what new questions it may lead us to.





Questions it may lead us to:		Question Type (circle one): Lookup Arithmetic Statistical
<b>Ask Questions</b> 	<i>Are more animals fixed or unfixed?</i> What question do you have?  <hr/>	
<b>Consider Data</b> 	<i>All the rows</i> Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)  <hr/> <i>fixed</i> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)  <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want?  <hr/>	
<b>Interpret Data</b> 	<p>The chart shows that there are _____ fixed animals _____ unfixed animals.                                             more / less / about the same number of         as / than</p> <p>Some new questions this raises include:            _____            _____            _____</p>	

Let's make a **stacked-bar-chart** to see if the ratio of fixed to unfixed animals differs by species.





<p>What does the stacked bar chart show about the ratio of fixed to unfixed animals across the different species?</p>		<p>Question Type (circle one):</p> <p>Lookup Arithmetic Statistical</p>
<p><b>Ask Questions</b></p> 	<p><i>How does the ratio of fixed to unfixed animals differ by species?</i></p> <p>What question do you have?</p> <p>_____</p>	
<p><b>Consider Data</b></p> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p>_____</p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p> <p>_____</p>	
<p><b>Analyze Data</b></p> 	<p>What code will make the table or display you want?</p> <p>_____</p>	
<p><b>Interpret Data</b></p> 	<p>The stacked bar chart shows that _____ species have _____ fixed animals _____ unfixed animals. I also notice _____</p> <p>Some new questions this raises include:</p> <p>_____</p> <p>_____</p>	

# Data Cycle: Categorical Distributions 2 (Animals)

Open the [Expanded Animals Starter File](#). Explore the distribution of a categorical column using **pie-chart** or **bar-chart**.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	<div> <input type="checkbox"/> The chart shows that there is an even distribution of _____ variable.         </div> <div> <input type="checkbox"/> The chart shows that the most common _____ variable is/are _____.         </div> <div>           I notice that _____         </div> <div>           I wonder _____         </div> <div> <ul style="list-style-type: none"> <li>How does the distribution of _____ variable differ by _____ variable?</li> <li>Another question I have is...</li> </ul> </div>	

Explore the distribution of two categorical columns using **stacked-bar-chart** or **multi-bar-chart**.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	<div>           When we break the distribution of _____ variable down by _____ variable:         </div> <div> <ul style="list-style-type: none"> <li>I notice that _____</li> <li>I wonder _____</li> </ul> </div> <div>           Another question I have is...         </div>	

# Question Types: Animals

A subset of the whole Animals Dataset is shown in the table below.

name	species	sex	age	fixed	legs	pounds	weeks
Sasha	cat	female	1	false	4	6.5	3
Sunflower	cat	female	5	true	4	8.1	6
Felix	cat	male	16	true	4	9.2	5
Sheba	cat	female	7	true	4	8.4	6
Billie	snail	hermaphrodite	0.5	false	0	0.1	3
Snowcone	cat	female	2	true	4	6.5	5
Wade	cat	male	1	false	4	3.2	1
Hercules	cat	male	3	false	4	13.4	2
Toggle	dog	female	3	true	4	48	1

Using this table - or the full dataset - write three questions of each type below.

- **Lookup** - Answered by only reading the table, no further calculations are necessary!
- **Arithmetic** - Answered by doing calculations (comparing, averaging, totalling, etc.) with values from one single column.
- **Statistical** - Best asked with "in general" attached, because the answer isn't black and white. If we ask "are dogs heavier than cats?", we know that not every dog is heavier than every cat! We just want to know if it is *generally true* or *generally false* !




	Type	Question
1	Lookup	
2	Lookup	
3	Lookup	
4	Arithmetic	
5	Arithmetic	
6	Arithmetic	
7	Statistical	
8	Statistical	
9	Statistical	




(optional)

# Data Cycle: Analyzing with Count




For each question below, complete the first three steps of the Data Cycle.

Once you know what code to write, type it into Pyret and try it out!

<b>Ask Questions</b> 	<i>How many of each species are at the shelter?</i> What question do you have? _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____	
	What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	
<b>Analyze Data</b> 	What code will make the table or display you want? _____	

<b>Ask Questions</b> 	<i>How many of each sex are at the shelter?</i> What question do you have? _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____	
	What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	
<b>Analyze Data</b> 	What code will make the table or display you want? _____	

For the final Data Cycle, develop your own question and complete the remaining steps.

<b>Ask Questions</b> 	What question do you have? _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____	
	What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	
<b>Analyze Data</b> 	What code will make the table or display you want? _____	

(optional)



# Rubric: Exploration Project (1)

## About this Dataset

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I explained why this dataset is interesting to me, others like me, and why others should care about it. I considered why the dataset was collected, and what purpose it might serve. I correctly identified all rows, columns, and types in my dataset.	I explained why this dataset was interesting to me and at least one other person/group, and shared <i>something</i> about where it came from. I correctly identified most of the rows, columns, and types in my dataset.	I explained why this dataset was interesting to me, and shared <i>something</i> about where it came from. I correctly identified some rows, columns, and types in my dataset.

## Criteria for Visualizations

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I either included multiple visualizations of this type or wrote about why I my data didn't allow for multiple. I indicated which column(s) I used and added the relevant code. I made a strong attempt to interpret the interesting visualizations and report about the visualizations that weren't useful. I added the questions that emerged to the "My Questions" section.	I included one display of this type. I provided the column name and relevant code. My interpretation lacked detail. I added the questions that emerged to the "My Questions" section.	I included one or no visualizations of this type. My slides may be missing a correct column name or code. My data interpretation may be missing or inaccurate. I may not have added to the "My Questions" section.

Visualizations	Rating	Teacher Feedback
Bar Chart	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
Pie Chart	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
Dot Plot	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
Histogram	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
Box Plot	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	

# Rubric: Exploration Project (2)

## Measures of Center

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I selected at least two columns in my dataset, and correctly filled out the entire summary table for each one (or wrote about why my data didn't allow for this.) Based on these measures, I decided which measure of center was best for each column, and I provided a detailed interpretation of what these measures tell me about the dataset.	I selected at least two columns in my dataset (or wrote about why my data didn't allow for this), and correctly filled out the entire summary table for each one. I tried to interpret what these measures tell me about the dataset, but my interpretation lacked detail.	I filled out most of the table but didn't demonstrate understanding of what these measures tell about the dataset.

## Correlation and Linear Regression

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I either included multiple scatter plots or wrote about why my data didn't allow for multiple. I described my observations, including identifying outliers and patterns that could point to possible correlations. If the scatter plot didn't reveal any patterns or outliers, I wrote about that. When the corresponding linear regression plot(s) showed a correlation, I included an additional slide and a thoughtful interpretation.	I included at least one scatter plot with cursory descriptions and observations. I included a slide of a linear regression plot showing a correlation or described why I didn't include any linear regression plots.	I added at least one slide about a scatter plot. The description and/or display may be lacking. I may have left out the linear regression, included one that didn't reveal a correlation, or offered an incorrect interpretation of it.

## My Questions

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I had lots of questions by the end of the exploration, and I chose at least two that I thought were most interesting. I explained why I thought they were interesting, and wrote about grouped samples that might be good to explore when answering those questions.	I had a few questions by the end of the exploration, and I chose at least one that was interesting. I wrote about grouped samples that might be good to explore.	I picked a question, and wrote about grouped samples.

## Additional Teacher Feedback

# Choosing Your Dataset in a Nutshell

When selecting a dataset to explore, *pick something that matters to you!* You'll be working with this data for a while, so you don't want to pick something at random just to get it done.

When choosing a dataset, it's a good idea to consider a few factors:

1. Is it **interesting**?

Pick a dataset you're genuinely interested in, so that you can explore questions that fascinate you!

2. Is it **relevant**?

Pick a dataset that deals with something personally relevant to you and your community!

Does this data impact you in any way?

Are there questions you have about the dataset that mean something to you or someone you know?

3. Is it **familiar**?

Pick a dataset you know about, so you can use your expertise to deepen your analysis! You wouldn't be able to make samples of the Animals Dataset properly if you didn't know that some animals are much bigger or longer-lived than others.

# Consider and Analyze

Fill in the tables below by considering the rows and columns you need. Look up the [Contract](#) for the display and record the Pyret code you'd need to make it. If time allows, type your code into [\(CPO\)](http://code.pyret.org) to see your display!

1) A pie-chart showing the species of animals from the shelter.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

2) A bar-chart showing the sex of animals from the shelter.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

3) A histogram of the number of pounds that animals weigh.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

4) A box-plot of the number of pounds that animals weigh.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

5) A scatter-plot, using the animals' species as the labels, age as the x-axis, and pounds as the y-axis.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

6) A scatter-plot, using the animals' name as the labels, pounds as the x-axis, and weeks as the y-axis.

Which Rows?	Which Column(s)?	What will you Create?
<i>All the animals</i>		

code: \_\_\_\_\_

# My Dataset

The \_\_\_\_\_ dataset contains \_\_\_\_\_ data rows.

1) I'm interested in this data because \_\_\_\_\_

2) My friends, family or neighbors would be interested because \_\_\_\_\_

3) Someone else should care about this data because \_\_\_\_\_

4) In the table below, write down what you Notice and Wonder about this dataset.

What do you Notice?	What do you Wonder?	Question
		Lookup Arithmetic Statistical Can't Answer
		Lookup Arithmetic Statistical Can't Answer
		Lookup Arithmetic Statistical Can't Answer
		Lookup Arithmetic Statistical Can't Answer
		Lookup Arithmetic Statistical Can't Answer
		Lookup Arithmetic Statistical Can't Answer

5) Consider each Wonder you wrote above and Circle what type of question it is.




**Choose two columns to describe below.**

6) \_\_\_\_\_, which contains \_\_\_\_\_ data. Example values from this column include:  
column name categorical/quantitative

7) \_\_\_\_\_, which contains \_\_\_\_\_ data. Example values from this column include:  
column name categorical/quantitative

# Data Cycle: Categorical Data

Use the Data Cycle to explore the distribution of one or more categorical columns using **pie-charts** and **bar-charts**, and record your findings.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

# Datasets and Starter Files

Click through the datasets below. (Your teacher might also ask you to work with Global Food Supply [[Dataset](#)] [[Starter File](#)].) When you find one you'd like to use in Pyret, (1) click the "Starter File" link to open it in a new tab and (2) select "Save a copy" from the "File" menu.

★ Looking for a shorter list? We've starred a few good beginner datasets.

## The Environment & Health

Global Waste by Country 2019	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
World Cities' Proximity to the Ocean	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Earthquakes	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Air Quality, Pollution Sources & Health in the U.S.	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Health by U.S. County	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
COVID in the U.S. by County	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Arctic Sea Ice	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]

## Politics

Countries of the World	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Gerrymandering	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Marijuana Laws & Arrests by State 2018	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
LAPD Arrests 2010-2019	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
NYPD Stop, Search & Frisk 2019	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Refugees 2018	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
State Demographics	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
U.S. Income	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
U.S. Jobs	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
U.S. Voter Turnout 2016	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]

## Sports

Esports Earnings	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
MLB Hitting Stats	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
NBA Players	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
NFL Passing	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
NFL Rushing	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]

## Entertainment

★ Movies	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
IGN video game Reviews	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
International Exhibition of Modern Art	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
North American Pipe Organs	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Pokemon	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
Music	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]

## Education

College Majors	[ <a href="#">Dataset</a> <a href="#">Starter File</a> ]
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U.S. Colleges 2019-2020 [ [Dataset Starter File](#) ]

★R.I. Schools [ [Dataset Starter File](#) ]

Evolution of College Admissions in California [ [Dataset Starter File](#) ]

## Nutrition

Soda, Coffee & Other Drinks [ [Dataset Starter File](#) ]

Fast Food Nutrition [ [Dataset Starter File](#) ]

[Would you like to contribute a dataset of your own, or is there something you'd like to change about one of ours?](#)



# Relationships Between Quantitative Columns

## Scatter Plots

Scatter plots can be used to look for relationships between columns. Each row in the dataset is represented by a point, with one column providing the x-value (**explanatory variable**) and the other providing the y-value (**response variable**). The resulting “point cloud” makes it possible to look for a relationship between those two columns.

- **Form**
  - If the points in a scatter plot appear to follow a straight line, it suggests that a **linear relationship** exists between those two columns.
  - Relationships may take other forms (u-shaped for example). If they aren't linear, it won't make sense to look for a correlation.
  - Sometimes there will be no relationship at all between two variables.
- **Direction**
  - The correlation is **positive** if the point cloud slopes up as it goes farther to the right. This means larger y-values tend to go with larger x-values.
  - The correlation is **negative** if the point cloud slopes down as it goes farther to the right.
- **Strength**
  - It is a **strong** correlation if the points are tightly clustered around a line. In this case, knowing the x-value gives us a pretty good idea of the y-value.
  - It is a **weak** correlation if the points are loosely scattered and the y-value doesn't depend much on the x-value.

## Line of Best Fit

**Linear Relationships** can be graphically summarized by drawing a straight line through the data cloud. This summary line is called a “model”, as it attempts to provide a simple summary for trends in the dataset. For most datasets, there is no line that will touch every dot, so *all possible models will have some error!* But if the line is close enough to enough of the dots, the model can still help us reason and make predictions about y-values from x-values

$$\text{Data} = \text{Model} + \text{Error}$$

The line that is *closest* to all the other points is known as the **line of best fit**, meaning it is the *best possible summary* of the relationship and therefore the *best possible model*.

**Linear Regression** is a way of computing the **line of best fit**. It considers every single data point to generate the optimal linear model, with the smallest possible vertical distance between the line and all the points taken together. *(More specifically, the computer minimizes the sum of the squares of the vertical distances from all of the points to the line. There's a reason we use computers to do this!)*

Points that do not fit the trend line in a scatter plot are called **unusual observations**.

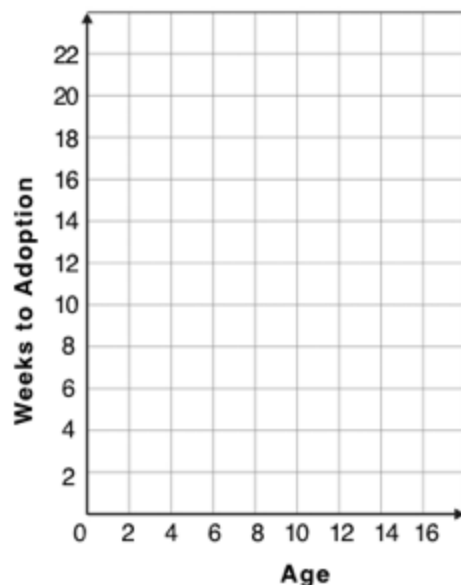
# Creating a Scatter Plot

## New Animals

1) The table below has some new animals!

- Choose an animal and plot a dot for it on the scatter plot on the right using its age and weeks values. *(Pay careful attention to how the axes are labelled.)*
- Then write the animal's name next to the dot you made.

name	species	age	weeks
"Alice"	"cat"	1	2
"Bob"	"dog"	17	2
"Callie"	"cat"	14	16
"Diver"	"lizard"	1	20
"Eddie"	"dog"	6	9
"Fuzzy"	"cat"	8	5
"Gary"	"rabbit"	4	2
"Hazel"	"dog"	3	3
"Chelsea"	"cat"	12	14
"Josie"	"dog"	9	12
"Cheetah"	"dog"	10	8



2) Plot the rest of the animals - one at a time - labeling each point as you go. After each animal, ask yourself whether or not you see a pattern in the data.

3) After how many animals did you begin to see a pattern? \_\_\_\_\_

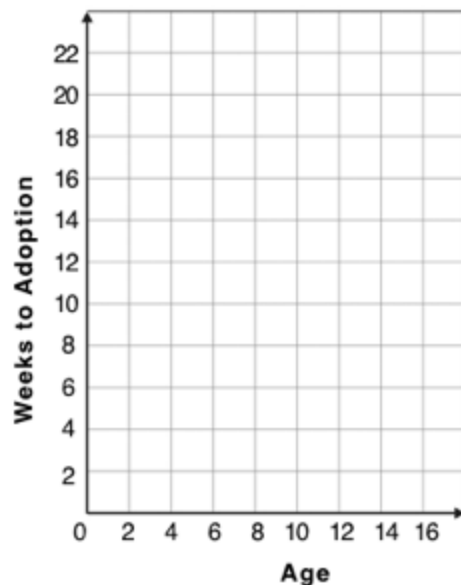
## Generalizing the pattern

4) Use a straight edge to draw a line on the graph that best represents the pattern you see, then circle the cloud of points around that line.

5) Are the points tightly clustered around the line or loosely scattered? \_\_\_\_\_

6) Does this display support the claim that younger animals get adopted faster? Why or why not?

7) Now place 10 points on the graph to make a scatter plot that appears to have NO relationship.



# Exploring Relationships Between Columns

This page is designed to be used with the [Animals Starter File](#). Log into [\(code.pyret.org \(CPO\)\)](https://code.pyret.org) to open your saved copy.

As you consider each of the following relationships, first think about what you *expect*, then make the scatter plot to see if it supports your hunch.

1) How are the pounds an animal weighs related to its age ?  
explanatory variable                      response variable

- What would you expect? \_\_\_\_\_  
\_\_\_\_\_

- What did you learn from your scatter plot? \_\_\_\_\_  
\_\_\_\_\_

2) How are the number of weeks it takes for an animal to be adopted related to its number of legs ?  
explanatory variable                      response variable

- What would you expect? \_\_\_\_\_  
\_\_\_\_\_

- What did you learn from your scatter plot? \_\_\_\_\_  
\_\_\_\_\_

3) How are the number of legs an animal has related to its age ?  
explanatory variable                      response variable

- What would you expect? \_\_\_\_\_  
\_\_\_\_\_

- What did you learn from your scatter plot? \_\_\_\_\_  
\_\_\_\_\_

4) Do any of these relationships appear to be linear (straight-line)?




\_\_\_\_\_  
\_\_\_\_\_

5) Are there any unusual observations?

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

# Data Cycle: Looking for Relationships (Animals)





Open the [Animals Starter File](#). Use the Data Cycle to search for relationships between columns. *The first cycle has a question to get you started. What question will you ask for the second?*





<b>Ask Questions</b> 	Is there a relationship between weight and adoption time? What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

# Data Cycle: Looking for Relationships (My Dataset)

Open [your chosen dataset](#). Use the Data Cycle to search for relationships between columns.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	<input type="checkbox"/> There appears to be no relationship between _____ x-variable _____ and _____ y-variable _____. <input type="checkbox"/> There appears to be a _____ strong / weak / moderate _____, _____ positive / negative _____, _____ linear / non-linear _____ relationship between _____ x-variable _____ and _____ y-variable _____. Some possible outliers might be _____	

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	<input type="checkbox"/> There appears to be no relationship between _____ x-variable _____ and _____ y-variable _____. <input type="checkbox"/> There appears to be a _____ strong / weak / moderate _____, _____ positive / negative _____, _____ linear / non-linear _____ relationship between _____ x-variable _____ and _____ y-variable _____. Some possible outliers might be _____	

# Defining Functions in a Nutshell

Functions can be viewed in *multiple representations*.

## Contract and Purpose

You already know one of them: **Contracts**, which specify the Name, Domain, and Range of a function. Contracts are a way of thinking of functions as a *mapping* between one set of data and another. For example, a mapping from Numbers to Strings:

```
# f :: Number -> String
```

## Examples

The goal of the **Examples** step is to *find the pattern* that represents what the function does.

Examples are essentially input-output tables, showing what the functions does with a list of specific inputs. *In our programming language, we write the table columns as code.*

How $f$ is used	What $f$ does
$f(1)$	$1 + 2$
$f(2)$	$2 + 2$
$f(3)$	$3 + 2$
$f(4)$	$4 + 2$

```
examples:  
f(1) is 1 + 2  
f(2) is 2 + 2  
f(3) is 3 + 2  
f(4) is 4 + 2  
end
```

## Definition

The final step in the Design Recipe is to *generalize the pattern* we see in our examples by writing a formal **function definition**. To do this we replace the inputs with **variables** that can work with any input.

In the example below, the definition for the examples above is written in both math and code:

$$f(x) = x + 2$$

```
fun f(x): x + 2 end
```

## Look for connections between these three representations!

- The function name is always the same, whether looking at the Contract, Examples, or Definition.
- The number of inputs in the Examples is always the same as the number of types in the Domain, which is always the same as the number of variables in the Definition.
- The "what the function does" pattern in the Examples is almost the same in the Definition, but with specific inputs replaced by variables.

# The Great gt domain debate!

**Kermit:** The domain of `gt` is `Number, String, String`.

**Oscar:** The domain of `gt` is `Number`.

**Ernie:** I'm not sure who's right!

In order to make a triangle, we need a size, a color and a fill style...

but all we had to tell our actor was `gt(20)`...and they returned `triangle(20, "solid", "green")`.

**Please help us!**

1) What is the correct domain for `gt`?

---

2) What could you tell Ernie to help him understand how you know?

---

---

---

---

---

---

---

---

# Let's Define Some New Functions!

1) Let's define a function `rs` to generate solid red squares of whatever size we give them!

If I say `rs(5)`, what would our actor need to say?

---

Let's write a few more examples:

`rs( )` → \_\_\_\_\_

`rs( )` → \_\_\_\_\_

`rs( )` → \_\_\_\_\_

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable:

```
fun rs( ): _____ end
```

2) Let's define a function `bigc` to generate big solid circles of size 100 in whatever color we give them!

If I say `bigc("orange")`, what would our actor need to say?

---

Let's write a few more examples:

`bigc( )` → \_\_\_\_\_

`bigc( )` → \_\_\_\_\_

`bigc( )` → \_\_\_\_\_

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable:

```
fun bigc( ): _____ end
```

3) Let's define a function `ps` to build a pink star of size 50, with the input determining whether it's solid or outline!

If I say `ps("outline")`, what would our actor need to say?

---

Write examples for all other possible inputs:

`ps( )` → \_\_\_\_\_

`ps( )` → \_\_\_\_\_

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable:

```
fun ps( ): _____ end
```

4) Add these new function definitions to your [gt Starter File](#) and test them out!



# Let's Define Some More New Functions!

1) Let's define a function `sun` to write SUNSHINE in whatever color and size we give it!

If I say `sun( 5, "blue" )`, what would our actor need to say?

---

Let's write a few more examples:

`sun( _____, _____ )` → \_\_\_\_\_

`sun( _____, _____ )` → \_\_\_\_\_

`sun( _____, _____ )` → \_\_\_\_\_

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable(s):

```
fun sun( _____, _____ ): _____ end
```

2) Let's define a function `me` to generate your name in whatever size and color we give it!

If I say `me( 18, "gold" )`, what would our actor need to say?

---

Let's write a few more examples:

`me( _____, _____ )` → \_\_\_\_\_

`me( _____, _____ )` → \_\_\_\_\_

`me( _____, _____ )` → \_\_\_\_\_

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable(s):

```
fun me( _____, _____ ): _____ end
```

3) Let's define a function `gr` to build a solid, green rectangle of whatever height and width we give it!

If I say `gr( 10, 80 )`, what would our actor need to say?

---

Let's write a few more examples:

`gr( _____, _____ )` → `rectangle( _____, _____, "solid", "green" )`

`gr( _____, _____ )` → `rectangle( _____, _____, "solid", "green" )`

`gr( _____, _____ )` → `rectangle( _____, _____, "solid", "green" )`

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable(s):

```
fun gr( _____, _____ ): _____ end
```

4) Add these new function definitions to your [gt Starter File](#) and test them out!

# Describe and Define Your Own Functions!

1) Let's define a function \_\_\_\_\_ to generate...

\_\_\_\_\_

If I say \_\_\_\_\_, what would our actor need to say? \_\_\_\_\_

Let's write a few more examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable.

fun \_\_\_\_\_ ( \_\_\_\_\_ ) : \_\_\_\_\_ end

2) Let's define a function \_\_\_\_\_ to generate...

\_\_\_\_\_

If I say \_\_\_\_\_, what would our actor need to say? \_\_\_\_\_

Let's write a few more examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable.

fun \_\_\_\_\_ ( \_\_\_\_\_ ) : \_\_\_\_\_ end

3) Let's define a function \_\_\_\_\_ to generate...

\_\_\_\_\_

If I say \_\_\_\_\_, what would our actor need to say? \_\_\_\_\_

Let's write a few more examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

\_\_\_\_\_ ( \_\_\_\_\_ ) → \_\_\_\_\_ ( \_\_\_\_\_ )

What changes in these examples? Name your variable(s): \_\_\_\_\_

Let's define our function using the variable.

fun \_\_\_\_\_ ( \_\_\_\_\_ ) : \_\_\_\_\_ end

4) Add your new function definitions to your [gt Starter File](#) and test them out!

# Matching Examples and Contracts

Match each set of examples (left) with the Contract that best describes it (right).

Examples	Contract
----------	----------

```
examples:
f(5) is 5 / 2
f(9) is 9 / 2
f(24) is 24 / 2
end
```

1

A # f :: Number -> Number

```
examples:
f(1) is rectangle(1, 1, "outline", "red")
f(6) is rectangle(6, 6, "outline", "red")
end
```

2

B # f :: String -> Image

```
examples:
f("pink", 5) is star(5, "solid", "pink")
f("blue", 8) is star(8, "solid", "blue")
end
```

3

C # f :: Number -> Image

```
examples:
f("Hi!") is text("Hi!", 50, "red")
f("Ciao!") is text("Ciao!", 50, "red")
end
```

4

D # f :: Number, String -> Image

```
examples:
f(5, "outline") is star(5, "outline", "yellow")
f(5, "solid") is star(5, "solid", "yellow")
end
```

5

E # f :: String, Number -> Image

# Matching Examples and Function Definitions

(1) Find the variables in `gt` and label them with the word "size".

examples:

```
gt(20) is triangle(20, "solid", "green")
gt(50) is triangle(50, "solid", "green")
```

end

```
fun gt(size): triangle(size, "solid", "green") end
```

(2) Highlight and label the variables in the example lists below.

(3) Then, using `gt` as a model, match the examples to their corresponding function definitions.

Examples			Definition
<p>examples:</p> <pre>f("solid") is circle(8, "solid", "red") f("outline") is circle(8, "outline", "red")</pre> <p>end</p>	1	A	<pre>fun f(s): star(s, "outline", "red") end</pre>
<p>examples:</p> <pre>f(2) is 2 + 2 f(4) is 4 + 4 f(5) is 5 + 5</pre> <p>end</p>	2	B	<pre>fun f(num): num + num end</pre>
<p>examples:</p> <pre>f("red") is circle(7, "solid", "red") f("teal") is circle(7, "solid", "teal")</pre> <p>end</p>	3	C	<pre>fun f(c): star(9, "solid", c) end</pre>
<p>examples:</p> <pre>f("red") is star(9, "solid", "red") f("grey") is star(9, "solid", "grey") f("pink") is star(9, "solid", "pink")</pre> <p>end</p>	4	D	<pre>fun f(s): circle(8, s, "red") end</pre>
<p>examples:</p> <pre>f(3) is star(3, "outline", "red") f(8) is star(8, "outline", "red")</pre> <p>end</p>	5	E	<pre>fun f(c): circle(7, "solid", c) end</pre>

# Creating Contracts From Examples

Write the contracts used to create each of the following collections of examples. The first one has been done for you.

1) `# big-triangle :: Number, String -> Image`

```
examples:
  big-triangle(100, "red") is triangle(100, "solid", "red")
  big-triangle(200, "orange") is triangle(200, "solid", "orange")
end
```

2)

```
examples:
  purple-square(15) is rectangle(15, 15, "outline", "purple")
  purple-square(6) is rectangle(6, 6, "outline", "purple")
end
```

3)

```
examples:
  sum(5, 8) is 5 + 8
  sum(9, 6) is 9 + 6
  sum(120, 11) is 120 + 11
end
```

4)

```
examples:
  banner("Game Today!") is text("Game Today!", 50, "red")
  banner("Go Team!") is text("Go Team!", 50, "red")
  banner("Exit") is text("Exit", 50, "red")
end
```

5)

```
examples:
  twinkle("outline", "red") is star(5, "outline", "red")
  twinkle("solid", "pink") is star(5, "solid", "pink")
  twinkle("outline", "grey") is star(5, "outline", "grey")
end
```

6)

```
examples:
  half(5) is 5 / 2
  half(8) is 8 / 2
  half(900) is 900 / 2
end
```

7)

```
examples:
  Spanish(5) is "cinco"
  Spanish(30) is "treinta"
  Spanish(12) is "doce"
end
```

# Contracts, Examples & Definitions - bc

We've already found the Contract for gt, made Examples, and described the pattern with a Definition. Let's review the process.

**Directions:** Define a function called gt, which makes solid green triangles of whatever size we want.

## Contract and Purpose Statement

Every contract has three parts...

# gt:: Number -> Image  
function name Domain Range

## Examples

Write some examples, then circle and label what changes...

examples:

gt(10) is triangle(10, "solid", "green")  
function name input(s) what the function produces

gt(20) is triangle(20, "solid", "green")  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun gt(size):  
function name variable(s)

triangle(size, "solid", "green")  
what the function does with those variable(s)

end

Now, let's apply the same steps to think through a new problem!

**Directions:** Define a function called bc, which makes solid blue circles of whatever radius we want.

## Contract and Purpose Statement

Every contract has three parts...

# :: Domain -> Range  
function name

## Examples

Write some examples, then circle and label what changes...

examples:

( ) is   
function name input(s) what the function produces

( ) is   
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun ( ):  
function name variable(s)

what the function does with those variable(s)

end

# Contracts, Examples & Definitions - Stars

**Directions:** Define a function called `sticker`, which consumes a color and draws a solid 50px star of the given color.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `gold-star`, which takes in a radius and draws a solid gold star of that given size.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

# Contracts, Examples & Definitions - Name

**Directions:** Define a function called `name-color`, which makes an image of your name at size 50 in whatever color is given.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `name-size`, which makes an image of your name in your favorite color (be sure to specify your name and favorite color!) in whatever size is given.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end



# Do the Examples Have the Same Contracts?

For each pair of Examples below, decide whether the two examples have the same Contract. If they do, fill in the Contract in the space provided. If not, write a few words explaining how you know their contracts aren't the same.

1) \_\_\_\_\_

```
examples:  
  mystery(30) is 30 * 50  
  mystery(10) is text("Welcome!", 10, "darkgreen")  
end
```

2) \_\_\_\_\_

```
examples:  
  mystery(30, 40) is 40 - (2 * 30)  
  mystery(10, 15) is 15 - (2 * 10)  
end
```

3) \_\_\_\_\_

```
examples:  
  mystery("New York") is text("New York", 20, "red")  
  mystery(20) is text("New York", 20, "red")  
end
```

4) \_\_\_\_\_

```
examples:  
  mystery("green", 32) is circle(32, "outline", "green")  
  mystery(18, "green") is circle(18, "outline", "green")  
end
```

5) \_\_\_\_\_

```
examples:  
  mystery(6, 9, 10) is 6 / (9 + 10)  
  mystery(3, 7) is 3 / (7 + 10)  
end
```

6) \_\_\_\_\_

```
examples:  
  mystery("red", "blue") is text("blue", 25, "red")  
  mystery("purple", "Go Team!") is text("Go Team!", 25, "purple")  
end
```

## Do the Examples Have the Same Contracts? (2)

For each pair of Examples below, decide whether the two examples have the same Contract. If they do, fill in the Contract in the space provided. If not, write a few words explaining how you know their contracts aren't the same.

1) \_\_\_\_\_  
**examples:**  
mystery(triangle(70, "solid", "green")) is triangle(140, "solid", "green")  
mystery(circle(100, "solid", "blue")) is circle(200, "solid", "blue")  
**end**

2) \_\_\_\_\_  
**examples:**  
mystery("red") is triangle(140, "solid", "red")  
mystery("blue", "circle") is circle(140, "solid", "blue")  
**end**

3) \_\_\_\_\_  
**examples:**  
mystery("+", 4, 5) is 4 + 5  
mystery("sqrt", 25) is sqrt(25)  
**end**

4) \_\_\_\_\_  
**examples:**  
mystery("circle", 4) is PI \* sqr(4)  
mystery("square", 5) is sqr(5)  
**end**

5) \_\_\_\_\_  
**examples:**  
mystery("dog") is 3  
mystery("cat") is "kitten"  
**end**

6) \_\_\_\_\_  
**examples:**  
mystery("dog") is 3  
mystery("kitten") is 6  
**end**

## Matching Examples and Contracts (2)

Match each Example on the left with its Contract on the right. NOTE: Multiple examples may match to the same Contract!

Contract	Examples	
<pre>examples:   match(circle(10, "solid", "green")) is rotate (37, circle(10, "solid", "green")) end</pre>	1	A <code># match :: Number, Image -&gt; Image</code>
<pre>examples:   match(triangle(20, "solid", "blue"), 3) is scale(3, triangle(20, "solid", "blue")) end</pre>	2	
<pre>examples:   match(circle(20, "outline", "gold")) is rotate(37, circle(20, "outline", "gold")) end</pre>	3	B <code># match :: Image, Number -&gt; Image</code>
<pre>examples:   match(30, "red") is 30 + string-length("red") end</pre>	4	
<pre>examples:   match(circle(10, "solid", "orange"), 22) is scale(22, circle(10, "solid", "orange")) end</pre>	5	
<pre>examples:   match(10, "blue") is 10 + string-length( "blue") end</pre>	6	C <code># match :: Image -&gt; Image</code>
<pre>examples:   match(5, star(20, "solid", "red")) is rotate( 90 - 5, star(20, "solid", "red")) end</pre>	7	
<pre>examples:   match(abs(-4), "45") is 4 end</pre>	8	D <code># match :: Number, String -&gt; Number</code>

(optional)

# Matching Examples and Contracts (3)

Match each Example on the left with its Contract on the right. NOTE: Multiple examples may match to the same Contract!

Contract	Examples	
<pre>examples:   match(1.5) is "greater than 1" end</pre>	1	
<pre>examples:   match(24) is star(24 * 2, "outline", "purple") end</pre>	2	
<pre>examples:   match(string-length("tabletop")) is "8" end</pre>	3	A # match :: Number -> String
<pre>examples:   match(star(20, "outline", "red"), 3) is 3 *   image-height(star(20, "outline", "red")) end</pre>	4	B # match :: Number -> Image
<pre>examples:   match(circle(10, "solid", "silver"), 16) is   16 * image-height(circle(10, "solid", "silver")) end</pre>	5	C # match :: Number, Number -> Number
<pre>examples:   match("triangle", "blue") is triangle(40,   "outline", "blue") end</pre>	6	D # match :: String, String -> Image
<pre>examples:   match(30) is star(30 * 2, "outline", "purple") end</pre>	7	E # match :: Image, Number -> Number
<pre>examples:   match(string-length("coffee"), string-length(   "tea")) is 6 + 3 end</pre>	8	

# Lookups in a Nutshell

## Let's Review...

We can define names for values in Pyret, the same way we do in math:

```
x = 7
name = "Shanti"
age = 16
logo = star(50, "solid", "red")
snuffles = row-n(animals-table, 1)
```

When **looking up a data Row** from a Table, programmers use the `row-n` function. This function takes a Table and a Number as its inputs. The numbers tell the computer which Row we want from the Table. *Note: Rows are numbered starting at zero!*

For example:

```
row-n(animals-table, 0)      # the first row (Sasha)
row-n(animals-table, 2)      # the third row (Mittens)
```

When we define these rows, it's most useful to name them based on their *properties* (rather than their identifiers, e.g. snuffles):

```
rabbit-row = row-n(animals-table, 1)  # Snuffles is a rabbit
cat-row = row-n(animals-table, 0)      # Sasha is a cat
dog-row = row-n(animals-table, 10)     # Toggle is a dog
```

## What's New?

When **looking up a column** from a Row, programmers use square brackets and the name of the column they want.

For example:

```
row-n(animals-table, 0)["age"]      # look up Sasha's age (in row 0)
cat-row["age"]                      # look up Sasha's age (using the defined name)

# Note: Both of these examples produce the same thing!
# Using defined expressions allows us to simplify our code.
```

Values produced from lookups can be used as part of Pyret expressions:

```
# Number expressions
dog-row["age"] + 2
cat-row["age"] > 10

# String expressions
string-contains(dog-row["name"], "Kujo")
cat-row["name"] == "Sasha"

# Boolean expressions
dog-row["fixed"] and (dog-row["age"] < 5)

# Image expressions
triangle(dog-row["pounds"], "solid", "green")
scale(cat-row["age"], triangle(20, "solid", "green"))
```

# Lookup Questions

The table below represents four pets at an animal shelter:

`pets-table`

name	sex	age	pounds
"Toggle"	"female"	3	48
"Fritz"	"male"	4	92
"Nori"	"female"	6	35.3
"Maple"	"female"	3	51.6

1) Match each Lookup Question (left) to the code that will give the answer (right).

"How much does Maple weigh?"

1

A `row-n(pets-table, 3)`

"Which is the last row in the table?"

2

B `row-n(pets-table, 2)["name"]`

"What is Fritz's sex?"

3

C `row-n(pets-table, 1)["sex"]`

"What's the third animal's name?"

4

D `row-n(pets-table, 3)["age"]`

"How much does Nori weigh?"

5

E `row-n(pets-table, 3)["pounds"]`

"How old is Maple?"

6

F `row-n(pets-table, 0)`

"What is Toggle's sex?"

7

G `row-n(pets-table, 2)["pounds"]`

"What is the first row in the table?"

8

H `row-n(pets-table, 0)["sex"]`

2) For each value on the left, write the Pyret expression that will produce that value on the right. The first one has been completed for you.

a.	"Maple"	<code>row-n(pets-table, 3)["name"]</code>
b.	"male"	
c.	4	
d.	48	
e.	"Nori"	

# Lookup Expressions

Make sure you've opened your **saved copy** of the [Row Functions Starter File](#). The Definitions Area will contain sample Rows such as `lizard-row`, `old-row`, etc.

The code below draws a solid, green triangle, using 5x the age of `old-row` as the size:

```
triangle((5 * old-row["age"]), "solid", "green")
```

For each of the prompts below **write the code** on the blank lines that will produce the desired result. The first one has been done for you.

1) An animal is "old" if it is greater than 10 years old. Is `lizard-row` old?

```
lizard-row["age"] > 10
```

---

2) An animal is "young" if it is less than 1 year old. Is `female-row` young?

---

3) Using `male-row`, draw a solid, blue circle where the radius is the `age` of the row.

---

4) If every week is 7 days, how many *days* did it take for our `rabbit-row` to be adopted?

---

5) If every 2.2 pounds is 1 kilogram, how many *kilograms* does our `rabbit-row` weigh?

---

6) Is the species of our `fixed-row` animal a `"dog"`?

---

7) Is the species of our `young-row` animal a `"cat"`?

---

8) Using `male-row`, draw the species of the animal in red, 15px letters.

---

9) Is `lizard-row` fixed?

---

10) If a year has 52 weeks, how many *years* did it take `unfixed-row` to be adopted?

---

11) Does `old-row` have an "s" in its name?

---

12) Using any Row you like, draw the `name` of the animal in red letters and use the `pounds` of the animal for the font size.

---

★ Draw a solid pink star, using the age of `dog-row` as the radius. Rotate it by the number of pounds it weighs.

---

★ ★ Get creative. Choose one defined Row and think of as many ways as you can to use its columns!

# Functions with Lookups

Open the [Row Functions Starter File](#) on your computer, save a copy, and **Click "Run"**!

1) Write the code to lookup the value of the `age` column for each of the rows listed (the first one has been completed for you).

row	code to lookup the value of the <code>age</code> column
<code>cat-row</code>	<code>cat-row["age"]</code>
<code>dog-row</code>	
<code>old-row</code>	

2) Write the code that uses the `triangle` function to draw a solid, green triangle whose size is 5 times the `age` of the animal (the first one has been completed for you).

row	code to draw a triangle using 5 times the "age" of the row as the radius
<code>cat-row</code>	<code>triangle(5 * cat-row["age"], "solid", "green")</code>
<code>dog-row</code>	
<code>old-row</code>	

3) Check with your partner or another student to confirm that your code matches.

4) What is the name of the animal defined in `old-row`? \_\_\_\_\_ How many years old are they? \_\_\_\_\_

5) How large would you expect their triangle to be? \_\_\_\_\_

## age-gt

Scroll down in the [Row Functions Starter File](#) until you find the Contract, Examples and Definition for `age-gt`.

6) What is the Domain of `age-gt`? \_\_\_\_\_ The Range? \_\_\_\_\_ How many examples are provided? \_\_\_\_\_

7) According to the **comment** below the Contract, what should this function do, when given a Row? \_\_\_\_\_

**Notice:** The first two examples use `cat-row` and `dog-row`. And so do the third and fourth examples!

8) Which pair of examples does the definition look more like? \_\_\_\_\_

9) Why is it helpful to include the first two examples? \_\_\_\_\_

10) Why can't we write our definition using only the first two examples? \_\_\_\_\_

11) In the last two examples the numbers `3` and `1` have been replaced! Where do these examples get the numbers from? \_\_\_\_\_

12) Add an example for `old-row` to match the first pair of examples (using the actual number of age).

13) Then add an example `old-row` to match the second pair of examples (using a lookup).

★ Add another pair of examples using a row of your choosing from the definitions at the top of the file.



# More Practice with Lookups

Consider the `shapes-table` below, and the four value definitions that follow.

name	corners	is-round
"triangle"	3	false
"square"	4	false
"rectangle"	4	false
"circle"	0	true

```
shapeA = row-n(shapes-table, 0)
shapeB = row-n(shapes-table, 1)
shapeC = row-n(shapes-table, 2)
shapeD = row-n(shapes-table, 3)
```

1) Match each Pyret expression (left) to the description of what it evaluates to (right).

`shapeD`      1

A      Evaluates to 4

`shapeA`      2

B      Evaluates to the last row in the table

`shapeB["corners"]`      3

C      Evaluates to "square"

`shapeC["is-round"]`      4

D      Evaluates to true

`shapeB["name"]`      5

E      Evaluates to false

`shapeA["corners"]`      6

F      Evaluates to 3

`shapeD["name"] == "circle"`      7

G      Evaluates to the first row in the table

2) For each value on the left, write the Pyret expression that will produce that value on the right. The first one has been completed for you.

a.	"rectangle"	<code>shapeC["name"]</code>
b.	"square"	
c.	4	
d.	0	
e.	true	

(optional)

# Advanced Table Manipulation in a Nutshell

Pyret has special functions that we can use to manipulate Tables. We've seen some of these already and some will be introduced in this lesson.

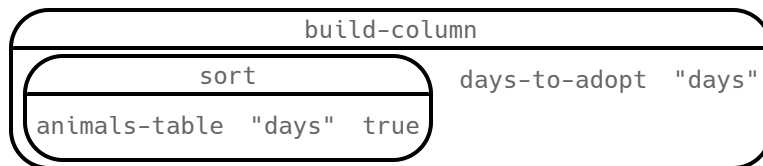
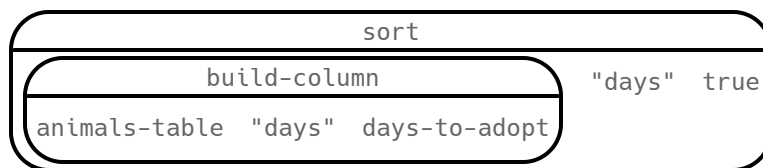
- `sort` - consumes the name of a column and a Boolean value to determine if that table should be sorted by that column in ascending order
- `row-n` - consumes an index (starting with zero!) and produces a Row from a table
- `count` - consumes the name of a column and produces a table that summarizes the number of times each value in the column appears
- `first-n-rows` - consumes a table and a number and produces a new table that includes the provided number of rows
- `filter` - consumes a *Boolean-producing function*, and produces a table containing only rows for which the function returns `true`
- `build-column` - consumes the name of a new column, and a function that produces the values in that column for each Row

We know that there is an "Order of Operations" for things like addition, subtraction, multiplication and division...

Is there an Order of Operations for manipulating tables?

Suppose you want to build a table from the `animals-table` using the `days-to-adopt` function defined below. Consider the two Circles of Evaluation that follow.

```
fun days-to-adopt(r): r["weeks"] * 7 end
```



- One of the Circles of Evaluation will sort the table by the number of days it took for each animal to be adopted.
- One of them will produce an error! Can you figure out which one?

We can't `sort` by a column that doesn't exist yet! In fact, we can't `filter` by that column either.

# Reading Row and Function Definitions

Open the [Table Functions Starter File](#) on your computer, save a copy, and click "Run".

1) What is the name of the Table defined on line 5? \_\_\_\_\_

How many columns does it have? \_\_\_\_\_ How many Rows? \_\_\_\_\_

2) What is the name of the Row defined on line 17? \_\_\_\_\_

3) What data type is `red-circle` defined as: a Number, String, Image, Boolean, Table, or Row? \_\_\_\_\_

Type `red-circle` into the Interactions Area. What do you get? \_\_\_\_\_

4) In the space provided on lines 19 and 20, add new definitions for two more Rows from this table.

5) Read the Contract on line 22.

What is the function's name? \_\_\_\_\_ Domain? \_\_\_\_\_ Range? \_\_\_\_\_

6) Type `is-red( blue-triangle )` into the Interactions Area. What do you get? \_\_\_\_\_

Then use the function `is-red`, passing in a different row. Explain what the `is-red` function does. \_\_\_\_\_

7) What other functions are defined in the starter file? \_\_\_\_\_

For each of the remaining functions, read the code and try to guess what it does **before** testing it out by passing in a Row.

8) What does `is-polygon` do? \_\_\_\_\_

9) What does `lookup-name` do? \_\_\_\_\_

10) What does `is-triangle` do? \_\_\_\_\_

11) Define two new functions: `is-green` and `is-blue`.

★ There is a hidden function called `draw-shape`. Try to use it. What is its Domain and Range? What does it do?

★ How else could we define `is-polygon`, without using the "polygon" column at all?

# Exploring Table Functions

Open your copy of the [Table Functions Starter File](#) and click "Run".

## Filtering Rows

1) Evaluate `filter(shapes-table, is-red)` in the Interactions Area. Describe the value you get back below.

2) Evaluate `filter(shapes-table, is-polygon)` in the Interactions Area. Describe the value you get back below.

3) Write the code to generate a table of only triangles. \_\_\_\_\_

Add your code to the *bottom* of the Definitions Area.

Click "Run" and evaluate `triangles` in the Interactions Area to confirm that it does what it's supposed to do before you continue.

4) Record the code to define `reds` to be a table of only red shapes. \_\_\_\_\_

5) What do the contracts for `is-red`, `is-polygon`, and `is-triangle` have in common? \_\_\_\_\_

6) Find the Contract for `filter` on the [Contracts Page](#). Explain how `filter` uses the two inputs specified in the Domain.

*If you're working with a printed workbook, the contracts pages are included in the back.*

7) What happens if you evaluate `filter(shapes-table, lookup-name)`? Why? \_\_\_\_\_

## Building Columns

8) What does `build-column(shapes-table, "red", is-red)` evaluate to? \_\_\_\_\_

9) What does `build-column(shapes-table, "img", draw-shape)` evaluate to? \_\_\_\_\_

10) Find the Contract for `build-column` on the [Contracts Page](#). Explain how `build-column` uses the three inputs in the Domain.

*If you're working with a printed workbook, the contracts pages are included in the back.*

## Define your own table!

★ In the Definitions Area, define a table of your own using `filter` or `build-column`. Add a comment to describe what's in it!

# What Table Do We Get?

Consider the table below, and the four function definitions that follow:

The table `t` below represents four animals from the shelter:

name	sex	age	fixed	species	pounds
"Toggle"	"female"	12	true	"dog"	48
"Fritz"	"male"	4	false	"dog"	92
"Nori"	"female"	6	true	"dog"	35.3
"Sunflower"	"female"	2	false	"cat"	51.6

```

fun lookup-fixed(animal): animal["fixed"]
fun is-dog(animal):       animal["species"] == "dog"
fun is-old(animal):       animal["age"] > 10
fun label(animal):        text(animal["name"], 20, "red")
end
end
end
end

```

Below is a list of expressions, each using one table function. Match each expression to the description of the table it will produce.

`sort(t, "age", true)`

1

A

Produces a table with Toggle, Fritz, and Nori - but not Sunflower.

`sort(t, "pounds", false)`

2

B

Produces a table of all four animals, sorted youngest-to-oldest

`build-column(t, "sticker", label)`

3

C

Produces a table, with only Toggle.

`filter(t, is-old)`

4

D

Produces an identical table with an extra column called "dog", whose values are true, true, true, false

`filter(t, lookup-fixed)`

5

E

Produces a table containing only Nori and Toggle.

`filter(t, is-dog)`

6

F

Produces a table with all four animals, sorted from heaviest to lightest.

`build-column(t, "dog", is-dog)`

7

G

Won't run: will produce an error. (Why?)

`filter(t, label)`

8

H

Produces an identical table with an extra column called "sticker", whose values are images

# Putting it All Together

Open the [Putting it All Together Starter File](#) and take a look at the helper functions in the Definitions Area.

Write the names of those functions here: \_\_\_\_\_  
\_\_\_\_\_

## Filter and Building with our Helper Functions

Example: Make a table of only dogs (define it as `dogs`)

`dogs = filter(animals-table, is-dog)`

1) Make a table of only fixed animals (define it as `fixed`)

`fixed =` \_\_\_\_\_

2) Make a table with a column called "sticker", containing a label for every animal

`stickers =` \_\_\_\_\_

3) Make a table of only fixed dogs (define it as `fixed-dogs`)

`fixed-dogs =` \_\_\_\_\_

★ Make a table of old, fixed dogs... with a "sticker" column! (define it as `sticker-table`)

`sticker-table =` \_\_\_\_\_

## Define Additional Helper Functions

4) Define a function called `is-lizard`, which consumes a `Row` of the animals table and *computes* whether the animal is a lizard.

5) Define a function called `months`, which consumes a `Row` of the animals table and divides the weeks by `4.435` to get the approximate equivalent number of months to adoption.

★ Make a table with a "months" column (define it as `months-table`)

## Make Visualizations Using Your New Tables

6) Make a pie chart showing the sex of only fixed dogs.

7) Make a dot plot showing the distribution of months to adoption.

★ Make a scatter plot of old, fixed dogs, comparing age to pounds using the "sticker" as the label!

# Function Cards

Print and cut these out, for use with the **Filter** activity in this lesson. You can make up your own using the blanks provided at the bottom!

```
# has-glasses :: Student -> Boolean
# consumes a student, produces true if they are
wearing glasses
```

```
# is-taller :: Student -> Boolean
# consumes a student, and produces true if they
are taller than you
```

```
# has-long-hair :: Student -> Boolean
# consumes a student, and produces true if they
have long hair
```

```
# has-red-hair :: Student -> Boolean
# consumes a student, and produces true if they
have red hair
```

```
# is-shorter :: Student -> Boolean
# consumes a student, and produces true if they
are shorter than you
```

```
# is-smiling :: Student -> Boolean
# consumes a student, and produces true if they
are smiling
```

```
# starts-with-vowel :: Student -> Boolean
# consumes a student, and produces true if the
first letter of their name is a vowel
```

```
# wears-jeans :: Student -> Boolean
# consumes a student, and produces true if they
are wearing jeans
```

# Circles of Evaluation for Filtering and Building a New Table

To complete this page, open the [Putting it All Together Starter File](#).

- 1) Draw the Circles of Evaluation for how you would combine the relevant functions from the starter file to make:  
A new table of just the old cats at the shelter with an added column for weight in "kilos".

- 2) Translate the Circles of Evaluation above into the code you'll type into Pyret.

---

---

- 3) Test out the expression you wrote in the starter file.

- 4) What do you Notice and Wonder when you look at the display?

---

---

---

---



# Circles of Evaluation for Filtering and Building a Dot Plot

To complete this page, open the [Putting it All Together Starter File](#).

- 1) **Draw the Circles of Evaluation** for how you would combine the relevant functions from the starter file:  
A dot-plot showing the distribution of the weight (in kilos) of young dogs at the shelter.

- 2) Translate the Circles of Evaluation above into the code you'll type into Pyret.

---

---

- 3) Test out the expression you wrote in the starter file.

- 4) What do you Notice and Wonder when you look at the display?

---

---

---

---

# Circles of Evaluation for Filtering and Building a Scatter Plot

To complete this page, open the [Putting it All Together Starter File](#).

- 1) **Draw the Circles of Evaluation for** for how you would combine the relevant functions from the starter file to make the display:  
A scatter plot showing the relationship between kilograms and weeks to adoption for old dogs at the shelter...

- 2) Translate the Circles of Evaluation above into the code you'll type into Pyret.

---

---

- 3) Test out the expression you wrote in the starter file.

- 4) What do you Notice and Wonder when you look at the display?

---

---

---

---

# Defining Table Functions in a Nutshell

The steps of the Design Recipe don't change just because we're working with Rows, but we can make some adjustments when using Row-consuming functions to filter tables and build columns!

Let's try a concrete example: Write a function `is-lizard`, which tells us whether an animal is a lizard

## Contract and Purpose

- We still want to pick good names. Since we're writing a function to check if an animal is a lizard, call it `is-lizard`!
- The Domain is a lot easier — it's *always* a Row!
- The Range is easier, too. If we're writing a function to filter a Table, we know the Range *has to be a Boolean*. (What would it be if we were building a column of Numbers? Images? Strings?)

## Examples

The goal of the Examples step is to *find the pattern* that represents what the function does. When working with Rows, sometimes we have to start by just focusing on what the answer should be.

Suppose we have two rows defined:

`lizard-row` (which happens to be a lizard)      `cat-row` (which happens to be a cat)

We can imagine the answers for an `is-lizard` function to be...

```
examples:
  is-lizard(lizard-row) is true
  is-lizard(cat-row)   is false
end
```

But why do we think these expressions will evaluate to `true` and `false`?

We *KNOW* `lizard-row` is a lizard, and we *KNOW* `cat-row` is a cat and not a lizard...

If we replace our answers with the Boolean expressions that compare their species, someone else would be able to follow our logic.

```
examples:
  is-lizard(lizard-row) is "lizard" == "lizard" # will produce true
  is-lizard(cat-row)   is "cat"    == "lizard"  # will produce false
end
```

And what work would the computer need to do to know that `lizard-row` is a lizard and `cat-row` is a cat? Look in the `species` column!

```
examples:
  is-lizard(lizard-row) is lizard-row["species"] == "lizard" # will produce true
  is-lizard(cat-row)   is cat-row["species"]    == "lizard"  # will produce false
end
```

Sometimes we can get straight to this final form in one step, but sometimes it helps to break our thinking down into pieces.

Once we see the pattern, we can *circle and label what changes*.

In this case, only the Row representing the animal changes! So we might use `r` as our label, to represent the Row.

## Definition

The final step in the Design Recipe is to take the pattern from our examples and *generalize it* to work with any input.

It's no different when working with Rows.

Our previous step is a huge help. We can **copy everything that stays the same**, and replace the part that changes with the label we used.

Combining the Contract, Purpose, Examples and Definitions, we end up with:

```
# is-lizard :: Row -> Boolean
# Consumes a Row, and checks to see if the species column is "lizard"
examples:
  is-lizard(lizard-row) is lizard-row["species"] == "lizard" # will produce true
  is-lizard(cat-row)   is cat-row["species"]    == "lizard"  # will produce false
end
fun is-lizard(r): r["species"] == "lizard" end
```

## Matching Data Science Problems and Purpose Statements

Match each data science problem below to its corresponding purpose statement.

Data Science Problem	Purpose Statement
Steve wants a function that will look at an animal from the <code>animals-table</code> , and return true if it's older than six.	<div>1</div> <div>A</div> <div>Consume a Row, and check if <code>species == "cat"</code> and <code>age &lt; 1</code></div>
Mandolin wants a function that will draw a red star for each animal in the shelter. The size of the star should be a measure of how many pounds the animal weighs.	<div>2</div> <div>B</div> <div>Consume a Row, and produce a solid red star using <code>points</code> as the radius.</div>
Tara wants to see a table of ONLY cats, rabbits, and tarantulas. She needs a function that will check if an animal is one of those species.	<div>3</div> <div>C</div> <div>Consume a Row, and check if <code>age &gt; 6</code></div>
Bharti is looking for kittens, so she wants a function that only returns true if the animal is a cat AND is less than 1 year old.	<div>4</div> <div>D</div> <div>Consume a Row, and check if <code>species == "cat"</code>, <code>species == "rabbit"</code>, or <code>species == "tarantula"</code></div>

# Writing Examples from Purpose Statements

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

## Contract and Purpose Statement

Every contract has three parts...

# *is-young*:: \_\_\_\_\_ *Row* *Boolean*  
function name Domain Range  
# *Consumes a Row checks to see if age < 1.*  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces  
\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces  
end

## Contract and Purpose Statement

Every contract has three parts...

# *is-lizard*:: \_\_\_\_\_ *Row* *Boolean*  
function name Domain Range  
# *Consumes a Row, and checks if species = "lizard"*  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces  
\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces  
end

# Writing Examples from Purpose Statements (2)

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

## Contract and Purpose Statement

Every contract has three parts...

# <u>age-dot::</u>	<u>Row</u>	->	<u>Image</u>
function name	Domain		Range
# <u>Consumes a Row draws a solid green circle using age for the radius.</u>			
what does the function do?			

## Examples

Write some examples, then circle and label what changes...

examples:

_____	( _____ )	is	_____
function name	input(s)		what the function produces
_____	( _____ )	is	_____
function name	input(s)		what the function produces

end

## Contract and Purpose Statement

Every contract has three parts...

# <u>kilos::</u>	<u>Row</u>	->	<u>Number</u>
function name	Domain		Range
# <u>Consumes a Row, and divides pounds by 2.2 to produce the weight in kg</u>			
what does the function do?			

## Examples

Write some examples, then circle and label what changes...

examples:

_____	( _____ )	is	_____
function name	input(s)		what the function produces
_____	( _____ )	is	_____
function name	input(s)		what the function produces

end

# Fixing Purpose Statements

Beneath each of the data science problems below is a purpose statement (generated by ChatGPT!) that is either missing information or includes unnecessary information.

- Write an improved version of each purpose statement beneath the original.
- Then, explain what was wrong with the ChatGPT-generated Purpose Statement.

1) **Data Science Problem:** *Alice is looking to adopt a pet, but only wants to look at animals who are fixed. Write a function `is-fixed`, which takes in a Row and returns true if the animal is fixed. Otherwise, return false.*

**The AI's Purpose Statement:** Take in a Row and check if the "is-fixed" column is true.

**Improved Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

**Problem with the AI's Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

2) **Data Science Problem:** *The animal shelter wants to make nametags for all the animals, drawing their names in large purple letters*

**The AI's Purpose Statement:** Given an animal, use the "name" column to draw the text in size 100 font.

**Improved Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

**Problem with the AI's Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

3) **Data Science Problem:** *The animal shelter decides that some dogs need to go on a diet, and get them different food to help them lose weight. Write a function `is-heavy`, which takes in a Row and checks to see if it's a dog weighing more than 100 pounds.*

**The AI's Purpose Statement:** Take in the species and the number of pounds, and check if the species is dog and it weighs a lot.

**Improved Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

**Problem with the AI's Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

4) **Data Science Problem:** Sammi wants to adopt a kitten less than a year old.

**The AI's Purpose Statement:** Take in a row, and check if the age is less than 1.

**Improved Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

**Problem with the AI's Purpose Statement:** \_\_\_\_\_  
\_\_\_\_\_

## The Design Recipe: days / years

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `days-to-adopt`, which computes the number of days it took an animal to be adopted by multiplying the number of weeks by 7. We've started both examples for you.

## Contract and Purpose Statement

Every contract has three parts...

# <i>days-to-adopt::</i> function name	Row Domain	-> <i>Number</i> Range
#	what does the function do?	

## Examples

Write some examples, then circle and label what changes...

**examples:**

<u>days-to-adopt(</u>	<u>fixed-row</u>	) is	<u>7 * fixed-row["weeks"]</u>	what the function produces
function name	input(s)			
<u>days-to-adopt(</u>	<u>unfixed-row</u>	) is	<u>7 * unfixed-row["weeks"]</u>	what the function produces
function name	input(s)			

end

### Definition

Write the definition, giving variable names to all your input values...

```

fun _____ ( _____ ):
    _____
    _____
    _____
    _____
end

```

**Directions:** Define a function called `years-to-adopt`, which divides the number of weeks by 52 to compute the number of years it took to be adopted.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name                  Domain                  Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name                      input(s)                      what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name                      input(s)                      what the function produces

end

### Definition

Write the definition, giving variable names to all your input values...

```
fun _____ ( _____ ):
    _____
end
```



# The Design Recipe: few-legs / many-legs

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `few-legs`, which consumes a Row of the animals table and *computes* whether it has fewer than 4 legs. HINT: use predefined rows like `snail-row` to make your examples easier!

## Contract and Purpose Statement

Every contract has three parts...

# few-legs:: Row -> Boolean  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

few-legs(snail-row) is snail-row["legs"] < 4  
function name input(s) what the function produces

few-legs(cat-row) is cat-row["legs"] < 4  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(                    ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `many-legs`, which consumes a Row of the animals table and *computes* whether it has more than 4 legs. HINT: use predefined rows like `dog-row` to make your examples easier!

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_(                    ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_(                    ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(                    ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

# The Design Recipe: get-name / name-has-s

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `get-name`, which returns the name of the animal

## Contract and Purpose Statement

Every contract has three parts...

# get-name:: Row -> String  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

get-name(cat-row) is cat-row["name"]  
function name input(s) what the function produces

get-name(young-row) is young-row["name"]  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(  
function name variable(s):

\_\_\_\_\_

what the function does with those variable(s)

end

**Directions:** Define a function called `name-has-s`, which returns true if an animal's name contains the letter "s". HINT: The name of the animal in `cat-row` is "Sasha" and the name of the animal in `dog-row` is "Toggle".

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_(  
function name input(s) is \_\_\_\_\_  
what the function produces

\_\_\_\_\_(  
function name input(s) is \_\_\_\_\_  
what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(  
function name variable(s):

\_\_\_\_\_

what the function does with those variable(s)

end

# The Design Recipe: is-male / is-female

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `is-male`, which consumes a `Row` of the `animals` table and *computes* whether the sex of the animal is male. HINT: use predefined rows like `male-row` to make your examples easier!

## Contract and Purpose Statement

Every contract has three parts...

# is-male:: Row -> Boolean  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

is-male( male-row ) is male-row["sex"] == "male"  
function name input(s) what the function produces

is-male( female-row ) is female-row["sex"] == "male"  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `is-female`, which consumes a `Row` of the `animals` table and returns true if the animal is female. HINT: use predefined rows like `female-row` to make your examples easier!

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

# The Design Recipe: is-rabbit / is-lizard

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `is-rabbit`, which consumes a Row of the animals table and *computes* whether the animal is a rabbit.

*HINT: use predefined rows like `rabbit-row` to make your examples easier!*

## Contract and Purpose Statement

Every contract has three parts...

# is-rabbit:: Row -> Boolean  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

is-rabbit( dog-row ) is dog-row["species"] == "rabbit"  
function name input(s) what the function produces

is-rabbit( rabbit-row ) is rabbit-row["species"] == "rabbit"  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `is-lizard`, which consumes a Row of the animals table and *computes* whether the animal is a lizard.

*HINT: use predefined rows like `lizard-row` to make your examples easier!*

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

# The Design Recipe: ounces / grams

Complete all steps of the Design Recipe to solve both of the problems below. We've provided a start to the first problem as a model.

**Directions:** Define a function called `ounces`, which consumes a Row of the animals table and computes the number of ounces the animal weighs (1 lb = 16oz). *HINT: use predefined rows like `cat-row` to make your examples easier!*

## Contract and Purpose Statement

Every contract has three parts...

# ounces:: Row -> Number  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

ounces(dog-row) is 16 \* dog-row["pounds"]  
function name input(s) what the function produces

ounces(cat-row) is 16 \* cat-row["pounds"]  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(variable(s)):  
function name

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called `grams`, which consumes a Row of the animals table and computes the weight of the animal in *grams* (1 lb is roughly 454 grams). *HINT: use predefined rows like `cat-row` to make your examples easier!*

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_(input(s)) is \_\_\_\_\_  
function name what the function produces

\_\_\_\_\_(input(s)) is \_\_\_\_\_  
function name what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_(variable(s)):  
function name

\_\_\_\_\_ what the function does with those variable(s)

end

# Advanced Data Visualizations in a Nutshell

## Functions as Data

You've learned that functions are ***machines that consume and produce values***.

In the real world, we see machines consume things to produce things all the time:

- Bulbs consume electricity and produce light.
- Toasters consume bread and produce toast.

Sometimes, machines consume other machines:

- A school bus is a machine. It comes with a stereo, which could be swapped out for a new one with more features. A stereo is a machine. And the bus needs one of them in order to play music over the speakers.
- A blender might have different attachments. Each attachment is a machine of its own and the blender needs one of them to work!

This is true of function machines in math and programming, as well! By now you've learned plenty of data types (e.g. - Numbers, Strings, Images, Booleans, Rows and Tables). ... **And Functions can be their own kind of data type!**

- Imagine a function `species-dot`, that consumes a Row from the Animals Dataset, and produces a different-colored square depending on the species.
- What if we used `species-dot` to customize the dots on our scatterplot, instead of using the same blue dot for each animal?  
*In this example, we'd be using the `species-dot` function as an input to our `scatter-plot` function!*

Here are the Contracts for some special display **functions that consume functions**, including the scatter plot we just described:  
*Look carefully at the last argument in each Domain. In each case, **the function consumes a Row and produces an Image**.*

```
# image-scatter-plot :: Table, String, String, (Row -> Image) -> Image
# image-histogram :: Table, String, Number, (Row -> Image) -> Image
# image-bar-chart :: Table, String, (Row -> Image) -> Image
# image-pie-chart :: Table, String, (Row -> Image) -> Image
```

## Piecewise Functions

Functions always apply a particular rule to their input.

- In an earlier lesson, you saw how `gt` always draws a solid, green triangle using the input as the size.
- In the `species-dot` example above, there's no single rule that will generate a different color for each species.

**We need a way for functions to change rules, depending on their input.**

**Piecewise Functions** are functions that can behave one way for part of their Domain, and another way for a different part.

- Piecewise functions are divided into "pieces".
- Each piece has two parts: the "if" and the "then".
- This tells the computer *when* to apply each rule, and *what* the rule is.

In our `species-dot` example, our function might draw black squares when the input is a dog, but orange squares when the input is a cat. The function definition would look like this:

```
# species-dot :: (Row) -> Image
fun species-dot(r):
  if (r["species"] == "dog"): square(5, "solid", "black")
  else if (r["species"] == "cat"): square(5, "solid", "orange")
  else if (r["species"] == "rabbit"): square(5, "solid", "pink")
  else if (r["species"] == "tarantula"): square(5, "solid", "red")
  else if (r["species"] == "lizard"): square(5, "solid", "green")
  end
end
```

# age-bc

1) Write the code to lookup the value of the `age` column for each of the rows listed (the first one has been completed for you).

row	code to lookup the value of the <code>age</code> column
dog-row	<code>dog-row["age"]</code>
old-row	
young-row	

2) Write the code that uses the `circle` function to draw a solid, blue circle whose radius is the *age of the animal* for each of the rows listed (the first one has been completed for you).

row	code to draw a circle using the "age" of the row as the radius
dog-row	<code>circle(dog-row["age"], "solid", "blue")</code>
old-row	
young-row	

3) Check with your partner or another student to confirm that your code matches.

*Instead of writing repetitive code like this over and over for each animal, let's define a function to do it for us!*

## Defining the Function

**Directions:** Define a function called `age-bc`, which takes in a row from the Animals Table and draws a solid, blue circle whose radius is the age of the animal. *HINT: Use the rows from above in your examples!*

### Contract and Purpose Statement

Every contract has three parts...

# `age-bc::` \_\_\_\_\_ *Row* \_\_\_\_\_ -> *Image*  
 function name Domain Range

### Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
 function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
 function name input(s) what the function produces

end

### Definition

Write the definition, giving variable names to all your input values...

fun `age-bc`( \_\_\_\_\_ ): \_\_\_\_\_  
 function name variable(s) what the function does with those variable(s)

end

# species-tag

To help you with this page, we've re-printed the Contract for the `text` function, and an example of how to use it.

(Remember, you can always refer to the [Contracts Pages](#). If you're working with a printed workbook, they are included in the back.)

```
# text :: (String, Number, String) -> Image
           message      size      color
```

```
text("hello", 24, "green")
```

1) On the three lines below, write the code to lookup the value of the `species` column from `dog-row`, `old-row`, and `young-row`.

---

---

---

2) On the three lines below, write the code that uses the `text` function to show the species of those same three rows in *red, 15px letters*.

---

---

---

3) Check with your partner or another student. Do you have the same code? Why or why not?

*Instead of writing this out over and over for each animal, let's define a function to do it for us!*

## Defining the Function

**Directions:** Define a function called `species-tag`, which takes in a row from the Animals Table and draws its name in red, 15px letters.

*HINT: Use of the rows from above in your examples!*

### Contract and Purpose Statement

Every contract has three parts...

# <code>species-tag</code> ::	Row	->	Image
function name	Domain		Range

### Examples

Write some examples, then circle and label what changes...

**examples:**

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name                      input(s)                      what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name                      input(s)                      what the function produces

end

### Definition

Write the definition, giving variable names to all your input values...

```
fun species-tag( _____ ):
  function name                      variable(s)
```

\_\_\_\_\_ what the function does with those variable(s)

end



# Exploring Image Scatter Plots

Look at the code in the [Custom Scatter Plot Starter File](#).

1) Compare the definitions of `age-dot` and `species-tag` to what you wrote. Are they the same? If not, what is different?

---

---

Answer the following questions about the last line of code in the file, which is commented out.

2) What is the **name** of the function being used here? \_\_\_\_\_ How many things are in its **Domain**? \_\_\_\_\_

3) What is the 1st argument? \_\_\_\_\_ What is its **data type**? \_\_\_\_\_

4) What is the 2nd argument? \_\_\_\_\_ What is its **data type**? \_\_\_\_\_

5) What is the 3rd argument? \_\_\_\_\_ What is its **data type**? \_\_\_\_\_

6) What is the 4th argument? \_\_\_\_\_

7) What is the **data type** of the fourth argument in the Domain? If you're not sure, write down your thinking. What can you rule out? What do you think it *might* be? \_\_\_\_\_

---

8) **Uncomment the last line at the bottom of the file, and click "Run".** What does `image-scatter-plot` do with its 4th argument?

---

---

9) Try changing your `age-dot` function to use different colors, or even different shapes! Can you make the size of the shape be *one half* the age of the animal?

10) **On a new line in the Definitions Area, try making an `image-scatter-plot` using the `species-tag` function.**

Click run, and describe what you see. \_\_\_\_\_

---

## Understanding Custom Visualizations

11) **Look at the image scatter plot that has dots of different sizes.**

Can you draw any conclusions about animals that are both *young* and *lightweight*? \_\_\_\_\_

---

12) Looking at that same scatter plot, the director of the shelter says: "Animals that are older *and* that weigh more than 50 pounds generally take at least 5 weeks to be adopted." Do you agree with this statement? Explain. \_\_\_\_\_

---

13) **Look at your image scatter plot with species nametags in red.**

What does this chart reveal that we couldn't see on the original (pounds v. weeks) scatter plot? \_\_\_\_\_

---

# Exploring Conditional / Piecewise Functions

Here's an example of a piecewise function with 3 "pieces" (or "conditions"):

```
# species-dot :: (Row) -> Image
fun species-dot(r):
  if (r["species"] == "dog"):      square(5, "solid", "black")
  else if (r["species"] == "cat"): square(5, "solid", "orange")
  else if (r["species"] == "lizard"): square(5, "solid", "green")
end
```

What do you Notice about this code?	What do you Wonder?

1) What will this function produce for a dog? \_\_\_\_\_

2) What will this function produce for a cat? \_\_\_\_\_

Open the [Piecewise Visualizations Starter File](#), and click "Run".

3) Compare the regular scatter plot with the image scatter plot. What can you see now that you couldn't see before?

---

---

4) Compare the regular histogram with the image histogram. What can you see now that you couldn't see before?

---

---

5) What do you think will happen if we run the function on a species that it has no condition for? \_\_\_\_\_

6) Comment out line 41 to "turn off" the condition for snails, by adding a (#) at the beginning of the line. Click Run and test your prediction. In your own words, describe how piecewise / conditional functions work.

---

---

---

★ Make a new function (don't delete `species-dot`!), which uses piecewise functions to draw something different! For example, have it draw different shapes depending on whether an animal is younger than 3 years old or not.

# Word Problem: fixed-dot

**Directions:** We want to generate a custom dot for our `image-scatter-plot`, to distinguish between animals that are fixed and unfixed. Write a function called `fixed-dot`, which takes in a Row from the `animals` table and generates a 5-pixel solid green dot if the animal is fixed and a 5-pixel black dot if the animal is not fixed.

**Every contract has three parts...**

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

**Write some examples, then circle and label what changes...**

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

**Write the definition, giving variable names to all your input values...**

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)  
\_\_\_\_\_  
what the function does with those variable(s)

end

# Animal Image - Explore

Open the [Animal Images Starter File](#) and look at the code.

What do you Notice?	What do you Wonder?

1) How is this program similar to the last one we looked at?

---

---

2) How is the code different from the other `image-scatter-plot` programs we've seen?

---

---

3) Click "Run". How does using clip art help us to better understand the data?

---

---

4) What risks might there be to using clip art for data that describes humans?

---

5) We have seen `image-scatter-plot` used to make a lot of different custom scatter plots. How could you use `image-scatter-plot` in your own analysis?

---

---

---

---

(optional)

# Dots for Value Ranges - Explore

Open the [Dots for Value Ranges Starter File](#) and look at the code.

What do you Notice?	What do you Wonder?

1) How is this program similar to the last one we looked at?

---

---

2) How is the code for `weight-dot` different from other functions we've seen?

---

---

3) Can you explain how this code works?

---

---

---

---

# Composing Table Operations

The table `t` below represents four animals from the shelter:

name	sex	age	fixed	pounds
"Susie Q"	"female"	0.6	true	54
"Fritz"	"male"	4	true	92
"Nori"	"female"	6	true	35.3
"Rebel"	"female"	0.3	false	4

```

fun is-fixed(r): r["fixed"]
fun is-young(r): r["age"] < 1
fun nametag(r): text(r["name"], 20, "red")
end
end
end

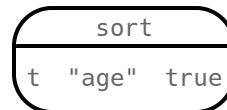
```

Match each table description on the left, to the Circle of Evaluation that will produce it.

A table containing only Susie Q and Rebel

1

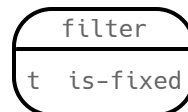
A



Produces a table of only young, fixed animals

2

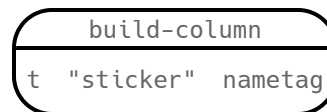
B



Produces a table, sorted youngest-to-oldest

3

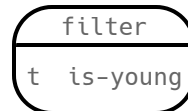
C



Produces a table with an extra column, named "sticker"

4

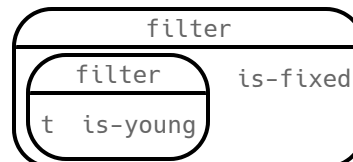
D



Produces a table containing Susie Q and Rebel, in that order

5

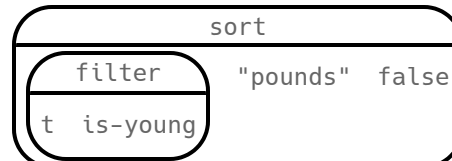
E



Produces a table containing Susie Q, Fritz, and Nori

6

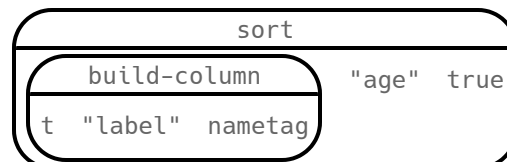
F



Won't run: will produce an error (why?)

7

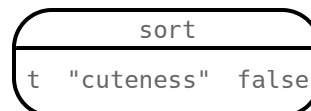
G



Produces a table with an extra "label" column, sorted youngest-to-oldest

8

H



# Composing Table Operations: Order Matters!

In table `t` below, fill in the "kilos" values by dividing each of the 4 animals' `pounds` column value by 2.2.

name	sex	age	fixed	pounds	kilos
"Toggle"	"female"	3	true	21.81	
"Fritz"	"male"	4	true	92	
"Nori"	"female"	6	true	35.3	
"Sasha"	"female"	1	false	6.5	

Then consider the table and the 2 function definitions.

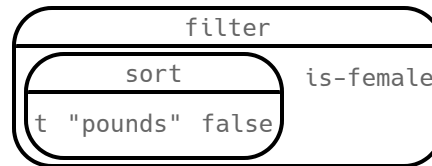
```
fun is-female(r): r["sex"] == "female" end
fun kilograms(r): r["pounds"] / 2.2 end
fun is-heavy(r): r["kilos"] > 25 end
```

Match each table description on the left, to the Circle of Evaluation that will produce it.

Produces a table containing Toggle, Nori and Sasha, with an extra column showing their weight in kilograms

1

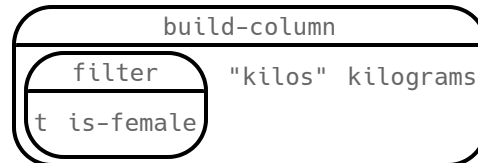
A



Produces a table containing Sasha, Nori and Toggle (in that order)

2

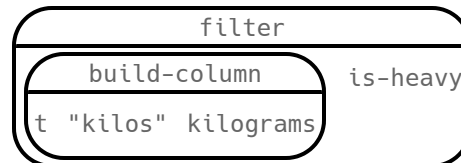
B



Produces a table with an extra column for kilos, but only animals with more than 25 kilos

3

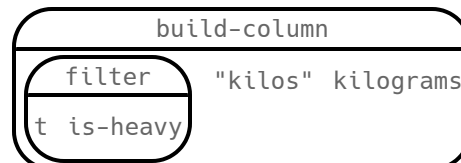
C



Won't run: will produce an error (if so, why?)

4

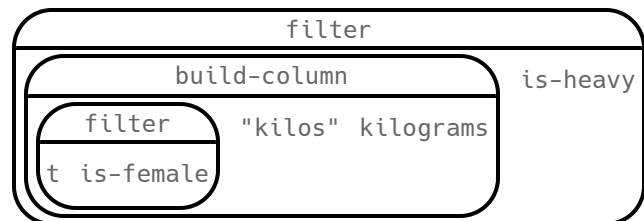
D



Produces a table containing Sasha, Toggle, and Nori (in that order) and adds an extra column showing their weight in kilograms

5

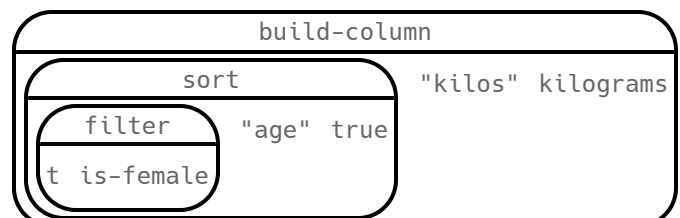
E



Produces an empty table - with no animals at all!

6

F



# From Circles to Code

The table `t` below represents four animals from the shelter:

name	sex	age	fixed	species	pounds
"Toggle"	"female"	12	true	"dog"	48
"Fritz"	"male"	4	false	"dog"	92
"Nori"	"female"	6	true	"dog"	35.3
"Sunflower"	"female"	2	false	"cat"	11.6

Define the functions specified below by filling in the blanks. The first one has been done for you.

- 1) `is-cat`: is the animal is a cat? `fun is-cat(r): r["species"] == "cat" end`
- 2) `is-dog`: is the animal is a dog? `fun is-dog(r): _____ end`
- 3) `is-big`: does the animal weigh more than 50 lbs? `fun is-big(r): _____ end`

Convert each Circle of Evaluation below into Pyret code. What do you think the resulting table will be? The first one has been done for you.

	Circle of Evaluation	Produces...
4)		<p>A table of only dogs, sorted alphabetically in <b>descending</b> order: Toggle, Nori, Fritz</p> <pre>sort(filter(t, is-dog), "name", false)</pre>
5)		
6)		
7)		
8)		



# Planning Table Operations

Consider the table below, and the function definitions that follow:

The table `t` below represents four animals from the shelter:

name	sex	age	fixed	pounds
"Susie Q"	"female"	0.6	true	54
"Fritz"	"male"	4	true	92
"Nori"	"female"	6	true	35.3
"Rebel"	"female"	0.3	false	4

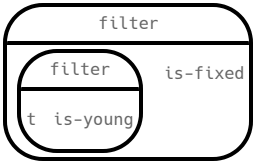
```

fun is-female(r): r["sex"] == "female" end
fun is-young(r):  r["age"] < 1          end
fun is-fixed(r):  r["fixed"]           end
  
```

For each prompt on the left, draw the Circle of Evaluation that will produce the desired table or display.

Prompt	Circle of Evaluation
--------	----------------------

- 1) Produce a Table containing all young, fixed animals



- 2) Produce a Table showing all fixed female animals, sorted by age

- 3) Produce a box-plot for all fixed female animals, showing the distribution of age

- 4) Produce a pie-chart for all young, fixed animals, showing the distribution of sex

## From Circles to Code (2)

The table `t` below represents four animals from the shelter:

name	sex	age	fixed	species	pounds
"Toggle"	"female"	12	true	"dog"	48
"Fritz"	"male"	4	false	"dog"	92
"Nori"	"female"	6	true	"dog"	35.3
"Sunflower"	"female"	2	false	"cat"	51.6

Define the functions specified below by filling in the blanks. The first one has been done for you.

- 1) `is-fixed` : is the animal fixed? `fun is-fixed(r):` `r["fixed"]` `end`
- 2) `kilograms` : divides pounds by 2.2. `fun kilograms(r):` \_\_\_\_\_ `end`
- 3) `is-female` : is the animal female? `fun is-female(r):` \_\_\_\_\_ `end`

Convert each Circle of Evaluation below into Pyret code. What do you think the resulting table will be? The first one has been done for you.

	Circle of Evaluation	Pyret code
4)		<p>A table with all four animals sorted alphabetically by name, and an extra column "kg" showing their weight in kilograms: Fritz, Nori, Sunflower, Toggle</p> <pre>sort(build-column(t, "kg", kilograms), "name", true)</pre>
5)		
6)		
7)		
8)		

## Grouped Samples from the Animals Dataset

Use function composition to define the **grouped samples** below. We've given you the solution for the first sample, to get you started.

Assume that the following helper functions are defined exactly the way they are in the [Grouped Samples Starter File](#): `is-old`, `is-young`, `is-cat`, `is-dog`, `is-female`, `is-fixed`, and `name-has-s`.

	Subset	The code to define that subset
1)	Kittens	<code>kittens = filter(filter(animals-table, is-cat), is-young)</code>
2)	Puppies	
3)	Fixed Cats	
4)	Cats with "s" in their name	
5)	Old Dogs	
6)	Fixed Animals	
7)	Old Female Cats	
8)	Fixed Kittens	
9)	Fixed Female Dogs	
10)	Old Fixed Female Cats	

# Visualizing Data

Fill in the tables below, then use Pyret to make the following visualizations. Record the code you used in the line below.  
The first table has been filled in for you.

1) A `bar-chart` showing how many puppies (young dogs) are fixed or not.

What Rows?	Which Column(s)?	What will you Create?
<i>puppies</i>	<i>fixed</i>	<i>bar-chart</i>

code: `bar-chart(filter(filter(animals-table, is-dog), is-young), "fixed")`

2) A `pie-chart` showing how many heavy dogs are fixed or not.

What Rows?	Which Column(s)?	What will you Create?

code: \_\_\_\_\_

3) A `dot-plot` of the number of `weeks` it takes for a random sample of animals to be adopted.

What Rows?	Which Column(s)?	What will you Create?

code: \_\_\_\_\_

4) A `box-plot` of the number of `pounds` that kittens (young cats) weigh.

What Rows?	Which Column(s)?	What will you Create?

code: \_\_\_\_\_

5) A `scatter-plot` of a 35 random animals using `species` as the labels, `age` as the x-axis, and `weeks` as the y-axis.

What Rows?	Which Column(s)?	What will you Create?

code: \_\_\_\_\_




6) Describe **your own grouped sample** here, and fill in the table below.

What Rows?	Which Column(s)?	What will you Create?




code: \_\_\_\_\_

# Data Cycle: Analyzing Categorical Data

Use the [Animals Starter File](#) to analyze categorical data with the data cycle.

<b>Ask Questions</b> 	<p><i>How many of each species are fixed at the shelter?</i></p> <p>What question do you have?</p> <hr/> <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <hr/> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p> <hr/>	
<b>Analyze Data</b> 	<p>If you only need some rows, define your filter function here (Need help? Use the Design Recipe!)</p> <hr/> <p>If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!)</p> <hr/> <p>What code will make the table or display you want?</p> <hr/>	
<b>Interpret Data</b> 	<p>What did you find out? What can you infer?</p> <hr/> <hr/> <p>What - if any - new question(s) does this raise?</p> <hr/> <hr/> <hr/>	

---

<b>Ask Questions</b> 	<p><i>Are there more female cats than male cats at the shelter?</i></p> <p>What question do you have?</p> <hr/> <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <hr/> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p> <hr/>	
<b>Analyze Data</b> 	<p>If you only need some rows, define your filter function here (Need help? Use the Design Recipe!)</p> <hr/> <p>If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!)</p> <hr/> <p>What code will make the table or display you want?</p> <hr/>	
<b>Interpret Data</b> 	<p>What did you find out? What can you infer?</p> <hr/> <hr/> <p>What - if any - new question(s) does this raise?</p> <hr/> <hr/> <hr/>	

# Samples from My Dataset

Think back to when we defined grouped samples from the Animals Table, like "puppies", "old cats", etc. What grouped samples would be useful for *your* dataset? List a few of these in the first column.

Then, for each one, define a function that will identify if a row `r` is in the subset. *Hint: you can always use a blank design recipe page.*

Grouped Sample	A function that returns true if a row <code>r</code> is in the subset
	<pre> <b>fun</b> _____(r):     _____ <b>end</b> </pre>
	<pre> <b>fun</b> _____(r):     _____ <b>end</b> </pre>
	<pre> <b>fun</b> _____(r):     _____ <b>end</b> </pre>
	<pre> <b>fun</b> _____(r):     _____ <b>end</b> </pre>
	<pre> <b>fun</b> _____(r):     _____ <b>end</b> </pre>

# The Design Recipe

Write helper functions for **your** dataset, which you can use to define grouped samples. Since all helper functions will consume Rows, their Domains have already been filled in for you.

**Directions:** Define a function called \_\_\_\_\_, which consumes a Row of the \_\_\_\_\_ table and \_\_\_\_\_.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_  $(r :: \text{Row})$  -> *Boolean*  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

**Directions:** Define a function called \_\_\_\_\_, which consumes a Row of the \_\_\_\_\_ table and \_\_\_\_\_.

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_  $(r :: \text{Row})$  -> *Boolean*  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_ what the function does with those variable(s)

end

# Measures of Center in a Nutshell

There are three values used to report the **center** of a dataset.

- Each of these measures of center summarizes a whole column of quantitative data using just one number:
- **Mean** is the average of all the numbers in a dataset .
- **Median**: Half of the dataset will always be greater than or equal to the median. Half of the dataset will always be less than or equal to the median. In an ordered list, the median will either be the middle number or the average of the two middle numbers.
- **Mode(s)** of a dataset is the value (or values) occurring most often. When all of the values occur equally often, a dataset has no mode.

Which Measure of Center is most typical, depends on the shape of the data and the number of values.

- *When a dataset is symmetric* , values are just as likely to occur a certain distance above the mean as below the mean, and the median and mean are usually close together.
- *When a dataset is asymmetric* , the median is a more descriptive measure of center than the mean.
- **Left skew** datasets have a few values that are unusually low, which pull the mean *below* the median.
- **Right skew** datasets have a few values that are unusually high, which pull the mean *above* the median.
  - When a dataset contains a small number of values, the mode(s) may be the most descriptive measure of center. (Note that a small number of *values* is not the same as a small number of *data points* !)



# Mean, Median, Mode(s) Practice

## Mean

1) Find the mean of each dataset.

17, 23, 25, 23, 22	11, 3, 7, 4, 5	11, 3, 7, 4	5, 7, 11, 11, 7, 7	2, 3, 5, 4, 3, 7, 4

## Median

2) Find the median of each dataset.

17, 23, 25, 23, 22	5, 11, 3, 7, 4	11, 3, 7, 4	5, 7, 11, 11, 7, 7	2, 3, 5, 4, 3, 7, 4

## Mode(s)

3) Find the mode(s) of each dataset.

17, 23, 25, 23, 22	5, 11, 3, 7, 4	11, 3, 7, 4	5, 7, 11, 11, 7, 7	2, 3, 5, 4, 3, 7, 4

# Choosing the Best Measure of Center

Find the measures of center to summarize the `pounds` column of the [Animals Starter File](#), then respond to the prompts.

1) The three measures of center for this column are:

Mean (Average)	Median	Mode(s)
<code>mean(animals-table, "pounds")</code>	<code>median(animals-table, "pounds")</code>	<code>modes(animals-table, "pounds")</code>

2) If we scan the dataset, we can quickly see that **most** of the animals weigh less than the mean weight. Why is the average so high? \_\_\_\_\_

3) Referring to the pounds column of the Animals dataset, fill in the blanks:

- Outliers on the right pull the mean toward the right, causing the mean to be \_\_\_\_\_ the median.  
greater than / less than

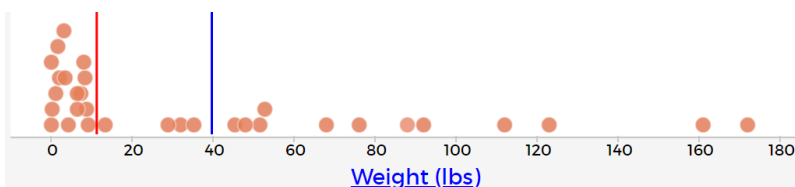
When the mean is greater than the median, the shape of the data is \_\_\_\_\_.  
skewed right / skewed left

- Outliers on the left pull the mean toward the left, causing the mean to be \_\_\_\_\_ the median.  
greater than / less than

When the mean is less than the median, the shape of the data is \_\_\_\_\_.  
skewed right / skewed left

4) In the dot plot below, identify which line is the median and which is the mean. Then label the lines.

Hint: You can refer to the table at the top of the page.



- Which has more data clustered quite close to it, the median or the mean? \_\_\_\_\_
- Which do you think better represents the data, the median or the mean? Why? \_\_\_\_\_

5) What did you learn from calculating the mode(s)? \_\_\_\_\_

6) In the Interactions area of the [Animals Starter File](#), type `modes(animals-table, "species")`. What does Pyret return? \_\_\_\_\_

7) Are there any measures of center that we can use for categorical data? \_\_\_\_\_

8) For which quantitative column(s) in the animals table do you think the modes might be a good measure of center? Why? \_\_\_\_\_

9) To take the average of a column, we add all the numbers in that column and divide by the number of rows. Will that work for every column? \_\_\_\_\_

# Critiquing Written Findings

Consider the following dataset, representing the heaviest bench press (in lbs) for ten powerlifters:

135, 95, 230, 135, 203, 55, 1075, 135, 110, 185

1) In the space below, rewrite this dataset in sorted order.

2) In the table below, compute the measures of center for this dataset.




Mean (Average)	Median	Mode(s)

3) The following statements are correct ... but misleading. Write down the reason why.





Statement	Why it's misleading
"More personal records are set at 135 lbs than any other weight!"	
"The average powerlifter can bench press about 236 lbs."	
"With a median of 135, that means that half the people in this group can't even lift 135 lbs."	

# Data Cycle: Measures of Center (Animals)

Open the [Animals Starter File](#). Complete both of the Data Cycles shown here, which have questions defined to get you started.





<b>Ask Questions</b> 	<p><i>What is the mean age for animals at the shelter?</i></p> <p>What question do you have?</p>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p>	
<b>Analyze Data</b> 	<p>If you only need some rows, define your filter function here (Need help? Use the Design Recipe!)</p> <p>If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!)</p> <p>What code will make the table or display you want?</p>	
<b>Interpret Data</b> 	<p>What did you find out? What can you infer?</p> <p>What - if any - new question(s) does this raise?</p>	

---





<b>Ask Questions</b> 	<p><i>What is the median time it takes for an animal to be adopted?</i></p> <p>What question do you have?</p>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p>	
<b>Analyze Data</b> 	<p>If you only need some rows, define your filter function here (Need help? Use the Design Recipe!)</p> <p>If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!)</p> <p>What code will make the table or display you want?</p>	
<b>Interpret Data</b> 	<p>What did you find out? What can you infer?</p> <p>What - if any - new question(s) does this raise?</p>	

# Data Cycle: Measures of Center (My Dataset)

Open [your chosen dataset](#). Complete both of the Data Cycles shown here.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

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<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

# Using Shape to Interpret Data

Read each scenario. Draw a **rough** histogram sketch (you do not need to label the axes), then decide if the histogram is skew left, skew right, or symmetric. Explain your interpretation.

1) In the United States, there are a few billionaires that have far greater incomes than the average (about \$28,000).

Rough histogram sketch:	Circle one: <i>skew left</i> <i>skew right</i> <i>symmetric</i>
	Explain your choice: _____
	_____
	_____
	_____

2) A school cafeteria mostly buys canned goods in huge sizes (48-64 ounces), but also purchases a few ingredients in smaller sizes.

Rough histogram sketch:	Circle one: <i>skew left</i> <i>skew right</i> <i>symmetric</i>
	Explain your choice: _____
	_____
	_____
	_____

3) It's just as likely for a newborn baby to be a certain number of ounces below the average weight (approximately 7.5 pounds) as it is to be that number of ounces above the average weight.

Rough histogram sketch:	Circle one: <i>skew left</i> <i>skew right</i> <i>symmetric</i>
	Explain your choice: _____
	_____
	_____
	_____

4) At many restaurants, the busiest dinner time is around 7pm, but there are always a few people who want to eat earlier or later.

Rough histogram sketch:	Circle one: <i>skew left</i> <i>skew right</i> <i>symmetric</i>
	Explain your choice: _____
	_____
	_____
	_____

# Reading Histograms

Students watched 5 videos, and rated them on a scale of 1 to 10. The average score for every video is the same (5.5).

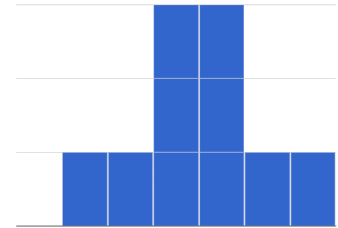
Match the summary description (left) with the *shape* of the histogram of student ratings (right).

- The x-axis shows the score, and the y-axis shows the number of students who gave it that score.
- These axes are intentionally unlabeled - the **shapes** of the ratings distributions were very different! And that's the focus here.

Most of the students were fine with the video, but a couple of them gave it an unusually low rating.

1

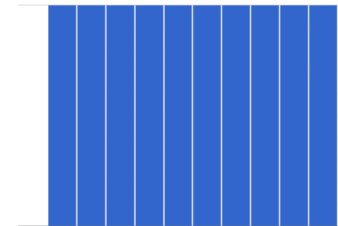
A



Most of the students were okay with the video, but a couple students gave it an unusually high rating.

2

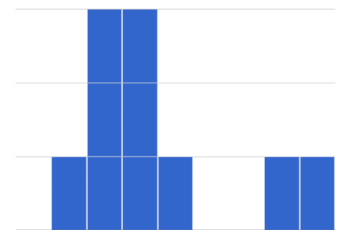
B



Students tended to give the video an average rating, and they weren't likely to stray far from the average.

3

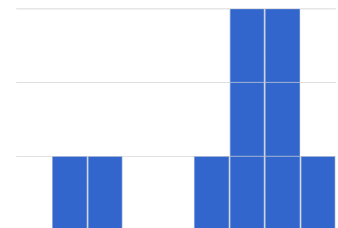
C



Students either really liked or really disliked the video.

4

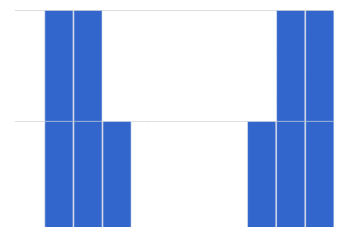
D



Reactions to the video were all over the place: high ratings and low ratings and inbetween ratings were all equally likely.

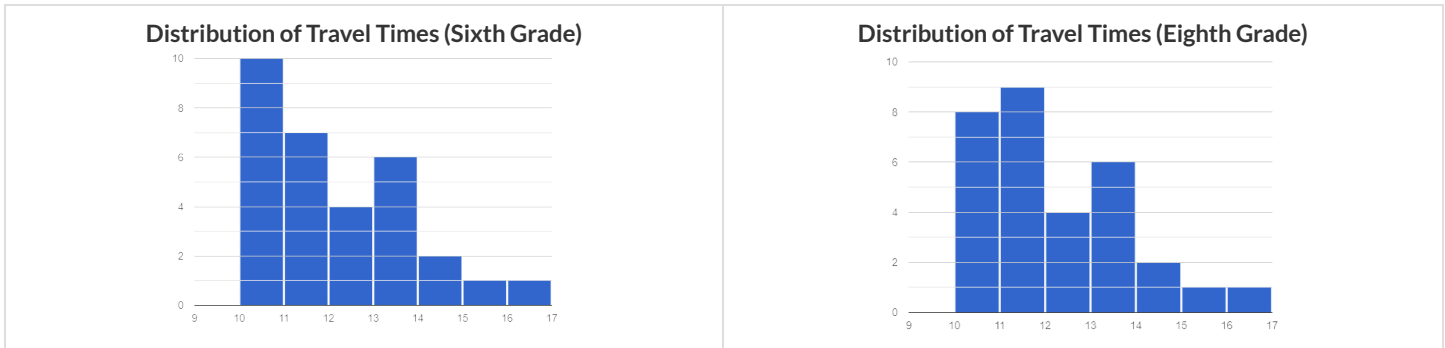
5

E



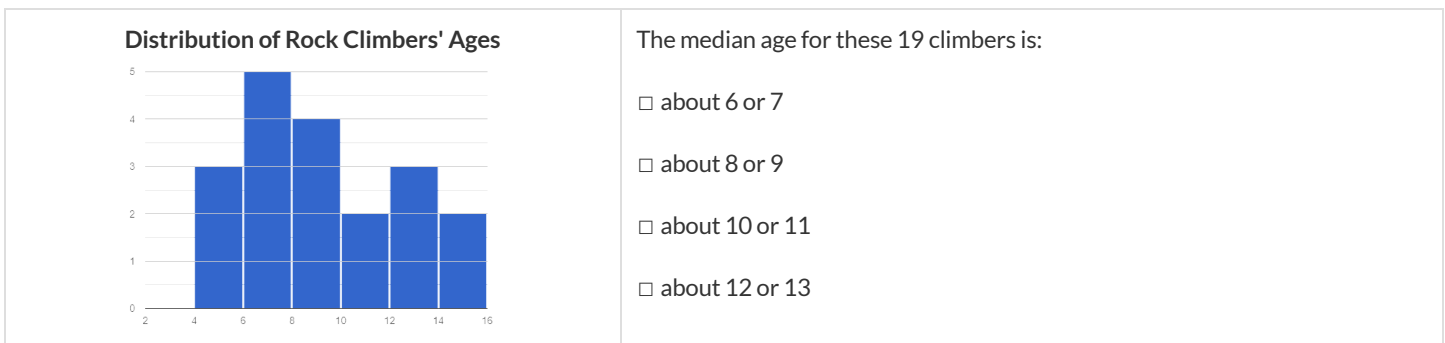
# Histograms and Measures of Center

1) The two histograms below show the number of minutes students spent traveling to school: one represents a sample of sixth grade students and the other represents a sample of eighth grade students. All travel times in the dataset are whole numbers.



2) Which group has the larger mode(s).    sixth graders    eighth graders    the modes are roughly the same

3) The histogram below shows the ages of the 19 children who signed up for rock climbing camp.

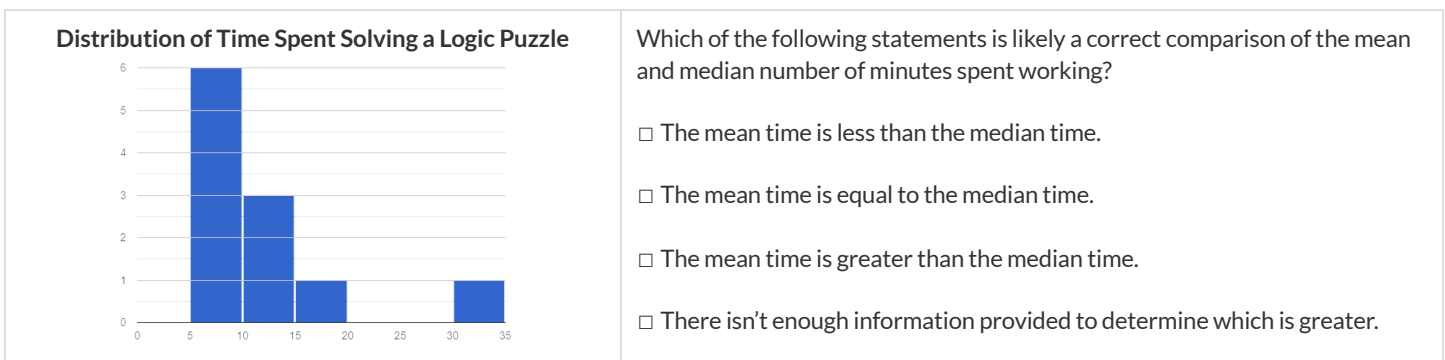


Explain how you determined the median value: \_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

4) Eleven students were asked to solve a logic puzzle. The minimum time was 5 minutes, and the maximum time was 35 minutes. The distribution of their times is shown on the histogram below.



Explain how you arrived at your choice: \_\_\_\_\_

\_\_\_\_\_

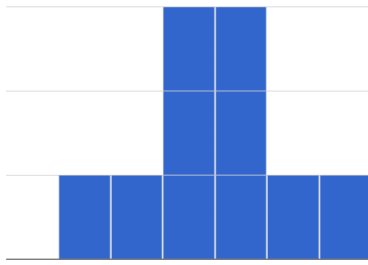
\_\_\_\_\_



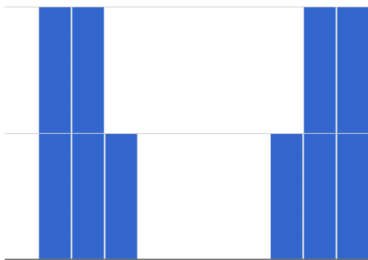
# Histograms and Variability

1) Students watched 2 videos, and rated them on a scale of 1 to 10. The average score for every video is the same (5.5).

Movie A



Movie B



Comparing the two graphs, we know that:

- ☐ The scores for Movie A have greater variability.
- ☐ The scores for Movie B have greater variability.
- ☐ The scores for Movie A and Movie B have equal variability.
- ☐ It is impossible to tell from the given information.

Explain how you arrived at your answer:

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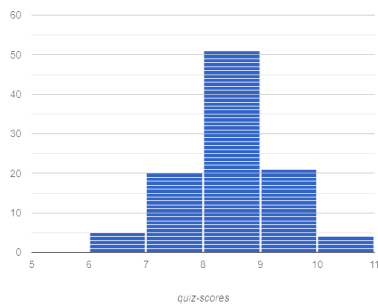
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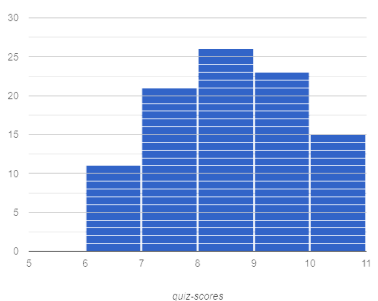
---

2) The following graphs show the distribution of quiz scores for two classes.

Class 1



Class 2



Comparing the two graphs, we know that:

- ☐ The quiz scores of Class 1 have greater variability.
- ☐ The quiz scores of Class 2 have greater variability.
- ☐ The quiz scores of Class 1 and Class 2 have equal variability.
- ☐ It is impossible to tell from the given information.

Explain how you arrived at your answer:

---

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---

---

3) Caro says, "Flatter histograms always show less variability." Is she correct? Explain why you agree or disagree with Caro.

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# Data Cycle: Quantitative Distributions (Animals) - Histograms

Describe two **histograms** made from columns of the animals dataset.

The first question is provided. You'll need to come up with the second question on your own!

<b>Ask Questions</b> 	<p>What is the distribution of weight among all animals at the shelter?</p> <p>What question do you have?</p>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p>	
<b>Analyze Data</b> 	<p>What code will make the table or display you want?</p>	
<b>Interpret Data</b> 	<p>The histogram I created is for _____ x-variable in context from _____ dataset or subset.</p> <p>The shape of this histogram is _____. There are peaks at _____ and gaps at _____.  <small>skewed left, skewed right, symmetric</small></p> <p>I notice that _____  <small>Consider statements like: Most of the histogram's area is... / A small amount of the histograms area trails out... / etc</small></p> <p>I wonder _____</p>	

---

<b>Ask Questions</b> 	<p>What question do you have?</p>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p>	
<b>Analyze Data</b> 	<p>What code will make the table or display you want?</p>	
<b>Interpret Data</b> 	<p>The histogram I created is for _____ x-variable in context from _____ dataset or subset.</p> <p>The shape of this histogram is _____. There are peaks at _____ and gaps at _____.  <small>skewed left, skewed right, symmetric</small></p> <p>I notice that _____  <small>Consider statements like: Most of the histogram's area is... / A small amount of the histograms area trails out... / etc</small></p> <p>I wonder _____</p>	

# Data Cycle: Quantitative Distributions (My Dataset) - Histograms

Open [your chosen dataset](#). Use the Data Cycle to explore the distribution of one or more quantitative columns using **histograms**, and write down your findings.

<b>Ask Questions</b> 	What question do you have? _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	
<b>Analyze Data</b> 	What code will make the table or display you want? _____	
<b>Interpret Data</b> 	What did you find out? What can you infer? _____ What - if any - new question(s) does this raise? _____ _____ _____	

<b>Ask Questions</b> 	What question do you have? _____	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____	
<b>Analyze Data</b> 	What code will make the table or display you want? _____	
<b>Interpret Data</b> 	What did you find out? What can you infer? _____ What - if any - new question(s) does this raise? _____ _____ _____	

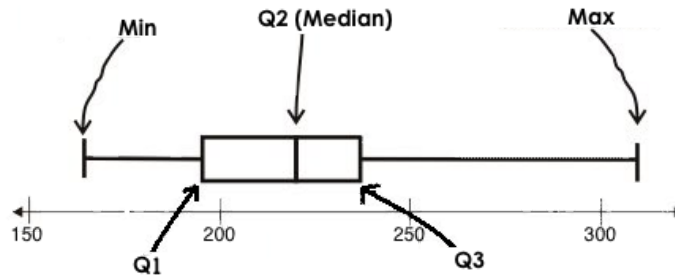
(optional)

# Measures of Spread in a Nutshell

Data Scientists measure the **spread** of a dataset using a **five-number summary** :

- **Minimum**: the smallest value in a dataset - it starts the first quarter
- **Q1 (lower quartile)**: the number that separates the first quarter of the data from the second quarter of the data
- **Q2 (Median)**: the middle value (median) in a dataset
- **Q3 (upper quartile)**: the value that separates the third quarter of the data from the last
- **Maximum**: the largest value in a dataset - it ends the fourth quarter of the data

The five-number summary can be used to draw a **box plot**.



- Each of the four sections of the box plot contains 25% of the data.
  - If the values are distributed evenly across the range, the four sections of the box plot will be equal in width.
  - Uneven distributions will show up as differently-sized sections of a box plot.
- The left **whisker** extends from the minimum to Q1.
- The **box**, or **interquartile range**, extends from Q1 to Q3. It is divided into 2 parts by the **median**. Each of those parts contains 25% of the data, so the whole box contains the central 50% of the data.
- The right **whisker** extends from Q3 to the maximum.

The box plot above, for example, tells us that:

- The minimum weight is about 165 pounds. The median weight is about 220 pounds. The maximum weight is about 310 pounds.
- The data is not evenly distributed across the range:
  - 1/4 of the players weigh roughly between 165 and 195 pounds
  - 1/4 of the players weigh roughly between 195 and 220 pounds
  - 1/4 of the players weigh roughly between 220 and 235 pounds
  - 1/4 of the players weigh roughly between 235 and 310 pounds
  - 50% of the players weigh roughly between 165 and 220 pounds
  - 50% of the players weigh roughly between 195 and 235 pounds
  - 50% of the players weigh roughly between 220 and 310 pounds
- The densest concentration of players' weights is between 220 and 235 pounds.
- Because the widest section of the box plot is between 235 and 310 pounds, we understand that the weights of the heaviest 25% fall across a wider span than the others.
  - 310 may be an outlier
  - the weights of the players weighing between 235 pounds 310 pounds could be evenly distributed across the range
  - or all of the players weighing over 235 pounds may weigh around 310 pounds.

# Distribution of a Dataset

## Family Gatherings by the Numbers

**Ledet Family Ages:** 1, 44, 3, 42, 46, 74, 75, 21, 74, 70, 40, 41, 45

**Average:** 44.3 years old

1) Order the Ages from Least to Greatest: \_\_\_\_\_

Then compute: Minimum   Q1   Median   Q3   Maximum   Range   Interquartile Range (IQR)

**Watson Family Ages:** 70, 68, 69, 72, 65, 75, 65, 78, 70, 72, 71, 70

**Average:** 70.4 years old

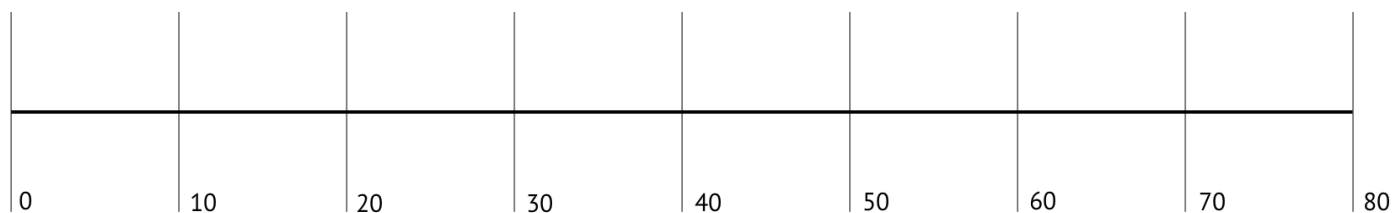
2) Order the Ages from Least to Greatest: \_\_\_\_\_

Then compute: Minimum   Q1   Median   Q3   Maximum   Range   Interquartile Range (IQR)

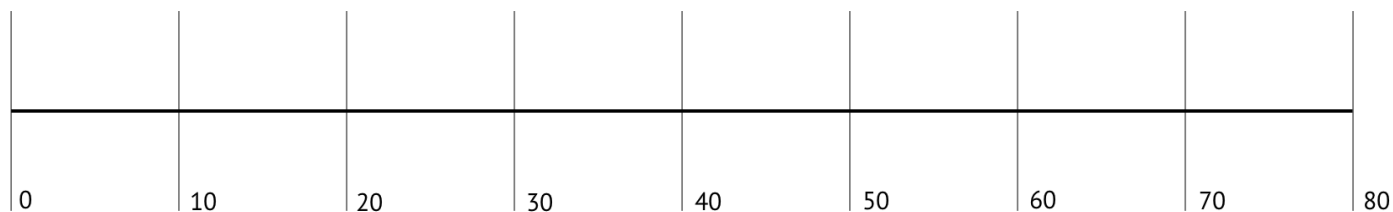
## Box Plots - Visualizing Shape

Make box plots for each family's age distribution on the number lines below. *Hint: Plot the 5-Number Summaries, draw a box around the IQR (from Q1 to Q3), let the median split the box into 2 parts, and add whiskers from the box to the minimum and maximum values.*

3) Ledet:



4) Watson:



## Compare and Contrast

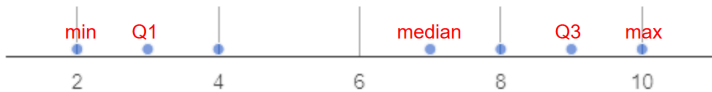
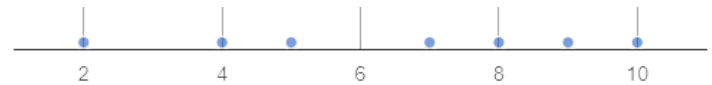
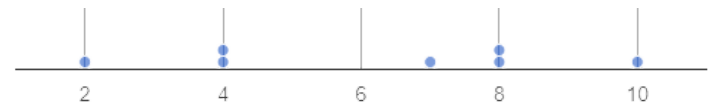
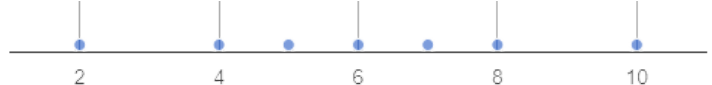
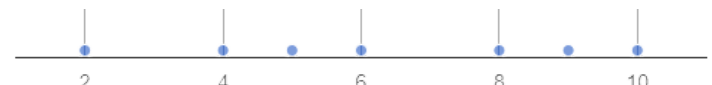
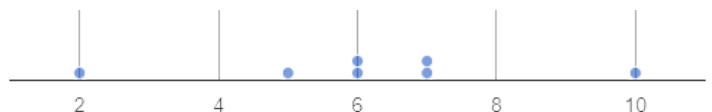
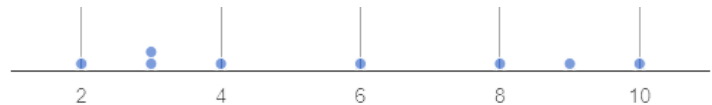
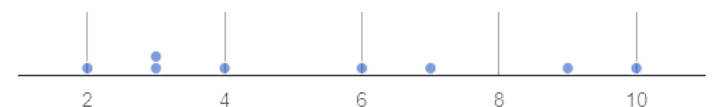
5) For which family gathering was the average age more typical? How do you know? \_\_\_\_\_

6) What else do you Notice and Wonder about the data from these two family gatherings?

7) We plotted both of these box plots on number lines with the same scale. What are the pros and cons of that choice?

# Matching Dot Plots and Five-Number Summaries

Draw a line from each dot plot on the left to the corresponding five-number summary on the right. You might find it useful to label the five-number summaries before you begin matching (see question 1 for an example).

Dot Plot		5-Number Summary
	1	<b>A</b> Min: 2 Q1: 4 Median: 7 Q3: 9 Max: 10
	2	<b>B</b> Min: 2 Q1: 4 Median: 6 Q3: 8 Max: 10
	3	<b>C</b> Min: 2 Q1: 3 Median: 7 Q3: 9 Max: 10
	4	<b>D</b> Min: 2 Q1: 4 Median: 6 Q3: 9 Max: 10
	5	<b>E</b> Min: 2 Q1: 5 Median: 6 Q3: 7 Max: 10
	6	<b>F</b> Min: 2 Q1: 4 Median: 7 Q3: 8 Max: 10
	7	<b>G</b> Min: 2 Q1: 3 Median: 5 Q3: 8.5 Max: 10
	8	<b>H</b> Min: 2 Q1: 3 Median: 5 Q3: 8 Max: 10

# Create Box Plots from Dot Plots

Use the five-number summary to draw a box plot above the corresponding dot plot. When you're finished, identify which quarter(s) of the data are packed the densest, and which quarter(s) of the data are the most dispersed. The first row has been completed as a sample.

	Five-Number Summary	Dot Plot	Densest Packed Quarter(s)	Most Dispersed Quarter(s)
1	Min: 1 Q1: 3 Median: 6.5 Q3: 9 Max: 20		first	fourth
2	Min: 1 Q1: 12 Median: 16 Q3: 18 Max: 20			
3	Min: 1 Q1: 5 Median: 9.5 Q3: 14 Max: 18			
4	Min: 1 Q1: 8 Median: 10 Q3: 12 Max: 19			

# Matching Dot Plots and Box Plots

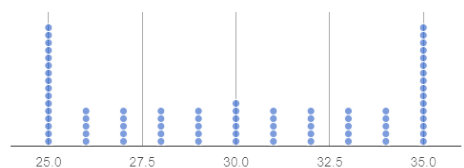
Draw a line from each dot plot on the left to the corresponding box plot on the right.

Dot Plot

Box Plot



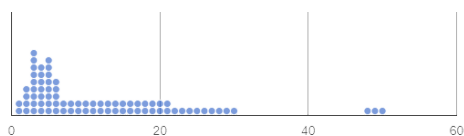
1



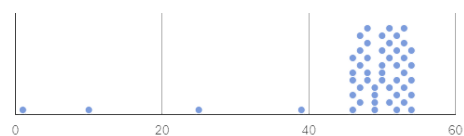
2



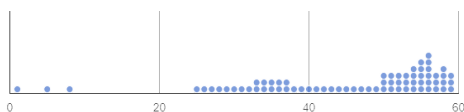
3



4

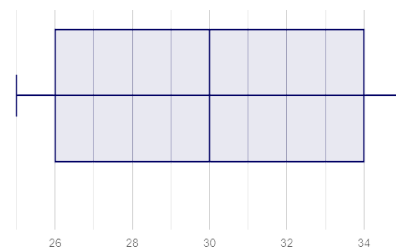


5

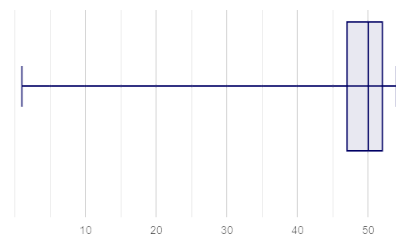


6

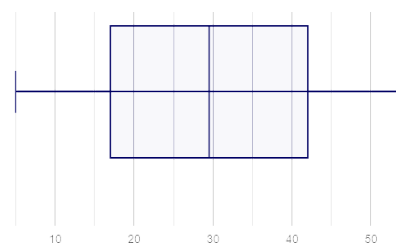
A



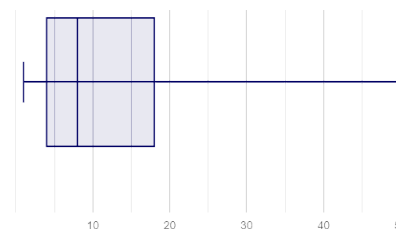
B



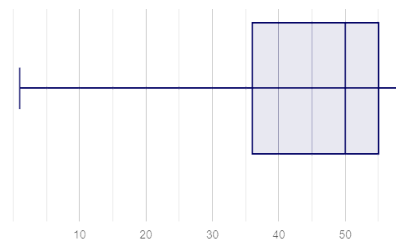
C



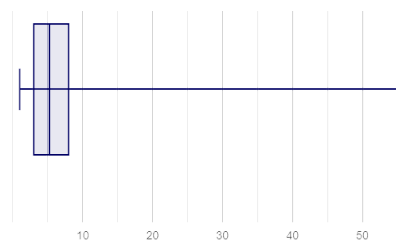
D



E



F





# Summarizing Columns with Measures of Spread

## Summarizing the Pounds Column

Get the values to summarize the spread of the \_\_\_\_\_ pounds \_\_\_\_\_ column of the [Animals Starter File](#) by typing

`box-plot(animals-table, "pounds")` into the Interactions Area.

1) My five-number summary is:

Minimum	Q1	Median	Q3	Maximum

2) Draw a box plot from this summary on the number line below. *Be sure to label the number line with consistent intervals.*



3) The **Range** is: \_\_\_\_\_ and the **Interquartile Range(IQR)** is: \_\_\_\_\_.

4) From this summary and box plot, I conclude that:

---

---

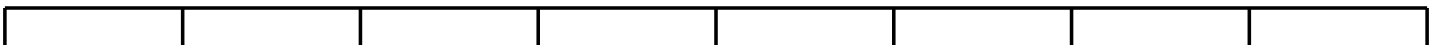
## Summarizing the \_\_\_\_\_ Column

Choose another column to investigate by making a `box-plot`

5) My five-number summary is:

Minimum	Q1	Median	Q3	Maximum

6) Draw a box plot from this summary on the number line below. *Be sure to label the number line with consistent intervals.*



7) The **Range** is: \_\_\_\_\_ and the **Interquartile Range(IQR)** is: \_\_\_\_\_.

8) From this summary and box plot, I conclude that:

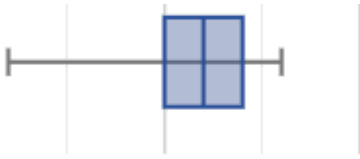
---

---

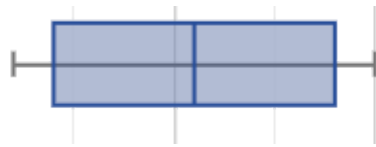
# Identifying Shape - Box Plots

Describe the shape of the box plots on the left. *Do your best to incorporate the vocabulary you've been introduced to.*

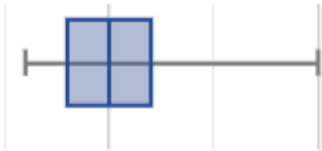
1



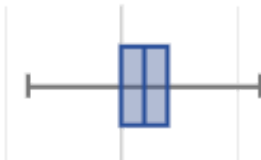
2



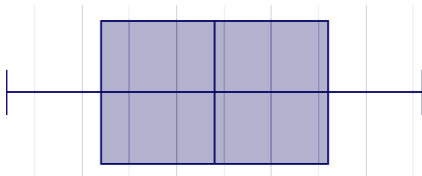
3



4



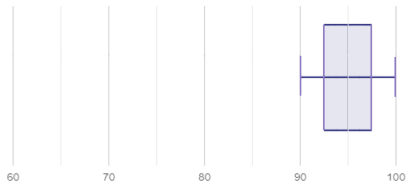
5



(optional)

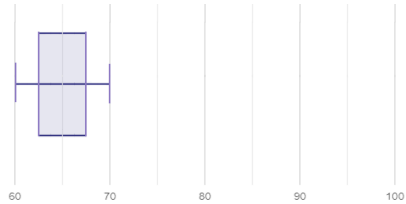
# Reading Box Plots

There are six different retirement homes in Retirement City. Each box plot (left) shows the spread of ages at one of the retirement homes. Match each box plot with the appropriate description (right) of residents' ages.



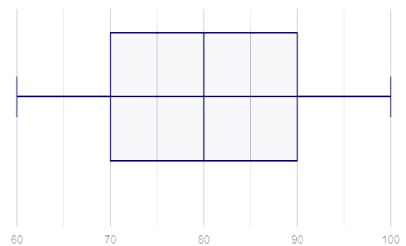
1

**A** At Apple Tree Independent Living, the majority of residents are at least 90 years old, but there are few younger residents as well.



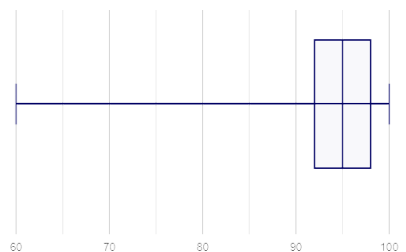
2

**B** The residents of Cherry Hill Retirement Home are all at least 90 years old.



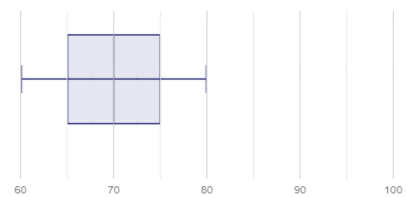
3

**C** The majority of seniors at the Edgewood Home are younger than 70, but there are some exceptions.



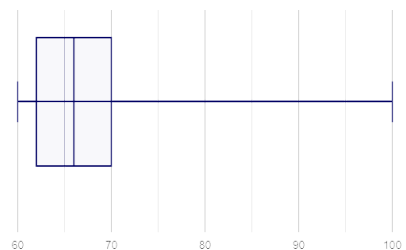
4

**D** The residents of Juneau Independent Living are mostly in their sixties.



5

**E** At Horizon Retirement Center, residents' ages are evenly distributed from 60 to 100.

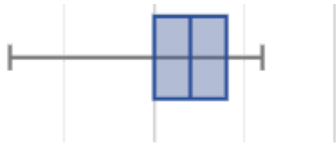


6

**F** The median age at Live Oak Assisted Living is 70.

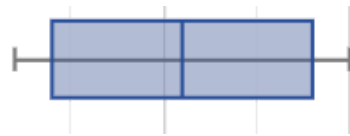
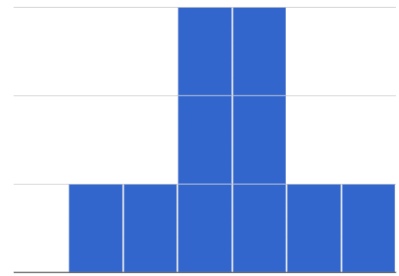
# Matching Box Plots to Histograms

Students watched 5 videos, and rated them on a scale of 1 to 10. For each video, their ratings were used to generate box plots and histograms. Match each box plot to the histogram that displays the same data.



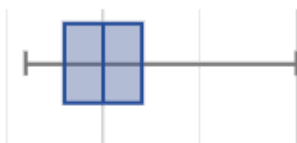
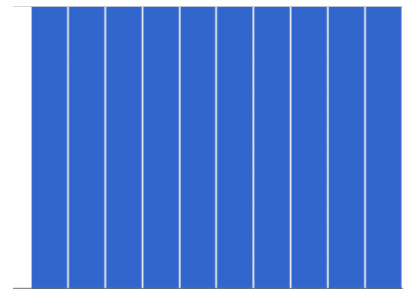
1

A



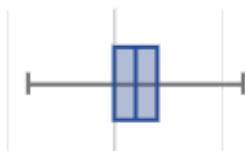
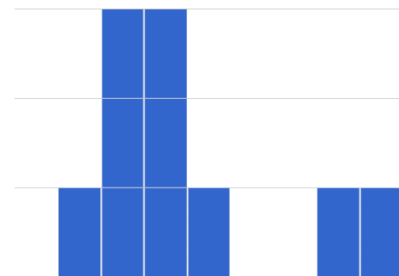
2

B



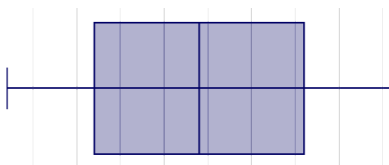
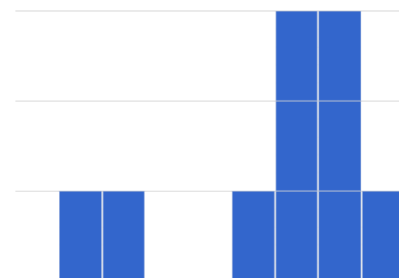
3

C



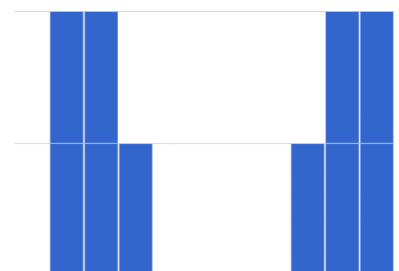
4

D



5

E



Directions: Connect each item on this page to at least one other item by drawing an arrow and writing an explanation of how they are connected along the arrow. (Arrows may curve.)

Minimum

Maximum

Quartile

Median

50%

Interquartile Range





Upper Quartile





Lower Quartile

25%

# Data Cycle: Quantitative Distributions - Box Plots (Animals)


Open the [Animals Starter File](#). Use the Data Cycle to explore the distribution of one or more quantitative columns using **box plots**.

<b>Ask Questions</b> 	What is the distribution of the weeks column from the animals dataset? What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	The box plot for _____ is _____. <div style="text-align: center;"> <span style="margin-right: 100px;">x-variable in context</span> <span>skewed left / skewed right / symmetric / etc.</span> </div> The 5-number summary is: min = _____ Q1 = _____ median = _____ Q3 = _____ max = _____ The middle 50% of the data lies between _____ and _____ so the Interquartile Range is _____ I notice that _____ <div style="text-align: center;"> <small>Consider statements like: 75% of the data fall below ... / The top 25% of the data fall between ... / etc</small> </div> <hr/> I wonder _____	


<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	The box plot for _____ is _____. <div style="text-align: center;"> <span style="margin-right: 100px;">x-variable in context</span> <span>skewed left / skewed right / symmetric / etc.</span> </div> The 5-number summary is: min = _____ Q1 = _____ median = _____ Q3 = _____ max = _____ The middle 50% of the data lies between _____ and _____ so the Interquartile Range is _____ I notice that _____ <div style="text-align: center;"> <small>Consider statements like: 75% of the data fall below ... / The top 25% of the data fall between ... / etc</small> </div> <hr/> I wonder _____	

# Data Cycle: Quantitative Distributions - Box Plots (My Dataset)

Open [your chosen dataset](#). Use the Data Cycle to explore the distribution of one or more quantitative columns using **box plots**, and write down your findings.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

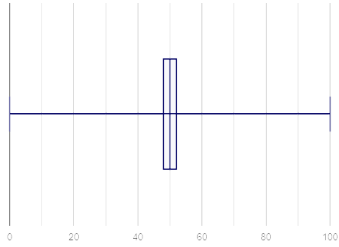
---

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

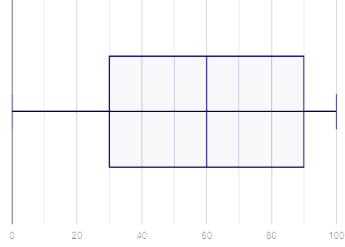
# Box Plots Card Sort

Cut out one set of cards for every pair of students. Instructions for this sorting activity can be found on [Sorting Box Plots](#).

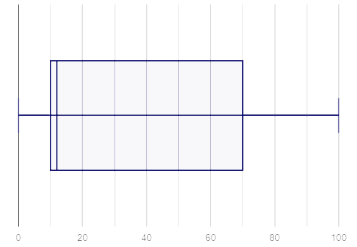
A



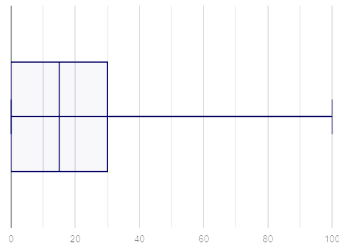
B



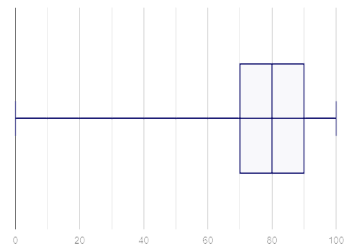
C



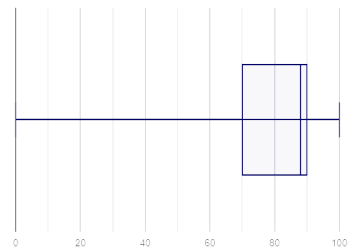
D



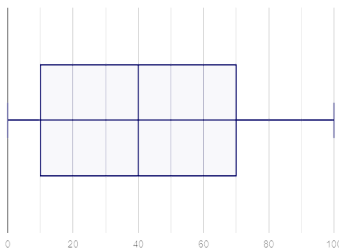
E



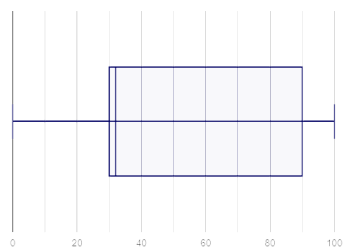
F



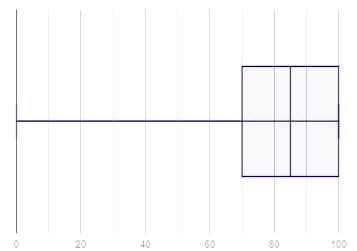
G



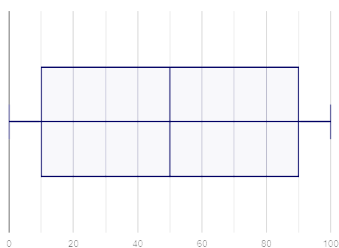
H



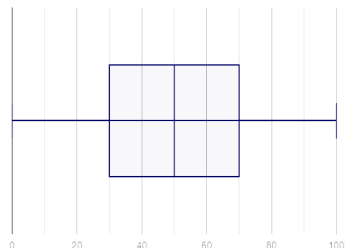
I



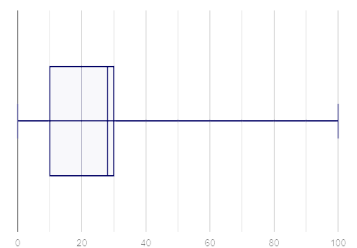
J



K



L





# Sorting Box Plots

## Notice & Wonder

1) What do you Notice about the box plots? \_\_\_\_\_  
\_\_\_\_\_

2) What do you Wonder about the box plots? \_\_\_\_\_  
\_\_\_\_\_

## Grouping Option #1

Identify two or three logical and related groupings that you could use to sort each of the box plot cards.

3) Group 1 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

4) Group 2 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

5) *Optional*: Group 3 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

6) Why are these groupings useful? What can you learn about a box plot based on the feature that you've chosen to focus on? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

## Grouping Option #2

Identify two or three logical and related groupings that you could use to sort each of the box plot cards.

7) Group 1 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

8) Group 2 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

9) *Optional*: Group 3 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

10) Why are these groupings useful? What can you learn about a box plot based on the feature that you've chosen to focus on? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

## Grouping Option #3

Identify two or three logical and related groupings that you could use to sort each of the box plot cards.

11) Group 1 Description: \_\_\_\_\_ Cards that belong: A, D, E, F, I, K, L

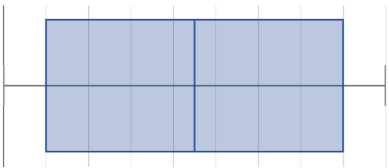
12) Group 2 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

13) *Optional*: Group 3 Description: \_\_\_\_\_ Cards that belong: \_\_\_\_\_

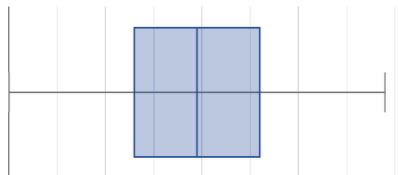
14) Why are these groupings useful? What can you learn about a box plot based on the feature that you've chosen to focus on? \_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

# Matching Box Plots to Histograms 2

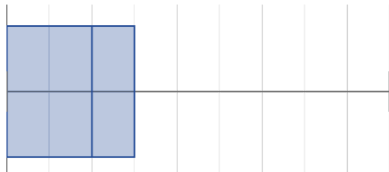
Match each box-plot to the histogram that displays the same data.



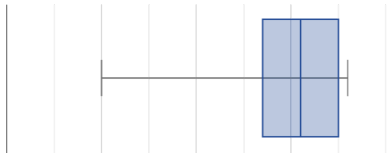
1



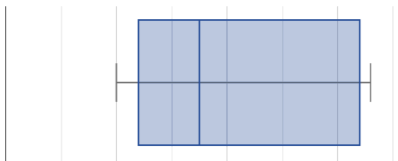
2



3

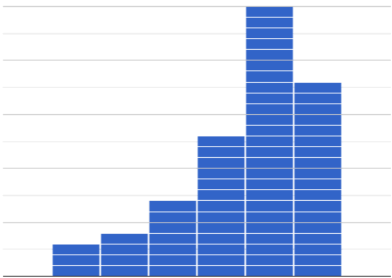


4

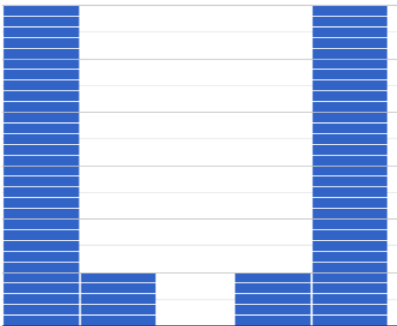


5

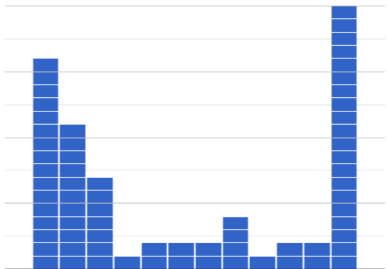
A



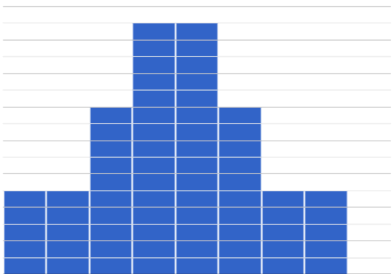
B



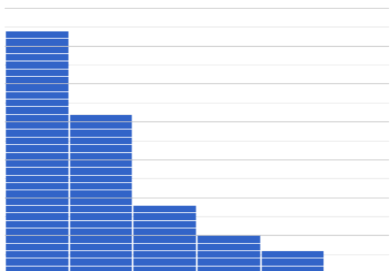
C



D



E

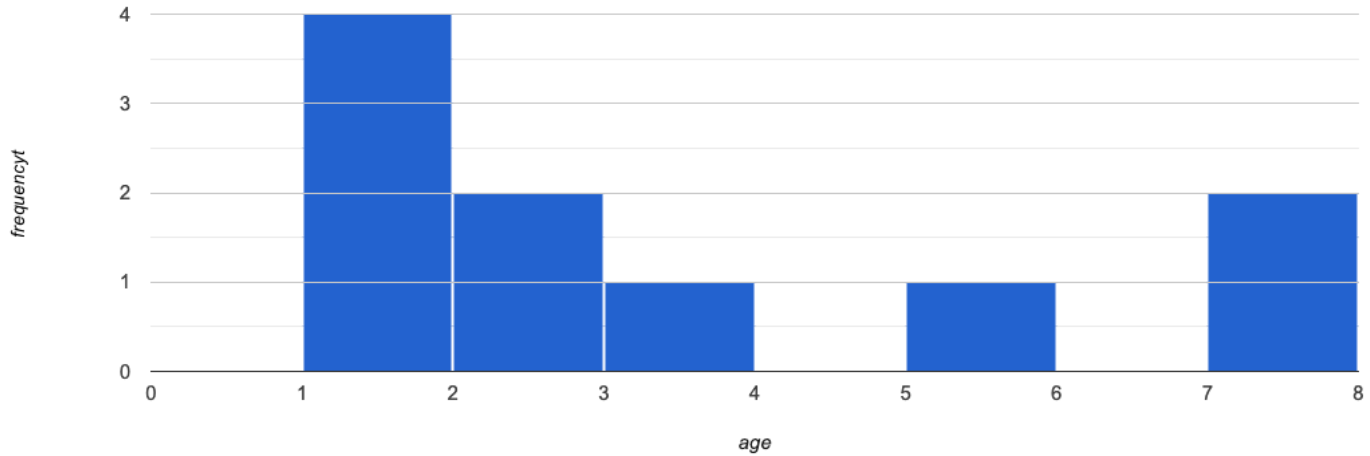


# Computing Standard Deviation

Here are the ages of different cats at the shelter: 1, 7, 1, 1, 2, 2, 3, 1, 5, 7

1) How many cats are represented in this sample? \_\_\_\_\_

The **distribution** of these ages is shown in the **histogram** below:



2) Describe the shape of this histogram. \_\_\_\_\_

3) What is the mean age of the cats in this dataset? \_\_\_\_\_

4) How many cats are 1 year old? 2 years old? Fill in the table below. The first column has been done for you.

age	1	2	3	4	5	6	7
frequency	4						

5) Draw a star to locate the mean on the x-axis of the histogram above.

6) For each cat in the histogram above, **draw a horizontal arrow** under the axis from your star to the cat's interval, and **label the arrow with its distance from the mean**. (For example, if the mean is 3 and a cat is in the 1yr interval, your arrow would stretch from 1 to 3, and be labeled with the distance "2")

To compute the standard deviation we square each distance and take the average, then take the square root of the average.

7) We've recorded the ages (N=10) shown in the histogram above in the table below, and listed the distance-from-mean for the four 1-year-old cats for you. As you can see, 1 year-olds are 2 years away from the mean, so their squared distance is 4. Complete the table.

age of cat	1	1	1	1	2	2	3	5	7	7
distance from mean	2	2	2	2						
squared distance	4	4	4	4						

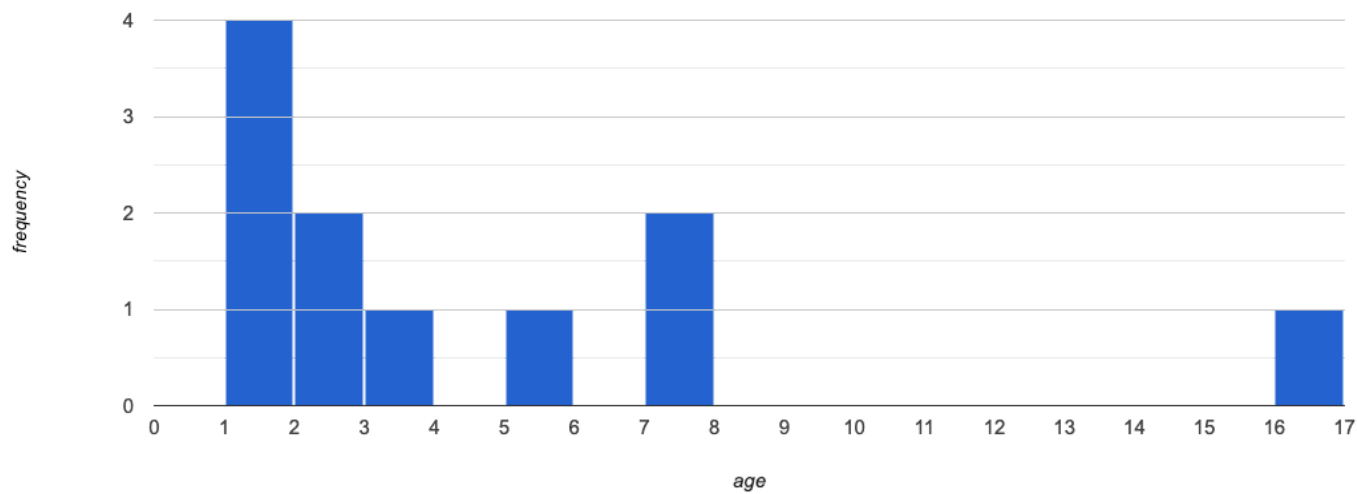
8) Add all the squared distances. What is their sum? \_\_\_\_\_

9) There are N=10 distances. What is N-1? \_\_\_\_\_ Divide the sum by N-1. What do you get? \_\_\_\_\_

10) Take the square root to find the **standard deviation**! \_\_\_\_\_

# The Effect of an Outlier

The histogram below shows the ages of eleven cats at the shelter:



1) Describe the shape of this histogram. \_\_\_\_\_

2) How many cats are 1 year old? 2 years old? Fill in the table below by reading the histogram. The first column has been done for you.

age	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
frequency	4															

3) What is the mean age of the cats in this histogram? \_\_\_\_\_

4) Draw a star to identify the mean on the histogram above.

5) For each cat in the histogram above, **draw a horizontal arrow** from the mean to the cat's interval, and **label the arrow with its distance from the mean**. (If the mean is 2 and a cat is 5 years old, your arrow would stretch from 2 to 5, and be labeled with the distance "3") To compute the standard deviation we square each distance and take the average, then take the square root of the average.

6) Recorded the 11 ages shown in the histogram in the first row of the table below. For each age, compute the distance from the mean and the squared distance.

age of cat																
distance from mean																
squared distance																

7) Add all the squared distances. What is their sum? \_\_\_\_\_

8) Divide the sum by  $N-1$  . What do you get? \_\_\_\_\_

9) Take the square root to find the **standard deviation**! \_\_\_\_\_

10) How did the outlier impact the standard deviation? \_\_\_\_\_

\_\_\_\_\_

# Data Cycle: Measure of Spread (Animals)

Open the [Animals Starter File](#). The mean time-to-adoption is 5.75 weeks. Does that mean most animals generally get adopted in 4-6 weeks? Use the Data Cycle to find out. Write your findings on the lines below, in response to the question.

<b>Ask Questions</b> 	<p><i>Do the animals all get adopted in around the same length of time?</i></p> <p>What question do you have?</p> <hr/> <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	<p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <hr/> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p> <hr/>	
<b>Analyze Data</b> 	<p>If you only need some rows, define your filter function here (Need help? Use the Design Recipe!)</p> <hr/> <p>If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!)</p> <hr/> <p>What code will make the table or display you want?</p> <hr/>	
<b>Interpret Data</b> 	<p>What did you find out? What can you infer?</p> <hr/> <hr/> <p>What - if any - new question(s) does this raise?</p> <hr/> <hr/> <hr/>	

Turn the Data Cycle above into a Data Story, which answers the question "If the average adoption time is 5.75 weeks, do all the animals get adopted in roughly 4-6 weeks?"

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# Data Cycle: Measure of Spread (My Dataset)

Open [your chosen dataset](#). Use the Data Cycle to find the standard deviation in two distributions, and write down your thinking and findings.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

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<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

# Computing Standard Deviation (2)

Here are ten different family incomes: \$43k, \$62k, \$39k, \$141k, \$58k, \$82k, \$41k, \$73k, \$68k, \$73k

1) Draw the **distribution** of these incomes by placing a dot on the number line below. If two families have the same income, put one dot on top of the other. Finally, draw a **box plot** on the number line, making sure to label the axis and show each quartile.



2) Describe the shape of this box-plot. \_\_\_\_\_

3) What is the mean income of the families in this dataset? \_\_\_\_\_

4) How many families earn \$39k? \$43k? Fill in the table below. The first column has been done for you.

income	\$39k	\$41k	\$43k	\$58k	\$62k	\$68k	\$73k	\$82k	\$141k
frequency	1								

5) Draw a star to locate the mean on the number line above.

6) For each family on the number line you drew,

- Draw a horizontal arrow under the axis from the star you drew in #5 to the dot for that family's income
- Label the arrow with its distance from the mean.

*e.g. if the mean is \$50k and a family's income is \$82k, your arrow would stretch from \$50k to \$82k, and be labeled with the distance "\$32k"*

To compute the standard deviation we square each distance and take the average, then take the square root of the average.

7) For each of the 10 incomes in the table below, list the distance-from-mean for each income, using the mean you computed above. Then fill in the squared distance in the next row to complete the table.

income (in 10s of thousands)	39	41	43	58	62	68	73	73	82	141
distance from mean										
squared distance										

8) Add all the squared distances. What is their sum? \_\_\_\_\_

9) There are  $N=10$  distances. What is  $N-1$ ? \_\_\_\_\_ Divide the sum by  $N-1$ . What do you get? \_\_\_\_\_

10) Take the square root to find the **standard deviation**! \_\_\_\_\_

# Matching Mean & Standard Deviation to Data

In the table below, match the mean and standard deviation to the list of data it describes.

Mean: 4 StDev: 0	1	A	-1, -2, -3, -4, -5, -6, -7
Mean: -5 StDev: ~5.66	2	B	1, 2, 3, 4, 5, 6, 7
Mean: 4 StDev: ~2.16	3	C	-1, -9
Mean: 4 StDev: ~2.65	4	D	0, 2, 3, 4, 5, 6, 8
Mean: -4 StDev: ~2.16	5	E	4, 4, 4, 4, 4



# Modeling Data

## A Quick Review...

When viewing a cloud of points on a scatter plot, sometimes we can see a pattern in the data.

- If the points cluster around a straight line, it might mean there's a **linear relationship** between the **explanatory variable** (x) and **response variable** (y).
- The line can slope up or down, indicating a *positive* relationship (where the two variables increase together) or *negative* relationship (where the response variable decreases as the explanatory variable increases).

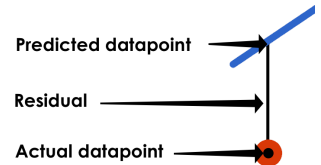
These lines are known as **models** for the data. The straight-line function describing a linear relationship is called a *linear model*.

- With a good model, the point cloud will hug the line tightly. A poor model will have lots of points that stray far from the line.
- Models *summarize* the data. For most datasets that means there will be data points that are not *exactly* on the line! And sometimes the line of best fit won't even pass through a single point in the dataset.
- We can use **linear regression** (`lr-plot` in Pyret) to compute the *best possible linear model* for a dataset, known as the **line of best fit**.

## S: Measuring Error in a Model

Differences between the predicted y-value and actual y-value for each x-value are called **residuals**. A residual tells us "how wrong" the model was at that particular point.

$$\text{Data} = \text{Model} + \text{Error}$$



We can summarize the error for *all* the points in a dataset using the **Standard Deviation of the Residuals** - known as **S** - to get a sense of how much to trust the predictions made by a model.

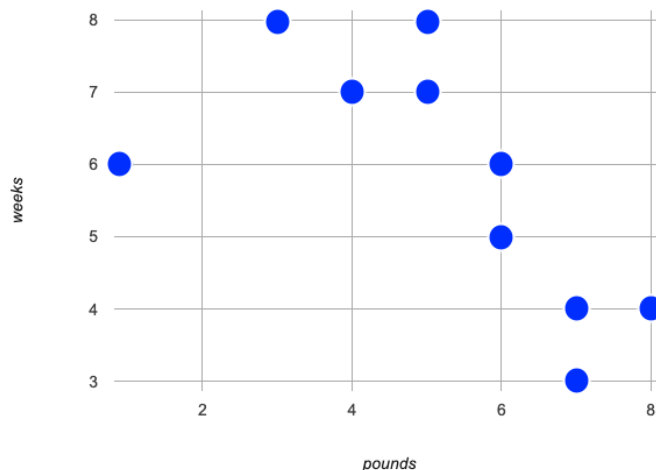
- **S** is expressed in terms of *units of the response variable* (y) and tells us how much error we expect in predictions made from the model. (e.g. up to \$8000, 5 years, 11 inches, etc. )
- The closer the data points are to the model, the smaller the residuals are, and the smaller **S** will be.
- If the **S-value** for a model is zero, *it fits the data perfectly!*
- When we compare two models for the same dataset, the one with the lower **S-value** fits better.
- We have no way of knowing whether or not **S-values** represent a small or large amount of error until we consider them in relation to the range of the dataset! (e.g. errors of \$20,000 are huge in the context of median salary, but small in the context of national budgets.)

# How could we Measure Whether a Model is a Good Fit? (Lizards)

## Summarize the Relationship You See

Below is a sample of lizards from the Animals Dataset.

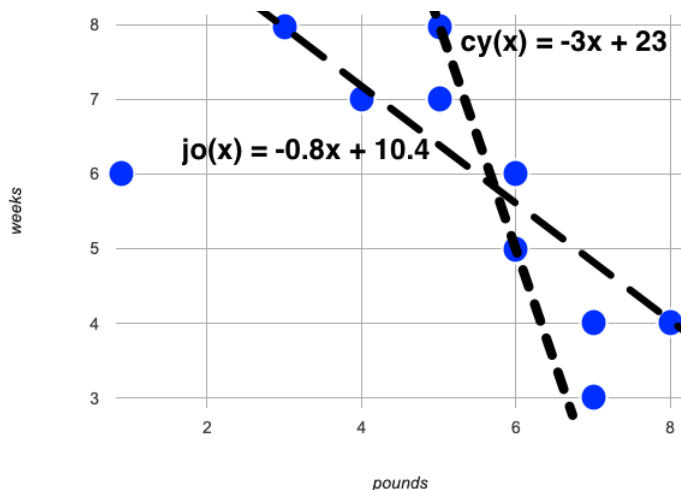
name	pounds	weeks
Amy	5	7
Aries	4	7
Boss	6	5
Brittany	3	8
Buck	7	4
Butterscotch	1	6
Chico	8	4
Coconut	6	6
Dodger	5	8
Dylan	7	3



- 1) Use a straightedge to draw the **line of best fit** that best summarizes the relationship you see in the data on the scatter plot.
- 2) Describe how you decided where to draw the line. \_\_\_\_\_

## Comparing Models

- 3) Cy and Jo drew the two lines below. Do you think  $cy(x)$  or  $jo(x)$  is a better model for this data? Why?



- 4) What could we measure, to calculate *how much better of a model* it is? \_\_\_\_\_
- 5) *Neither of these models is the best possible model!* What would have to be true of a third model, for us to know that it was a better fit than these two? \_\_\_\_\_

# Introducing fit-model

These data visualizations were generated using the [Lizard Sample Starter File](#). They can be viewed as interactive charts by uncommenting the final lines in the Definitions Area and clicking "Run".

```
fun cy(x): (-3 * x) + 23 end
```

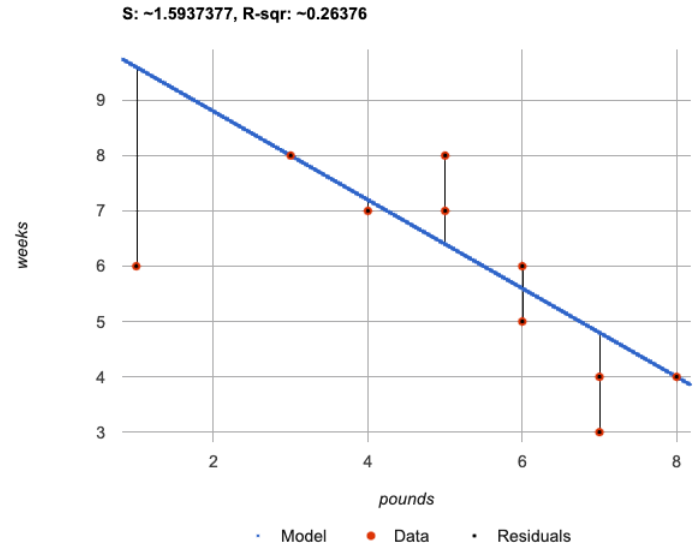
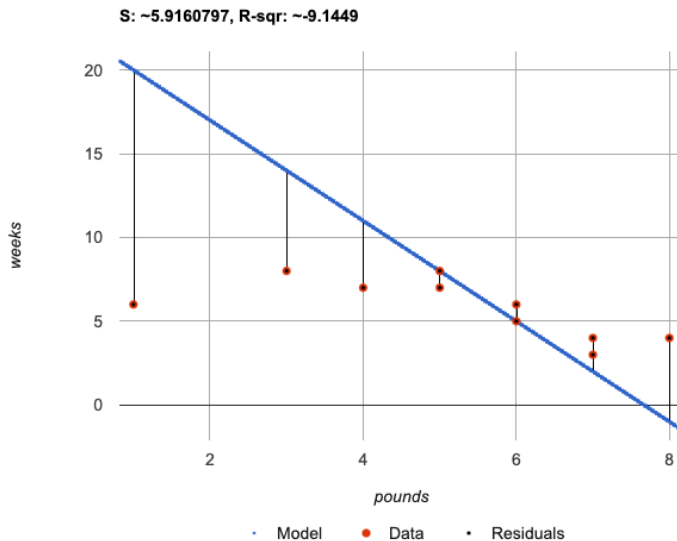
```
fit-model(
```

```
  lizard-sample, "name", "pounds", "weeks", cy)
```

```
fun jo(x): (-0.8 * x) + 10.4 end
```

```
fit-model(
```

```
  lizard-sample, "name", "pounds", "weeks", jo)
```



What do you Notice?

What do you Wonder?

1) How is the `fit-model` plot for cy's model **similar** to the `fit-model` plot for jo's model? \_\_\_\_\_

2) How is the `fit-model` plot for cy's model **different** from the `fit-model` plot for jo's model? \_\_\_\_\_

3) What do you think the three terms in the legend refer to?

- Model: \_\_\_\_\_
- Data: \_\_\_\_\_
- Residuals: \_\_\_\_\_

# Considering $S$ in Context

For each model below, decide whether you agree that the model is a good fit. Then rank the models from 1 (best fit) to 8 (worst fit).

How good is the model?	Ranking
<p>1) A data scientist is working with data from animals at a shelter.</p> <ul style="list-style-type: none"> <li>The range of days to adoption in this dataset are from 0 to 400.</li> <li>An <math>S</math> value of 300 means predicted adoption times could be off by 300 days.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>2) A student is exploring a dataset on climate change.</p> <ul style="list-style-type: none"> <li>The range of Arctic Sea Ice is from 3,920,000 to 7,670,000 square kilometers</li> <li>An <math>S</math> value of 300 means predicted Arctic Sea Ice coverage could be off by 300 square kilometers.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>3) A data scientist is working with data from US public schools.</p> <ul style="list-style-type: none"> <li>The range of graduates per school per year is 2 to 2003.</li> <li>An <math>S</math> value of 300 means predicted graduate values could be off by 300 students.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>4) A student is exploring a dataset on earthquakes.</p> <ul style="list-style-type: none"> <li>The range of earthquake depths in this dataset are from 4200m to 664000m.</li> <li>An <math>S</math> value of 300 means predicted earthquake depths could be off by 300 meters.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>5) A student is exploring a dataset on arrests in Los Angeles.</p> <ul style="list-style-type: none"> <li>The age range in this dataset is from 0 to 92.</li> <li>An <math>S</math> value of 1 means predicted ages could be off by 1 year.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>6) A data scientist is working with data about snowflakes.</p> <ul style="list-style-type: none"> <li>The range of snowflake weights is from 0.001 grams to 0.02 grams.</li> <li>An <math>S</math> value of 1 means predicted values could be off by 1 gram.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>7) A data scientist is working with data from animals at a shelter.</p> <ul style="list-style-type: none"> <li>The range of ages is from 0.5 years to 16 years.</li> <li>An <math>S</math> value of 1 means predicted ages could be off by 1 year.</li> </ul> <p>I _____ that this model is a good fit. strongly agree, agree, disagree, strongly disagree</p>	
<p>8) A student is working with a dataset of adult blue whales.</p> <ul style="list-style-type: none"> <li>The range of weights is 200,000 to 330,000 pounds.</li> <li>An <math>S</math> value of 1 means predicted weights could be off by 1 pound.</li> </ul> <p>I _____ that this model is a good fit strongly agree, agree, disagree, strongly disagree</p>	

# Interpreting our Models

**Cy's Model:**  $cy(x) = -3x + 23$

This model predicts that lizards weighing 0 pounds will be adopted in \_\_\_\_\_ and that,

for every additional \_\_\_\_\_, \_\_\_\_\_ will \_\_\_\_\_ by \_\_\_\_\_.

The error in the model is described by an **S-value** of about \_\_\_\_\_. I \_\_\_\_\_ that this model is a good fit considering that \_\_\_\_\_ in this dataset range from \_\_\_\_\_ to \_\_\_\_\_.

**Jo's Model:**  $jo(x) = -0.8x + 10.4$

This model predicts that lizards weighing 0 pounds will be adopted in \_\_\_\_\_ and that,

for every additional \_\_\_\_\_, \_\_\_\_\_ will \_\_\_\_\_ by \_\_\_\_\_.

The error in the model is described by an **S-value** of about \_\_\_\_\_. I \_\_\_\_\_ that this model is a good fit considering that \_\_\_\_\_ in this dataset range from \_\_\_\_\_ to \_\_\_\_\_.

## Comparing Models

- 1) Is Jo's model better or worse than Cy's model? \_\_\_\_\_
- 2) How much \_\_\_\_\_ error do we expect in predictions made with Jo's model than predictions made with Cy's model?

$$\text{Percent Change} = \frac{\text{Difference between the S-values}}{\text{S-value for Cy's model}} \times 100 = \underline{\hspace{2cm}}$$

We expect predictions made with Jo's model to have \_\_\_\_\_ percent \_\_\_\_\_ error than predictions made with Cy's model!

## My Model

If your teacher had you complete [From Lines to Functions](#), write the function you defined for your model on the line below and then complete the interpretation. If your class did not define models for the lines you drew, you can skip this section.

my-model( $x$ ) = \_\_\_\_\_

This model predicts that lizards weighing 0 pounds will be adopted in \_\_\_\_\_, and that,

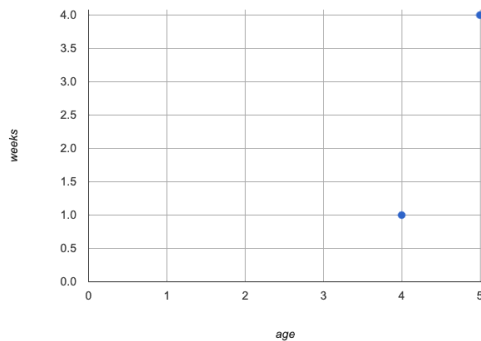
for every additional \_\_\_\_\_, \_\_\_\_\_ will \_\_\_\_\_ by \_\_\_\_\_.

The error in the model is described by an **S-value** of about \_\_\_\_\_. I \_\_\_\_\_ that this model is a good fit considering that \_\_\_\_\_ in this dataset range from \_\_\_\_\_ to \_\_\_\_\_.

# From Lines to Functions

## Defining a Function from Two Points

1) The scatter plot displays the relationship between clownfish age and adoption time in weeks. Identify the coordinates of the data points.



1st point: (       <sub>x<sub>1</sub></sub>,       <sub>y<sub>1</sub></sub> )

2nd point: (       <sub>x<sub>2</sub></sub>,       <sub>y<sub>2</sub></sub> )

2) We want to understand how change (  $\Delta$  ) in the age<sub>x-value</sub> of the clownfish relates to the change (  $\Delta$  ) in their adoption time in weeks<sub>y-value</sub>.

Compute the **slope** (rate of change) between the points:  $\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \underline{\hspace{2cm}}$

Based solely on data from these two clownfish, an increase in age of        <sub>$\Delta$  year(s)</sub> predicts an increase of        <sub>$\Delta$  weeks</sub> in adoption time.

3) Now, use **slope-intercept form** ( $y = mx + b$ ) to calculate the **y-intercept** (vertical shift) of the line passing through the two points.

Hint: Fill in the blanks for  $y$  and  $x$  below with the coordinates of the first point. Then use the slope we just calculate for  $m$ . Finally, solve for  $b$ .

$$\underline{\hspace{2cm}}_y = \underline{\hspace{2cm}}_{\text{slope (m)}} \times \underline{\hspace{2cm}}_x + \underline{\hspace{2cm}}_{\text{y-intercept / vertical shift}}$$

4) Use the slope and y-intercept you calculated to write the complete model below (in both Function and Pyret notation):

$$\text{clownfish}(x) = \underline{\hspace{2cm}}_{\text{slope (m)}} x + \underline{\hspace{2cm}}_{\text{y-intercept / vertical shift}} \quad \text{fun clownfish(x): ( } \underline{\hspace{2cm}} * x \text{ ) + } \underline{\hspace{2cm}} \text{ end}$$

## Define a Function for Your Lizard Line

5) Refer to the line you drew on [How could we Measure Whether a Model is a Good Fit? \(Lizards\)](#) to show the relationship you saw between the lizards' weight in pounds and adoption time in weeks. Identify two points that could be used to define the line (the points do not have to be dots from the scatter plot itself).

First point: (       <sub>x<sub>1</sub></sub>,       <sub>y<sub>1</sub></sub> )

Second point: (       <sub>x<sub>2</sub></sub>,       <sub>y<sub>2</sub></sub> )

6) Compute the **slope** (rate of change) between the points:  $\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \underline{\hspace{2cm}}$

Based solely on these 2 points, increasing a lizard's weight by 1 pound, predicts a(n)       <sub>increase or decrease?</sub> of        <sub>$\Delta$  weeks</sub> week(s) in adoption time.

7) Now, use **slope-intercept form** ( $y = mx + b$ ) to calculate the **y-intercept** (vertical shift) of the line passing through the two points.

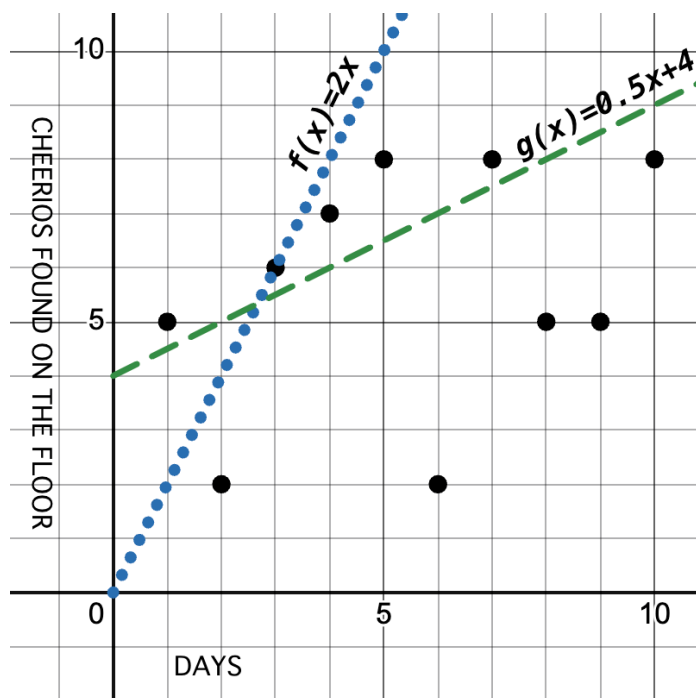
$$\underline{\hspace{2cm}}_y = \underline{\hspace{2cm}}_{\text{slope (m)}} \times \underline{\hspace{2cm}}_x + \underline{\hspace{2cm}}_{\text{y-intercept / vertical shift}}$$

8) Use the slope and y-intercept you calculated to write the complete model below (in both Function and Pyret notation):

$$\text{lizard}(x) = \underline{\hspace{2cm}}_{\text{slope (m)}} x + \underline{\hspace{2cm}}_{\text{y-intercept / vertical shift}} \quad \text{fun lizard(x): ( } \underline{\hspace{2cm}} * x \text{ ) + } \underline{\hspace{2cm}} \text{ end}$$

(optional)

# How could we Measure Whether a Model is a Good Fit? (Cheerios)



id	Days	Cheerios found on the floor
a	1	5
b	2	2
c	3	6
d	4	7
e	5	8
f	6	2
g	7	8
h	8	5
i	9	5
j	10	8

1) Do you think  $f(x)$  or  $g(x)$  is a better model for this data? \_\_\_\_\_

2) What makes you think that? \_\_\_\_\_

3) What could we measure, to calculate *how much better of a model* it is? \_\_\_\_\_

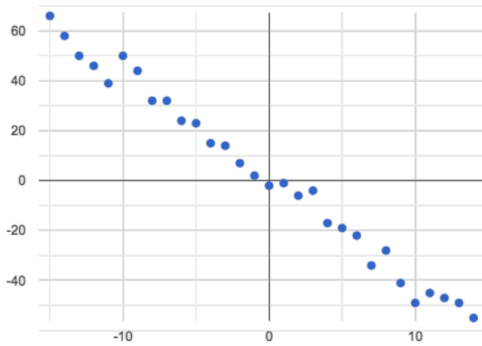
4) *Neither of these models is the best possible model!* What would have to be true of a third model, for us to know that it was a better fit than these two? \_\_\_\_\_

# Identifying Form, Direction and Strength

What do your eyes tell you about the Form, Direction, & Strength of these visualizations?

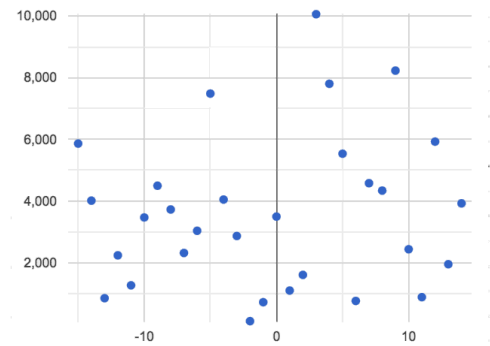
**Note:** If the form is nonlinear, we shouldn't report direction - a curve may rise and then fall.

A



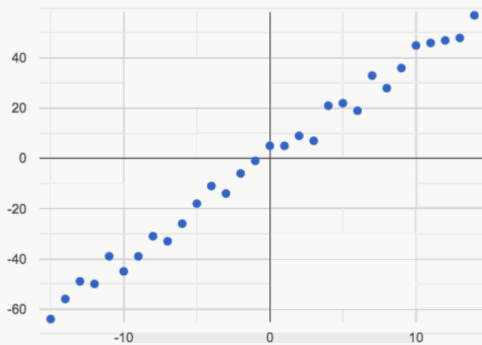
**Form:** Linear  
**Direction:** Negative  
**Strength:** Strong

B



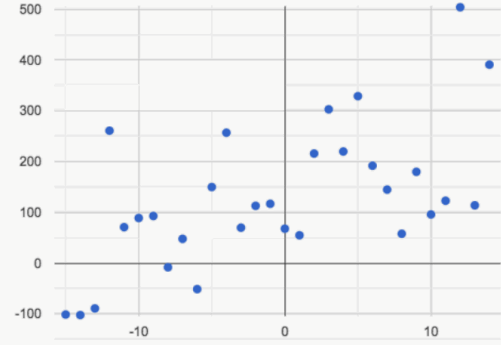
**Form:** Linear  
**Direction:** Positive  
**Strength:** Weak

C



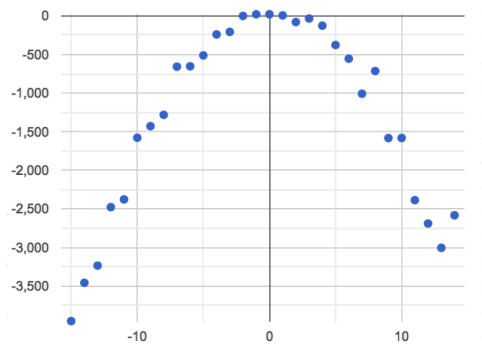
**Form:** Linear  
**Direction:** Positive  
**Strength:** Strong

D



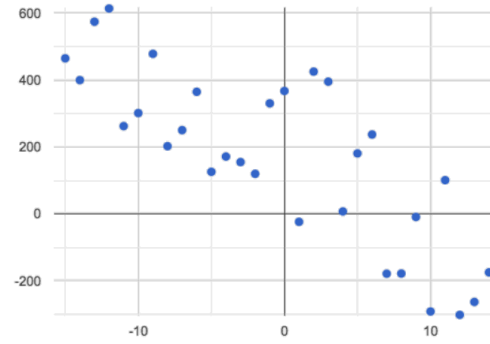
**Form:** Linear  
**Direction:** Positive  
**Strength:** Weak

E



**Form:** Linear  
**Direction:** Negative  
**Strength:** Strong

F



**Form:** Linear  
**Direction:** Positive  
**Strength:** Weak



# Reflection on Form, Direction and Strength

1) What has to be true about the *shape* of a relationship in order to start talking about the correlation's *direction* being positive or negative?

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2) What is the difference between a *weak* relationship and a *negative* relationship?

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3) What is the difference between a *strong* relationship and a *positive* relationship?

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4) If we find a strong relationship in a sample from a larger population, will that relationship *always hold* for the whole population? Why or why not?

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5) If two correlations are both positive, is the stronger one *more positive* (steeper slope) than the other?

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6) A news report claims that after surveying *10 million people*, a positive correlation was found between how much chocolate a person eats and how happy they are. Does this mean eating chocolate almost certainly makes you happier? Why or why not?

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# Summarizing Correlations with r-values

The **correlation** between two quantitative columns can be summarized in a single number, the  $r$ -value.

- The sign tells us whether the correlation is positive or negative.
- Distance from 0 tells us the strength of the correlation.
- Here is how we might interpret some specific  $r$ -values:
  - $-1$  is the strongest possible negative correlation.
  - $+1$  is the strongest possible positive correlation.
  - 0 means no correlation.
  - $\pm 0.65$  or  $\pm 0.70$  or more is typically considered a "strong correlation".
  - $\pm 0.35$  to  $\pm 0.65$  is typically considered "moderately correlated".
  - Anything less than about  $\pm 0.25$  or  $\pm 0.35$  may be considered weak.

*Note: These cutoffs are not an exact science!* In some contexts an  $r$ -value of  $\pm 0.50$  might be considered impressively strong! And sample size matters! We'd be more convinced of a positive relationship in general between cat age and time to adoption if a correlation of  $+0.57$  were based on 50 cats instead of 5.

**Correlation is not causation!** Correlation only suggests that two variables are related. It does not tell us if one causes the other. For example, hot days are correlated with people running their air conditioners, but air conditioners do not cause hot days!

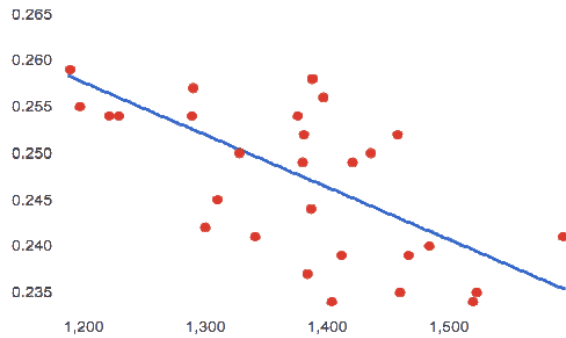
# Identifying Form and r-Values

What do your eyes tell you about the Form and Direction of the data? If the form is linear, approximate the  $r$ -value.

## Reminder:

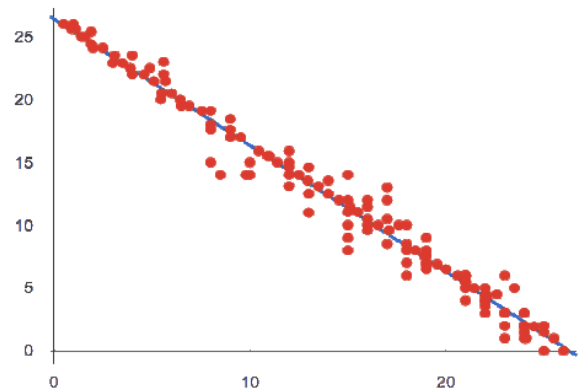
- $-1$  is the strongest possible *negative* correlation, and  $+1$  is the strongest possible *positive* correlation
- $0$  means no correlation
- $\pm 0.65$  or  $\pm 0.70$  or more is typically considered a "strong correlation"
- $\pm 0.35$  to  $\pm 0.65$  is typically considered "moderately correlated"
- Anything less than about  $\pm 0.25$  or  $\pm 0.35$  may be considered weak

A



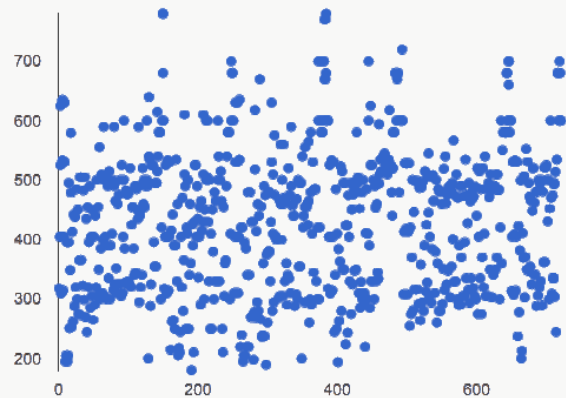
Form:  
r close to:

B



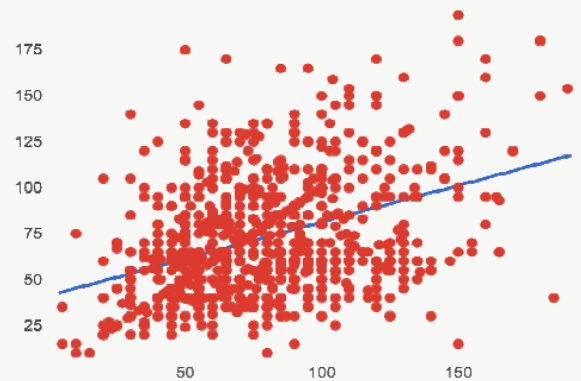
Form:  
r close to:

C



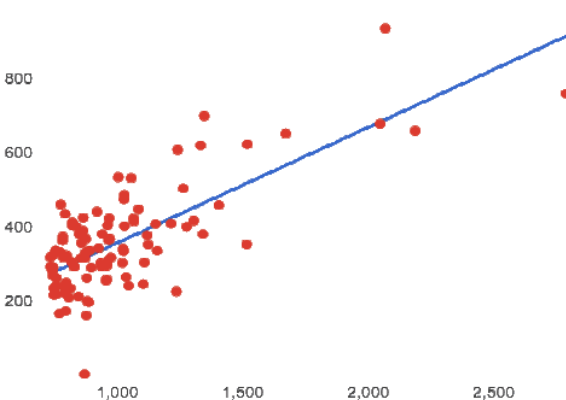
Form:  
r close to:

D



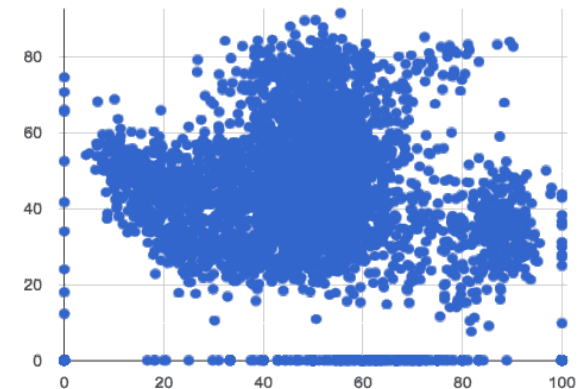
Form:  
r close to:

E



Form:  
r close to:

F



Form:  
r close to:

# Correlation Does Not Imply Causation!

Here are some possible correlations and the nonsense headlines a confused journalist might report as a result. In reality, the correlations have absolutely no causal relationship; they come about because both of them are related to another variable that's lurking in the background.

Can you think of another variable for each situation that might be the actual cause of the correlation and explain why the headlines the paper ran based on the correlations are nonsense?

1) **Correlation:** For a certain psychology test, the amount of time a student studied was negatively correlated with their score!

**Headline:** "Students who study less do better!"

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2) **Correlation:** Weekly data gathered at a popular beach throughout the year showed a positive correlation between sunburns and shark attacks.

**Headline:** "Sunburns Attract Shark Attacks!"

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3) **Correlation:** A negative correlation was found between rain and ski accidents.

**Headline:** "Be Safe - Ski in the Rain!"

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4) **Correlation:** Medical records show a positive correlation between Tylenol use and Death Rates.

**Headline:** "Tylenol use increases likelihood of dying!"

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5) **Correlation:** A positive correlation was found between hot cocoa sales and snow ball fights.

**Headline:** "Beware: Hot Cocoa Drinking encourages Snow Throwing!"

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# Correlations in the Animals Dataset

1) In the Interactions Area, create a scatter plot for the [Animals Starter File](#), using "pounds" as the xs and "weeks" as the ys.

- **Form:** Does the point cloud appear linear or nonlinear? \_\_\_\_\_
- **Direction:** If it's linear, does it appear to go up or down as you move from left to right? \_\_\_\_\_
- **Strength:** Is the point cloud tightly packed, or loosely dispersed? \_\_\_\_\_
- Would you predict that the  $r$ -value is positive or negative? \_\_\_\_\_
- Will it be closer to zero, closer to  $\pm 1$ , or in between? \_\_\_\_\_
- What  $r$ -value, does Pyret compute when you type `r-value(animals-table, "pounds", "weeks")`? \_\_\_\_\_
- Does this match your predictions? \_\_\_\_\_

---

---

2) In the Interactions Area, create a scatter plot for the Animals Dataset, using "age" as the xs and "weeks" as the ys.

- **Form:** Does the point cloud appear linear or nonlinear? \_\_\_\_\_
- **Direction:** If it's linear, does it appear to go up or down as you move from left to right? \_\_\_\_\_
- **Strength:** Is the point cloud tightly packed, or loosely dispersed? \_\_\_\_\_
- Would you predict that the  $r$ -value is positive or negative? \_\_\_\_\_
- Will it be closer to zero, closer to  $\pm 1$ , or in between? \_\_\_\_\_
- What  $r$ -value does Pyret compute? \_\_\_\_\_
- Does this match your prediction? \_\_\_\_\_

3) Is this correlation **stronger** or **weaker** than the correlation for "pounds"? \_\_\_\_\_

4) What does that *mean*? \_\_\_\_\_

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# Correlations in My Dataset

1) There may be a correlation between \_\_\_\_\_ and \_\_\_\_\_.

column

column

I think it is a \_\_\_\_\_, \_\_\_\_\_ correlation,

strong/weak

positive/negative

because \_\_\_\_\_

It might be stronger if I looked at \_\_\_\_\_

a sample or extension of my data

---

2) There may be a correlation between \_\_\_\_\_ and \_\_\_\_\_.

column

column

I think it is a \_\_\_\_\_, \_\_\_\_\_ correlation,

strong/weak

positive/negative

because \_\_\_\_\_

It might be stronger if I looked at \_\_\_\_\_

a sample or extension of my data

---

3) There may be a correlation between \_\_\_\_\_ and \_\_\_\_\_.

column

column

I think it is a \_\_\_\_\_, \_\_\_\_\_ correlation,

strong/weak

positive/negative

because \_\_\_\_\_

It might be stronger if I looked at \_\_\_\_\_

a sample or extension of my data

---

4) There may be a correlation between \_\_\_\_\_ and \_\_\_\_\_.

column

column

I think it is a \_\_\_\_\_, \_\_\_\_\_ correlation,

strong/weak

positive/negative

because \_\_\_\_\_

It might be stronger if I looked at \_\_\_\_\_

a sample or extension of my data

# Identifying Form, Direction and Strength (Matching)

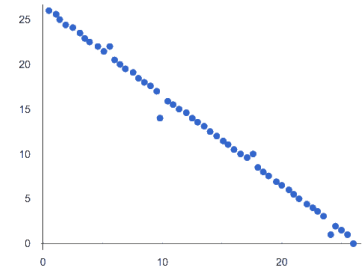
Match the description (left) with the scatter plot (right).

*Note: The computer won't tell us if the relationship we see in a scatter plot is linear, so it's important to train our eyes to decide this ourselves. For linear relationships, we should train our eyes to assess their direction and get a feel for their strength, so that we have a sense of whether the computed results make sense.*

The relationship appears to be linear,  
negative, and of moderate strength.

1

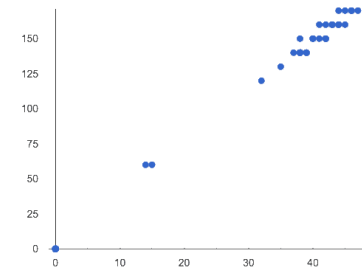
A



This relationship is nonlinear.

2

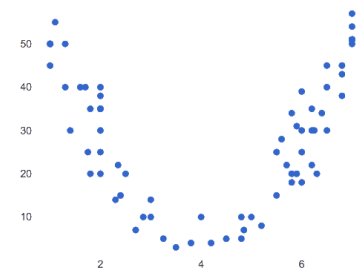
B



The x and y variables in this dataset do not  
appear to be related.

3

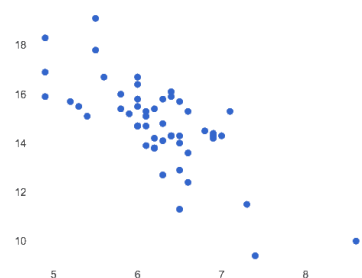
C



The relationship appears to be linear,  
positive, and strong.

4

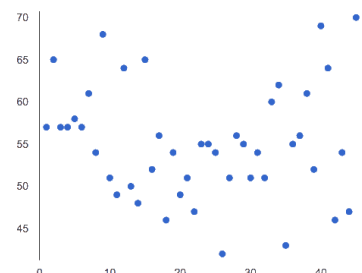
D



The relationship appears to be linear,  
negative, and strong.

5

E



(optional)

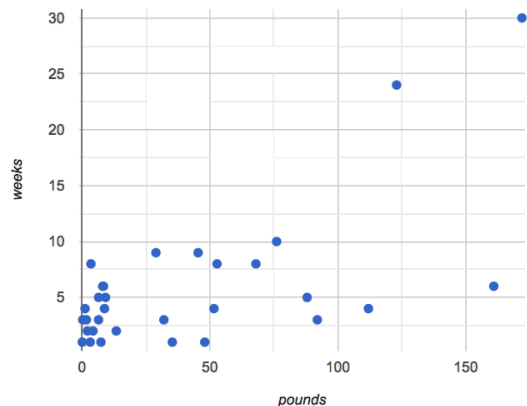
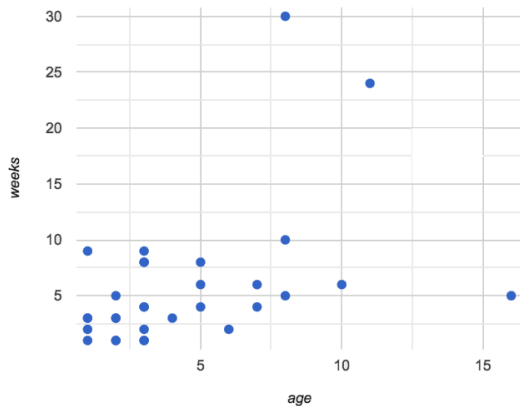
# Introduction to Linear Regression

## How much can one point move the line of best fit?

Open the [Interactive Regression Line \(Geogebra\)](#). Move the blue point "P", and see what effect it has on the red line.

- 1) Move P so that it is **centered amongst** the other points. Now move it all the way to top and bottom of the screen.
- 2) Move P so that it is **far to the left or right** of the other points. Now move it all the way to top and bottom of the screen. How - if at all - does the x-position of P impact on the line of best fit? \_\_\_\_\_  
\_\_\_\_\_
- 3) Could the **regression line** ever be above or below *all* the points (including the blue one you're dragging)? Why or why not? \_\_\_\_\_  
\_\_\_\_\_
- 4) Would it be possible to have a line with more points on one side than the other? Why or why not? \_\_\_\_\_  
\_\_\_\_\_
- 5) What is the highest  $r$ -value you can get? \_\_\_\_\_ Where did you place  $P$ ? (\_\_\_\_\_, \_\_\_\_\_)
- 6) What function describes the regression line with this value of  $P$ ?  $y = \text{_____} x + \text{_____}$
- 7) What is the lowest  $r$ -value you can get? \_\_\_\_\_ Where did you place  $P$ ? (\_\_\_\_\_, \_\_\_\_\_)
- 8) What function describes the regression line with this value of  $P$ ?  $y = \text{_____} x + \text{_____}$

## Predictions from Scatter Plots



- 9) Use a straight edge to draw what you think would be the line of best fit for **age vs. weeks** (on the left).  
Is this a strong correlation that will allow us to make a good prediction of an animal's adoption time just by knowing how old it is?  
\_\_\_\_\_
- 10) Use a straight edge to draw what you think would be the line of best fit for **pounds vs. weeks** (on the right).  
Is this a strong correlation that will allow us to make a good prediction of an animal's adoption time just by knowing how heavy it is?  
\_\_\_\_\_
- 11) Do either or both of the relationships appear to be linear?  
\_\_\_\_\_

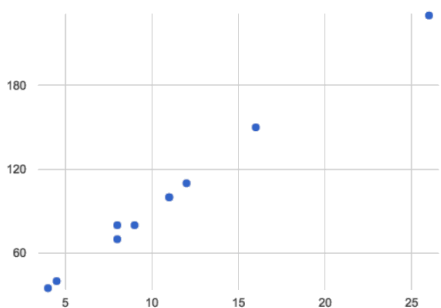
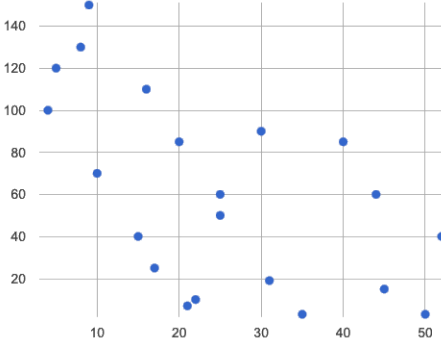
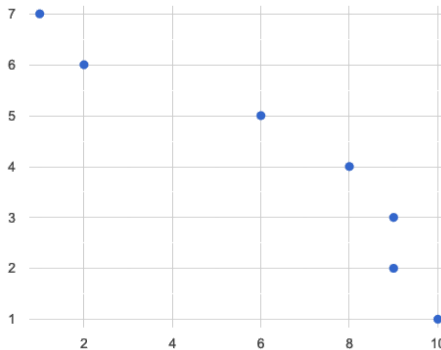
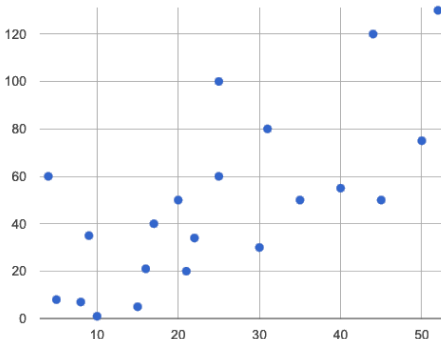


# Drawing Predictors

Remember what we learned about  $r$ -values...

$r = -1$	$r = -0.5$	$r = 0$	$r = 0.5$	$r = 1$
perfect negative correlation	moderate negative association	no correlation	moderate positive association	perfect positive correlation

For each of the scatter plots below, draw a **predictor line** that seems like the best fit. Describe the correlation in terms of Direction and whether you think it is **generally stronger** or **weaker**, then estimate the  $r$ -value as being close to -1, -0.5, 0, +0.5, or +1.

A		<p><b>Direction:</b>      Positive      Negative      None</p> <p><b>Strength:</b>      Stronger      Weaker</p> <p>I would guess that <math>r</math> is closest to...</p> <p style="text-align: center;">-1      -0.5      0      0.5      1</p>
B		<p><b>Direction:</b>      Positive      Negative      None</p> <p><b>Strength:</b>      Stronger      Weaker</p> <p>I would guess that <math>r</math> is closest to...</p> <p style="text-align: center;">-1      -0.5      0      0.5      1</p>
C		<p><b>Direction:</b>      Positive      Negative      None</p> <p><b>Strength:</b>      Stronger      Weaker</p> <p>I would guess that <math>r</math> is closest to...</p> <p style="text-align: center;">-1      -0.5      0      0.5      1</p>
D		<p><b>Direction:</b>      Positive      Negative      None</p> <p><b>Strength:</b>      Stronger      Weaker</p> <p>I would guess that <math>r</math> is closest to...</p> <p style="text-align: center;">-1      -0.5      0      0.5      1</p>

# Exploring lr-plot

## age

You should already have plotted `lr-plot(animals-table, "name", "age", "weeks")` in the [Animals Starter File](#).

- 1) What is the predictor function?  $y = \underline{\hspace{2cm}} x + \underline{\hspace{2cm}}$   $r = \underline{\hspace{2cm}}$
- 2) What is the slope?  $\underline{\hspace{2cm}}$
- 3) What is the y-intercept?  $\underline{\hspace{2cm}}$
- 4) How long would our line of best fit predict it would take for a 5 year-old animal to be adopted?  $\underline{\hspace{2cm}}$
- 5) What if they were a newborn, or just 0 years old?  $\underline{\hspace{2cm}}$
- 6) Does it make sense to find the adoption time for a newborn using this predictor function? Why or why not?  
 $\underline{\hspace{2cm}}$

## weight

Make another `lr-plot`, but this time use the animals' weight as our explanatory variable instead of their age.

- 7) How long would our line of best fit predict it would take for an animal weighing 21 pounds to be adopted?  $\underline{\hspace{2cm}}$
- 8) What if they weighed 0.1 pounds?  $\underline{\hspace{2cm}}$

## cats

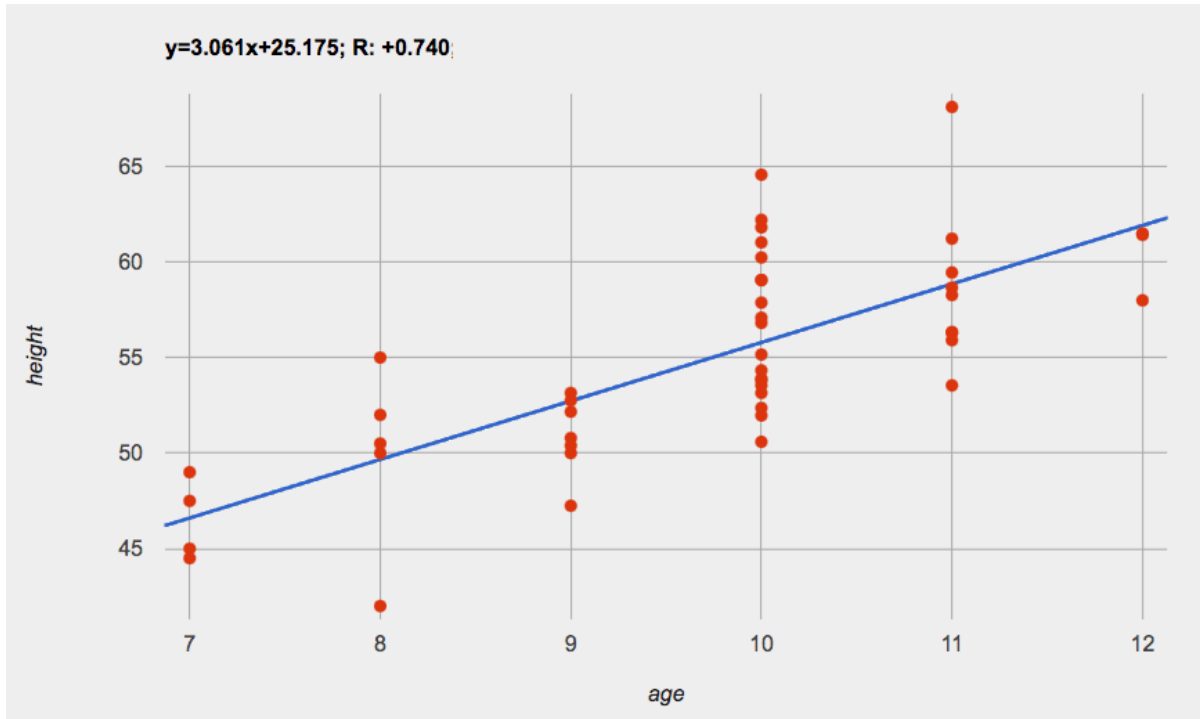
Make another `lr-plot`, comparing the `age` v. `weeks` columns for **only the cats** using the following code:

```
fun is-cat(r): r["species"] == "cat" end
lr-plot(filter(animals-table, is-cat), "name", "age", "weeks")
```

- 9) What is the predictor function?  $y = \underline{\hspace{2cm}} x + \underline{\hspace{2cm}}$   $r = \underline{\hspace{2cm}}$
- 10) What is the slope?  $\underline{\hspace{2cm}}$
- 11) What is the y-intercept?  $\underline{\hspace{2cm}}$
- 12) How does this line of best fit for *cats* compare to the line of best fit for *all animals*?  $\underline{\hspace{2cm}}$   
 $\underline{\hspace{2cm}}$   
 $\underline{\hspace{2cm}}$
- 13) How long would our line of best fit predict it would take for a 5 year-old cat to be adopted?  $\underline{\hspace{2cm}}$

★ Make another `lr-plot`, comparing the `age` v. `weeks` columns for *only the dogs*.

# Making Predictions



- 1) About how many inches are kids in this dataset expected to grow per year? \_\_\_\_\_
- 2) At that rate, if a child were 45" tall at age eight, how tall would you expect them to be at age twelve? \_\_\_\_\_
- 3) At that rate, if a ten-year-old were 55" tall, how tall would you expect them to have been at age 9? \_\_\_\_\_
- 4) Using the equation, how tall would you expect a seven-year-old child to be? \_\_\_\_\_
- 5) How many of the seven-year-olds in this sample are actually that height? \_\_\_\_\_
- 6) Using the equation, determine the expected height of someone who is...

7.5 years old	13 years old	6 years old	newborn	90 years old

- 7) For which ages is this predictor function likely to be the **most** accurate? Why? \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_
- 8) For which ages is this predictor function likely to be the **least** accurate? Why? \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_





# Interpreting Regression Lines & r-Values


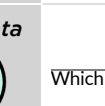

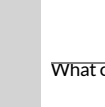
Use the predictor function and r-value from each linear regression finding on the left to fill in the blanks of the corresponding description on the right.

1	$\text{sugar}(m) = -3.19m + 12$ $r = -0.05$	<p>For every additional Marvel Universe movie released each year, the average person is predicted to consume _____ pounds of sugar! This correlation is _____.</p>
2	$\text{height}(s) = 1.65s + 52$ $r = 0.89$	<p>Shoe size and height are _____, _____ correlated. If person A is one size bigger than person B, we predict that they will be roughly _____ inches taller than person B as well.</p>
3	$\text{babies}(u) = 0.012u + 7.8$ $r = 0.01$	<p>There is _____ relationship found between the number of Uber drivers in a city and the number of babies born each year.</p>
4	$\text{score}(w) = -15.3w + 1150$ $r = -0.65$	<p>The correlation between weeks-of-school-missed and SAT score is _____ and _____. For every week a student misses, we predict a _____ point _____ in their SAT score.</p>
5	$\text{weight}(n) = 1.6n + 160$ $r = 0.12$	<p>There is a _____, _____ correlation between the number of streaming video services someone has, and how much they weigh. For each service, we expect them to be roughly _____ pounds heavier.</p>

## Data Cycle: Regression Analysis (Animals)

Open the [Animals Starter File](#). Before completing a data cycle on your own, read the provided example.

Question		Question Type
<b>Ask Questions</b> 	<p>How big of a factor is <i>age</i> in determining adoption time?</p> <p>What question do you have?</p>	<p>(circle one):</p> <p>Lookup Arithmetic <b>Statistical</b></p>
<b>Consider Data</b> 	<p><i>all animals at the shelter</i></p> <p>Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.)</p> <p><i>name, age, and weeks</i></p> <p>What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.)</p>	
<b>Analyze Data</b> 	<p><i>lr-plot(animals-table, "name", "age", "weeks")</i></p> <p>What code will make the table or display you want?</p>	
<b>Interpret Data</b> 	<p>I performed a linear regression on a sample of _____ animals at the shelter _____ and found a _____ correlation between _____ age _____ and _____ time to adoption _____. I would predict that a 1 _____ year _____ increase in _____ age _____ is associated with a _____ .789 week _____ increase _____ in _____ time to adoption _____.</p> <p><small>[dataset or subset]</small> <small>[x-axis]</small> <small>[y-axis]</small> <small>[x-axis units]</small> <small>[slope, y-units]</small> <small>[y-axis]</small></p>	

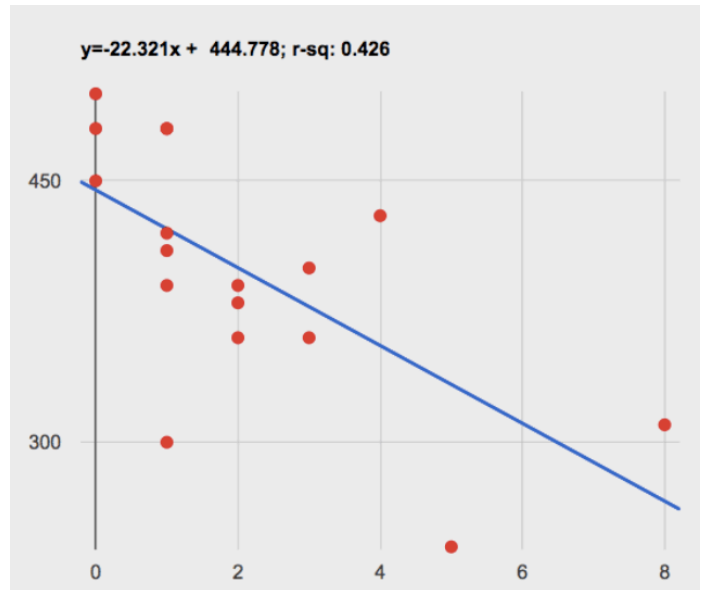
Ask Questions	Question Type (circle one): Lookup Arithmetic <b>Statistical</b>
	What question do you have? _____ _____
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) _____ What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) _____
<b>Analyze Data</b> 	What code will make the table or display you want? _____
<b>Interpret Data</b> 	I performed a linear regression on a sample of _____ and found a <div style="text-align: center;">[dataset or subset]</div> _____ correlation between _____ and <div style="text-align: center;">weak / strong / moderate (R=...), positive / negative</div> <div style="text-align: center;">[y-axis]</div> <div style="text-align: center;">[x-axis]</div> I would predict that a 1 _____ increase in _____ is <div style="text-align: center;">[y-axis]</div> <div style="text-align: center;">[x-axis units]</div> <div style="text-align: center;">[x-axis]</div> associated with a _____ in _____. <div style="text-align: center;">[slope, y-units]</div> <div style="text-align: center;">increase / decrease</div> <div style="text-align: center;">[y-axis]</div>

# Describing Relationships

A small sample of people were surveyed about their coffee drinking and sleeping habits. Does drinking coffee impact one's amount of sleep?

**NOTE: this data is made up for instructional purposes!**

Daily Cups of Coffee	Sleep (minutes)
3	400
0	480
8	310
1	300
1	390
2	360
1	410
0	500
2	390
1	480
3	360
4	430
0	450
5	240
1	420
2	380
1	480



1) Describe the relationship between coffee intake and minutes of sleep shown in the data above.

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2) Why is the y-axis of the display above misleading?

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# Data Cycle: Regression Analysis (My Dataset)

Open [your chosen dataset](#). Ask a question about your data to tell your Data Story.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	I performed a linear regression on a sample of _____ and found a <div style="text-align: center;">[dataset or subset]</div> _____ correlation between _____ and <div style="text-align: center;">[x-axis]</div> _____ . I would predict that a 1 _____ increase in _____ is <div style="text-align: center;">[y-axis]</div> <div style="text-align: center;">[x-axis units]</div> <div style="text-align: center;">[x-axis]</div> associated with a _____ in _____ . <div style="text-align: center;">[slope, y-units]</div> <div style="text-align: center;">increase / decrease</div> <div style="text-align: center;">[y-axis]</div>	

---

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic <b>Statistical</b>
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	I performed a linear regression on a sample of _____ and found a <div style="text-align: center;">[dataset or subset]</div> _____ correlation between _____ and <div style="text-align: center;">[x-axis]</div> _____ . I would predict that a 1 _____ increase in _____ is <div style="text-align: center;">[y-axis]</div> <div style="text-align: center;">[x-axis units]</div> <div style="text-align: center;">[x-axis]</div> associated with a _____ in _____ . <div style="text-align: center;">[slope, y-units]</div> <div style="text-align: center;">increase / decrease</div> <div style="text-align: center;">[y-axis]</div>	

# Age vs. Height Explore

Open the [Age vs. Height Starter File](#) and click "Run" to interact with data from another sample of students.

1) Take a look at the code in the Definitions Area. What do you notice? What do you wonder?

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---

2) Build `image-scatter-plot(h-table, "age", "height", dot)`. Try to visualize the line of best fit for just the blue dots. Then try to visualize the line of best fit for just the red stars. How do you think they would compare? Which line do you think would be steeper?

---

---

3) Make three linear regression plots comparing `age` and `height`, and record the results for each in the table below:

- The whole population: `lr-plot(h-table, "gender-id", "age", "height")`
- Females only: `lr-plot(filter(h-table, is-f), "gender-id", "age", "height")`
- Males only: `lr-plot(filter(h-table, is-m), "gender-id", "age", "height")`

Sample	Rate of change	y-intercept	R value
All			
Females			
Males			

4) What makes it difficult to compare these visualizations?

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---

Rebuild `lr-plot(filter(h-table, is-f), "gender-id", "age", "height")`, adjust the window of the interactive plot using the numbers in the table below, and click Redraw.

x-min:	x-max:	y-min:	y-max:
6.5	12.5	45	70

Then, do the same for `lr-plot(filter(h-table, is-m), "gender-id", "age", "height")`.

5) How do these visualizations compare now that their windows match?

---

---

6) What happens if you compare the students' height in inches to their height in centimeters by plotting `lr-plot(h-table, "gender-id", "height-cm", "height")`?

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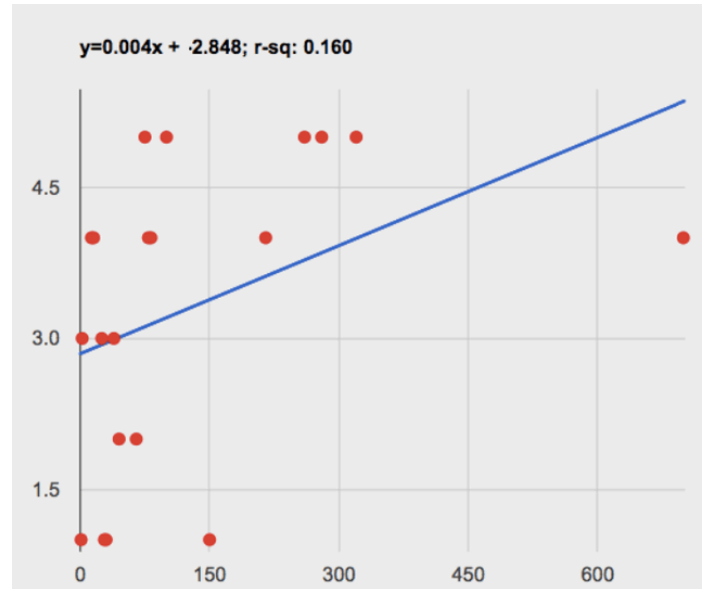


## Describing Relationships (2)

A small sample of people were surveyed about their satisfaction with their most recent purchase using a scale from 1 (very unsatisfied) to 5 (extremely satisfied).

**NOTE: this data is made up for instructional purposes!**

Dollars	Satisfaction
15.5	4
280	5
0.99	1
2.3	3
39	3
82	4
215	4
700	4
25	3
79	4
99.99	5
30	1
75	5
13	4
320	5
260	5
150	1
28	1
45	2
65	2



Describe the relationship between dollars spent and satisfaction shown in the data above.

---

---

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---





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# Data Cycle: Regression Analysis 2 (My Dataset)

Open [your chosen dataset](#). Ask a question about your data to tell your Data Story.

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

Write your Data Story below:

I performed a linear regression on a sample of \_\_\_\_\_ dataset or subset and found \_\_\_\_\_ correlation between \_\_\_\_\_ a weak/strong/moderate ( $R=...$ ), positive/negative \_\_\_\_\_ and \_\_\_\_\_ [x-axis] \_\_\_\_\_ [y-axis] . I would predict that a 1 \_\_\_\_\_ [x-axis units] increase in \_\_\_\_\_ [x-axis] is associated with a \_\_\_\_\_ [slope, y-units] \_\_\_\_\_ [increase/decrease] in \_\_\_\_\_ [y-axis] .

(optional)

# “Trust, but verify ...”

This page requires that you also open the [Trust but Verify Starter File](#).

A "helpful" Data Scientist gives you access to the following function:

```
# fixed-cats :: Table -> Table
# consumes a table of animals, and produces a table containing only cats that have been fixed, sorted
# from youngest-to-oldest
```

You can use the function, *but you can't see the code for it!* **How do you know if you can trust their code?**

- You could make a *verification subset* that contains one of every species, and make sure that the function filters out everything but cats.
- You could make sure this subset has multiple cats not already ordered youngest-to-oldest, and make sure the function puts them in the right order.

1) What other qualities would this subset need to have?

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2) Create your verification subset! In the space below, list the name of each animal in your subset.

Name

## “Trust, but verify...” (2)

@lesson-instructions{ This page requires that you also open the [Trust but Verify Starter File](#). }

A “helpful” Data Scientist gives you access to the following function:

```
# old-dogs-nametags :: Table -> Table
# consumes a table of animals, and produces a table containing only dogs 5 years or older, with an extra
# column showing their name in red
```

You can use the function, *but you can't see the code for it!* **How do you know if you can trust their code?**

1) What qualities would a verification subset need to have?

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2) Create your verification subset! In the space below, list the name of each animal in your subset.

Name

Katyanna Quach Wed 22 May 2019 // 23:50 UTC

**ANALYSIS** AI experts, lawyers, and law enforcement urged US Congress to regulate the use of facial recognition technology during a hearing held by the House Committee on Oversight and Reform on Wednesday, May 22, 2019.

The technical issues and social impacts of using AI software to analyse images or videos are well known. There have been repeated reports of how inaccuracies lead to people being misidentified in research and in real life. San Francisco just passed an ordinance banning the local government using facial recognition technology.

In some cases, like the experiment conducted by the American Civil Liberties Union's (ACLU), a nonprofit based in New York, that showed Amazon Rekognition incorrectly matched members of the US Congress to criminal mugshots, the effects have been minimal. It's simply absurd for elected politicians to be wanted criminals. But what happens when the technology is turned on civilians who have less power?

At a hearing of the House Committee on Oversight and Reform on Wednesday, Joy Buolamwini, founder of Algorithmic Justice League, an activist collective focused on highlighting the shortcomings of facial recognition, found that commercial computer models struggled most when it came to recognizing women with darker skin. IBM's system was incorrect for 34.7 per cent of the time when it came to identifying black women, she said...

The problem boiled down to biased training datasets, Buolamwini told the House committee. AI systems perform worse on data that they haven't seen before. So, if most datasets mainly represent white men then it's not surprising that they find it difficult when faced with an image of women of colour.

When it comes to databases of mugshots, however, the reverse is true. Black people are overrepresented in mugshot databases, explained Clare Garvie, Senior Associate at Georgetown University Law Center's Center on Privacy & Technology. If law enforcement are using these flawed models to target the group of people that it struggles to identify most then it will undoubtedly lead to police stopping and searching the wrong people. "It's a violation of the first and fourth amendment," Garvie said during the hearing.

### Law enforcement and lack of transparency

Cedric Alexander, the former president of the National Organization of Black Law Enforcement Executives who was also a witness at the hearing, estimated that at least a quarter of law enforcement agencies across the US use facial recognition to some degree.

Police from Washington County and Orlando are an example of some bureaus that are using Rekognition. Michael Punke, Amazon's VP of Global Public Policy, said at the time it has "not received a single report of misuse by law enforcement." It's difficult to verify that claim, however, considering that the police haven't been transparent about how it's used.

It's all done in secrecy, according to testimony. Elijah Cummings, the chair of the Oversight Committee, said that 18 states had shared data like passport photos or driver licenses with the FBI without explicit consent. When the witnesses were pressed with questions on what kind of information law agencies share with one another, nobody knew.

Neema Guliani, senior legislative counsel for the ACLU, took a tough stance and called for a moratorium on the technology. She urged the committee to "take steps to halt the use of face recognition for law enforcement and immigration enforcement purposes until Congress passes a law dictating what, if any, uses are permissible and ensures that individuals' rights can be protected." Unregulated use of the technology could also potentially lead to an "Orwellian surveillance state," where citizens are constantly tracked Guliani said. In the opening statement, Cummings said there are about 50 million surveillance cameras in the US, and that half of all American adults are probably part of facial recognition databases and they don't even know it.

Andrew Ferguson, professor of law at the University of the District of Columbia, agreed that the Congress needed to act now to prohibit facial recognition until Congress establishes clear rules. "Unregulated facial recognition should not be allowed to continue unregulated. It is too chilling, too powerful. The fourth amendment won't save us. The Supreme Court is trying to make amendments but it's not fast enough. Only legislation can react in real time to real time threats," he warned.

Alexander was more cautious about a blanket ban on the technology, however. He believed that there were still ways that law enforcement could positively use facial recognition. "There is a place for the technology, but the police need to be trained properly. They can't just be passed the technology by software companies." Effective policing is about building relationships in the local community, and it can't afford the effects of misidentifying people. How can we utilise the technology, whilst developing some standards?, he asked.

### Benchmark tests simply aren't good enough

The National Institute of Standards and Technology (NIST), a laboratory part of the US Department of Commerce, is currently conducting official benchmark tests for commercial facial recognition systems. But they need to be better, Buolamwini said. She brought up the issue of what she called "pale male datasets". "The gold standard benchmark dataset is biased and can lead to a false understanding of progress," she said.

Even if there was a facial recognition system with near-perfect accuracy in the testing phase, it doesn't solve the problem that most data used by law enforcement is often grainy and low resolution. A recent report by Georgetown University found that in some cases police were even trying to match people by composite artist sketches.

"Faces maybe the final frontier of privacy," Buolamwini said.

The hearing took place at the same time as Amazon shareholders tried to stop Rekognition being sold to law enforcement. The proposal was defeated, but the vote tallies were not immediately disclosed. © **The Register.**

# Can Software be Biased?

*This page is designed as a reflection on either:*

- [A summary of US Congress Testimony on Artificial Intelligence](#) (article)
- [The Coded Gaze: Bias in Artificial Intelligence](#) (video)

1) Describe three concerns experts have raised about Artificial Intelligence.

2) What are some solutions that would address these concerns?

3) How would you test whether or not a facial recognition system was equally accurate for everyone?

# Threats to Validity in a Nutshell

**Threats to Validity** can undermine a conclusion, even if the analysis was done correctly.

## People Make Mistakes

Sometimes even well-meaning Data Scientists can make mistakes if they're not careful. Data Scientists need to be careful to avoid the four threats below.

- **Selection bias** - identifying the favorite food of the rabbits won't tell us anything reliable about what all the animals eat.
- **Study bias** - If someone is supposed to assess how much cat food is eaten each day on average, but they only measure how much cat food is put in the bowls (instead of how much is actually consumed), they'll end up with an over-estimate.
- **Poor choice of summary** - Suppose a different shelter that had 10 animals recorded adoption times (in weeks) as 1, 1, 1, 7, 7, 8, 8, 9, 9, 10. Using the mode (1) to report what's typical would make it seem like the animals were adopted more quickly than they really were, since 7 out of 10 animals took at least 7 weeks to be adopted.
- **Confounding variables** - Some shelter workers might prefer cats, and steer people towards cats as a result. This would make it appear that "cats are more popular with people", when the real variable dominating the sample is what *workers at the shelter* prefer.

## Fake News

But sometimes, it's not an accident: **some people deliberately misuse statistics to create "Fake News" and manipulate others!** An evil Data Scientist might make the four mistakes above *on purpose!* Here are some other slimy ways to make an analysis invalid:

- **Using the Wrong Measure of Center** - With heavily-skewed data (like income in America), using the mean is deeply misleading.
- **Using a Correlation to Imply Causation** - Just because two variables are correlated doesn't mean one is *causing* the other!
- **Incorrect Interpretation of a Visualization** - Someone might point to the tallest bar in a bar chart or histogram and say "See? Most of the people surveyed said...", even if the tallest bar represents only a small percentage of the people surveyed!
- **Intentionally Using the Wrong Chart** - Surveying pet-owners at a dog park to ask about their favorite animal is obviously misleading. A Bar Chart will show empty space for the "Cat" category, which would be a huge red-flag that the survey used a biased sample. But using a Pie Chart will hide the problem, because there's no such thing as an "empty pie slice"!
- **Changing the Scale of a Chart** - A change in poverty from 10.1% to 10.3% is really small, but if the y-axis of the graph goes from 10 to 10.5 it will look like a HUGE climb! The same trick can be played with bar charts, histograms, or box-plots, to exaggerate small differences or hide large ones.

## Outliers: Do they stay or do they go?

In any population, there are often one or two samples that are way outside the range of the group. These outliers can really change the results of your analysis, by altering up the average or skewing the shape of the data.

- It can be tempting to remove outliers, and *sometimes* there's a good reason to do it! You might spot an obvious typo, or an answer that you can tell was written by accident.
- But *some* outliers are completely valid, and very important! A small town that has a 30x higher rate of cancer than everywhere else might point to something really important!

As Data Scientists, outliers require us to investigate more closely. And whether we decide to keep or remove them, we should *always* explain our reasoning.

# Identifying Threats to Validity

Some volunteers from the animal shelter surveyed a group of pet owners at a local dog park. They found that almost all of the owners were there with their dogs. From this survey, they concluded that dogs are the most popular pet in the state.

1) What are some possible threats to the validity of this conclusion?

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The animal shelter noticed a large increase in pet adoptions between Christmas and Valentine's Day. They conclude that at the current rate, there will be a huge demand for pets this spring.

2) What are some possible threats to the validity of this conclusion?

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## Identifying Threats to Validity (2)

*The animal shelter wanted to find out what kind of food to buy for their animals. They took a random sample of two animals and the food they eat, and they found that 100% of animals surveyed ate spider food!*

1) Explain why sampling just two animals can result in unreliable conclusions about what kind of food is needed.

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*A volunteer opens the shelter in the morning and walks all the dogs. At mid-day, another volunteer feeds all the dogs and walks them again. In the evening, a third volunteer walks the dogs a final time and closes the shelter. The volunteers report that the dogs are much friendlier and more active at mid-day, so the shelter staff assume the second volunteer must be better with animals than the others.*

2) What are some possible threats to the validity of this conclusion?

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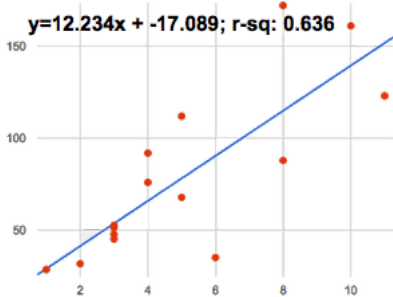
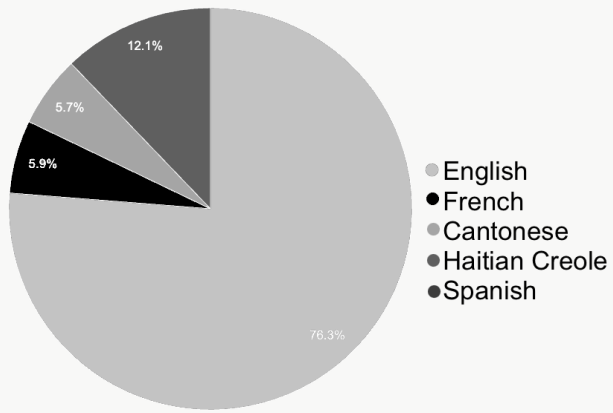
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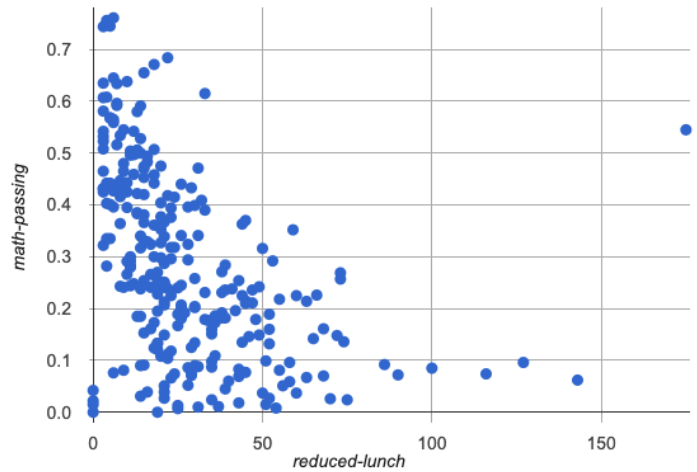
# Fake News

The *unrelated* claims below are ALL WRONG! Your job is to figure out why by looking at the data.

	The News Says...	Why it's Fake
1	 <p><i>"According to the predictor function indicated here, the value on the x-axis will predict the value on the y-axis 63.6% of the time."</i></p>	
2	<p>The average player on the Cranston East basketball team is 6'1", so we know that most of the players are taller than 6'!</p>	
3	<p>Linear regression found a positive correlation (<math>r=0.42</math>) between people's height and salary, so businesses are recognizing that taller people are more qualified.</p>	
★	 <p><i>"Despite El Paso High School being near the Mexican border, a sample of 67 students found that Haitian Creole was the most-commonly spoken language at home (after English)."</i></p>	

# Outliers: Should they Stay or Should they Go?

Tahli and Fernando are looking at a scatter plot showing the relationship between poverty and test scores at schools in Michigan. They find a trend, with low-poverty schools generally having higher test scores than high-poverty schools. However, one school is an extreme outlier: the highest poverty school in the state also has higher test scores than most of the other schools!



Tahli thinks the outlier should be removed before they start analyzing, and Fernando thinks it should stay. Here are their reasons:

Tahli's Reasons:	Fernando's Reasons:
<p>This outlier is so far from every other school - it <i>has</i> to be a mistake. Maybe someone entered the poverty level or the test scores incorrectly! We don't want those errors to influence our analysis. Or maybe it's a magnet, exam or private school that gets all the top-performing students. It's not right to compare that to non-magnet schools.</p>	<p>Maybe it's not a mistake or a special school! Maybe the school has an amazing new strategy that's different from other schools! Instead of removing an inconvenient data point from the analysis, we should be focusing our analysis on what is happening there.</p>

Do you think this outlier should stay or go? Why? What additional information might help you make your decision?

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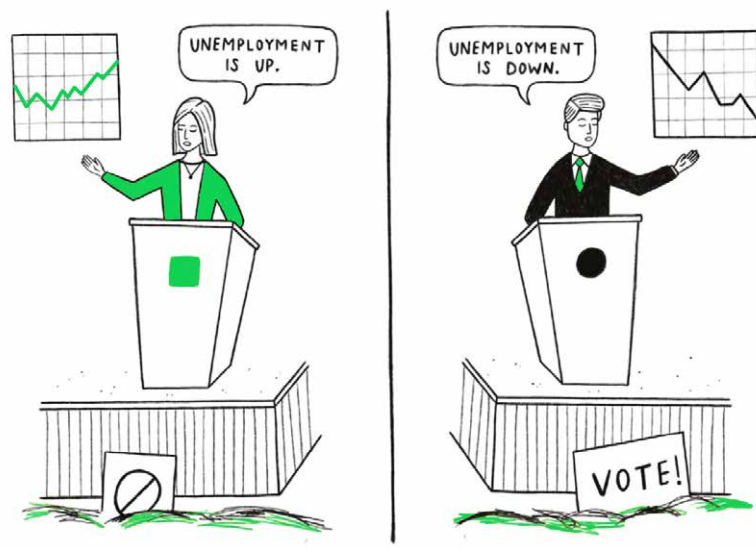
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# Data Fallacies to Avoid



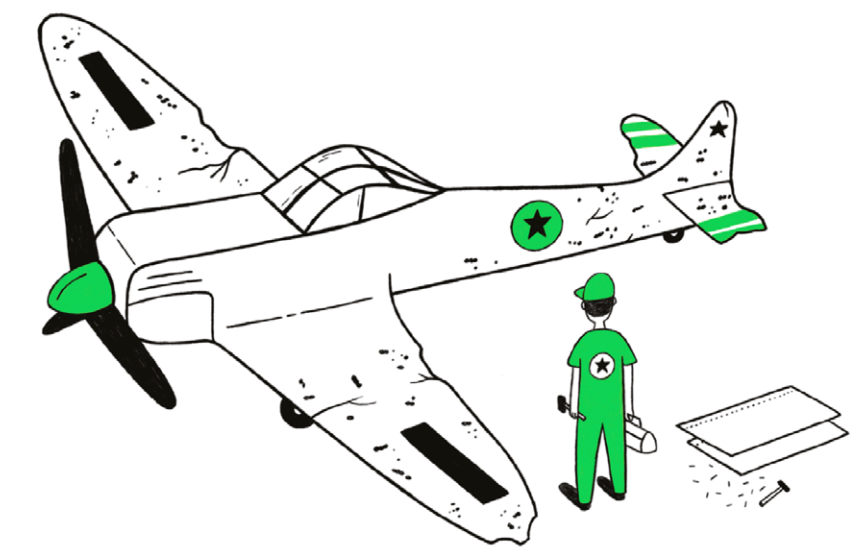
## Cherry Picking

Selecting results that fit your claim and excluding those that don't.



## Data Dredging

Repeatedly testing new hypotheses against the same set of data, failing to acknowledge that most correlations will be the result of chance.



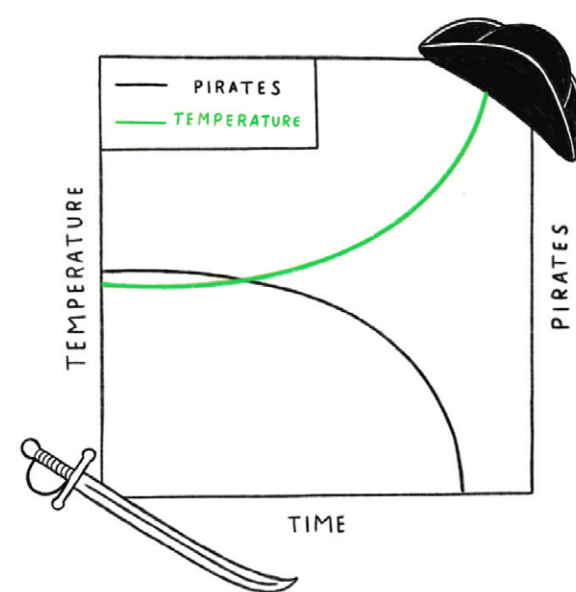
## Survivorship Bias

Drawing conclusions from an incomplete set of data, because that data has 'survived' some selection criteria.



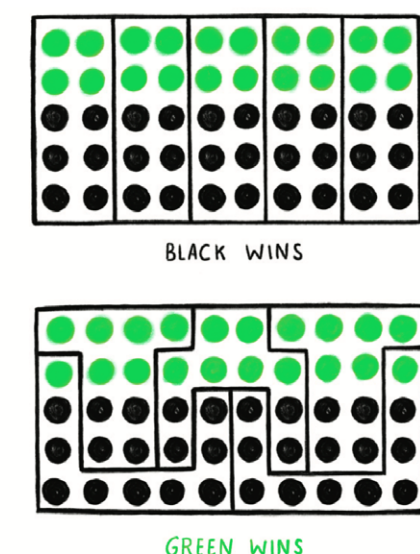
## Cobra Effect

Setting an incentive that accidentally produces the opposite result to the one intended. Also known as a Perverse Incentive.



## False Causality

Falsely assuming when two events appear related that one must have caused the other.



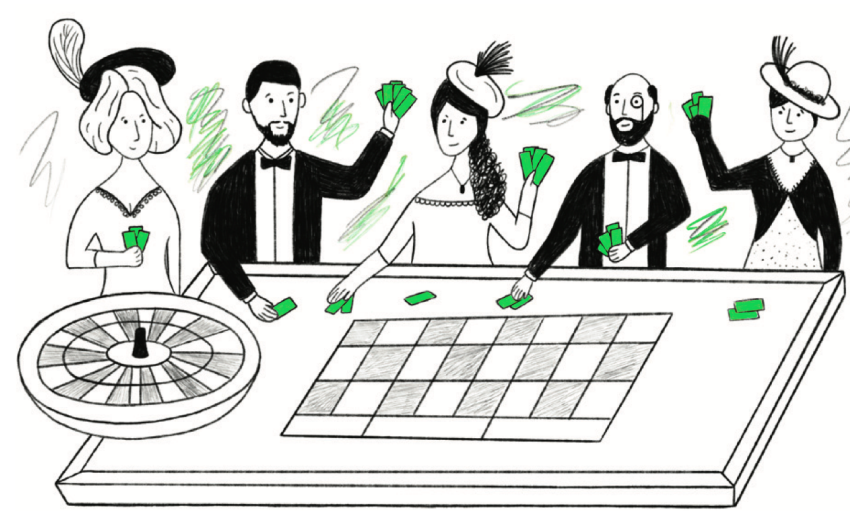
## Gerrymandering

Manipulating the geographical boundaries used to group data in order to change the result.



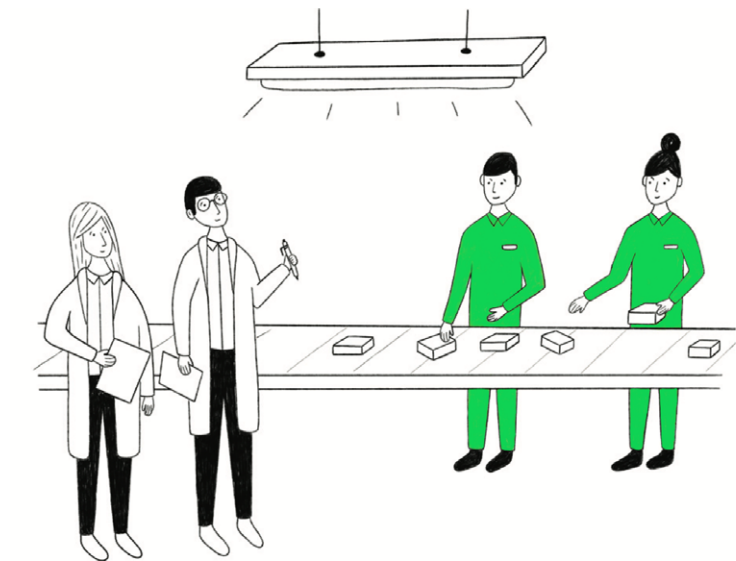
## Sampling Bias

Drawing conclusions from a set of data that isn't representative of the population you're trying to understand.



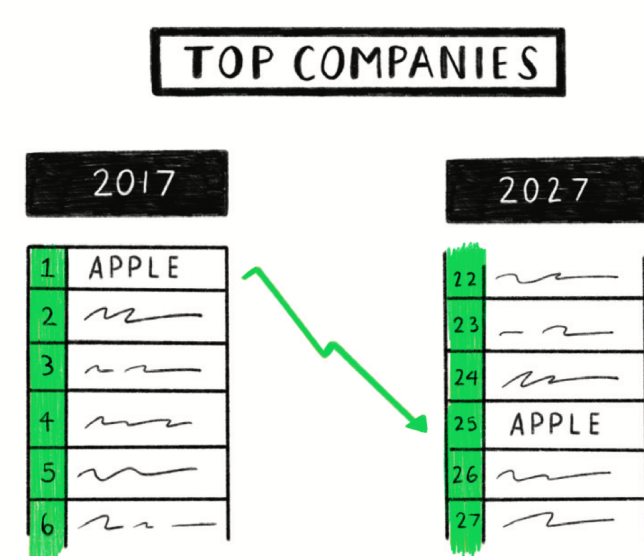
## Gambler's Fallacy

Mistakenly believing that because something has happened more frequently than usual, it's now less likely to happen in future (and vice versa).



## Hawthorne Effect

The act of monitoring someone can affect their behaviour, leading to spurious findings. Also known as the Observer Effect.



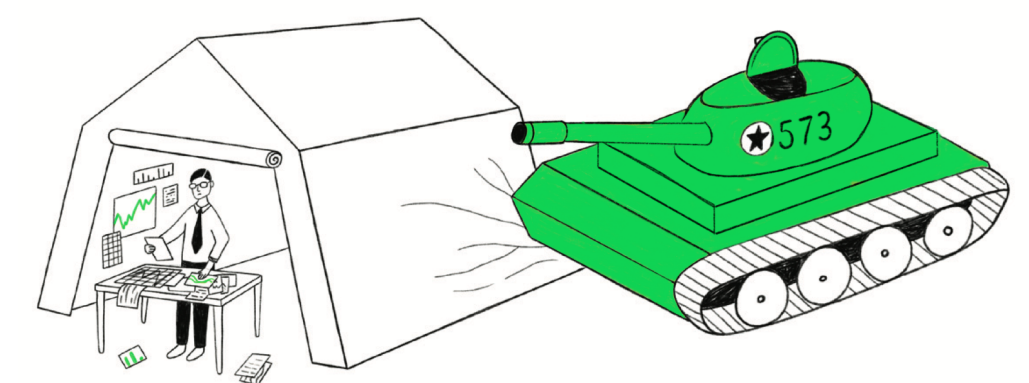
## Regression Towards the Mean

When something happens that's unusually good or bad, it will revert back towards the average over time.

APPLICATION SUCCESS RATE		
	MALE	FEMALE
SUBJECT 1	14 % (168 of 1200)	15 % (270 of 1800)
SUBJECT 2	50 % (400 of 800)	51 % (102 of 200)
TOTAL	28 % (568 of 2000)	19 % (372 of 2000) ??

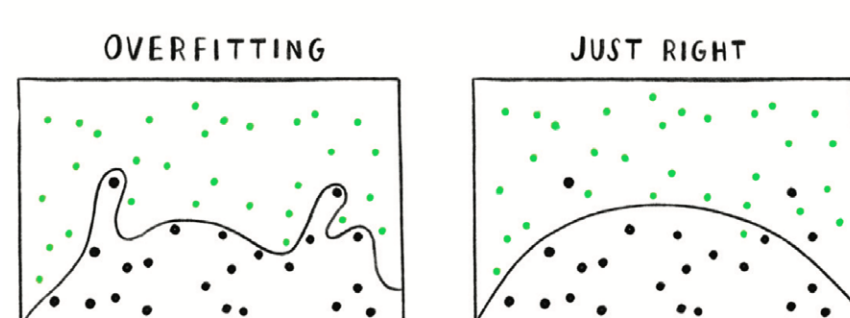
## Simpson's Paradox

When a trend appears in different subsets of data but disappears or reverses when the groups are combined.



## McNamara Fallacy

Relying solely on metrics in complex situations and losing sight of the bigger picture.



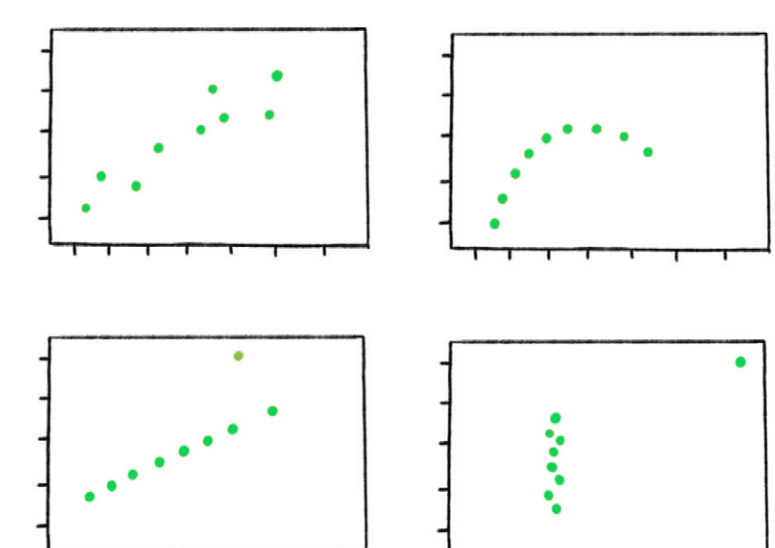
## Overfitting

Creating a model that's overly tailored to the data you have and not representative of the general trend.



## Publication Bias

Interesting research findings are more likely to be published, distorting our impression of reality.



## Danger of Summary Metrics

Only looking at summary metrics and missing big differences in the raw data.



# Selection Bias or Biased Study?

The school newspaper ran an article stating that chicken was more popular than pork in the East Village.

**Kendell thinks the study was biased.**

*Would you rather eat pork or delicious crispy fried chicken?* That's such a leading question! It encouraged people to pick chicken. I bet the results would have been different if they had asked about crispy bacon!

**Carson thinks the study suffered from selection bias.**

One of the survey sites was outside of a mosque?! Muslims don't even eat pork!

**Who's right? How do you know?**

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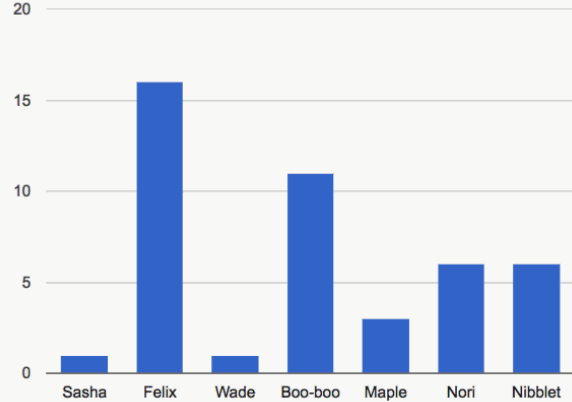
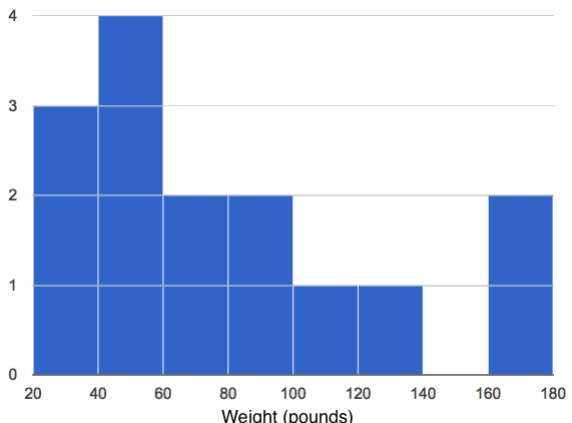
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# Fake News (2)

There are three separate, *unrelated* claims below, and ALL OF THEM ARE WRONG! Your job is to figure out why by looking at the data.

	The News Says...	Why it's Fake
1	<p>CNBC Now @CNBCnow · 4h</p> <p>BREAKING: Stocks sharply drop to new session lows; Bloomberg reports President Biden will propose a <b>capital gains</b> tax as high as 43.4% for the wealthy. <a href="https://cnb.cx/3atvBFd">cnb.cx/3atvBFd</a></p>  <p>"Stocks fell off a cliff today, plummeting sharply. Some fear the economic unrest will lead to rioting and looting!"</p>	
2	 <p>"According to this bar chart, Felix makes up a little more than 15% of the total ages of all the animals in the dataset."</p>	
3	 <p>"According to this histogram, most animals weigh between 40 and 60 pounds."</p>	

(optional)

## Identifying Threats to Validity (3)

Data scientists want to know if listening to music or podcasts reduces symptoms of stress in individuals.

- They conducted **a study of 1,000 people who were brought into a laboratory office for testing.**
- While wearing a heart-rate monitor, participants were asked to listen to either music or a podcast of their choosing while completing a series of complicated puzzles.
- The data scientists discovered that on average, **participants who listened to music had a 5% lower heart rate while completing the tasks than those who listened to podcasts.**

Before publishing their findings, the data scientists have asked you to review their claim. In the space below, indicate possible **threats to validity** faced by this study.

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## Rubric: Research Project 1

## About this Dataset

❑ Wow!	❑ Getting There	❑ Needs Improvement
I explained why this dataset is interesting to me, others like me, and why others should care about this data. I considered why the dataset was collected, and what purpose it might serve. I correctly identified all the rows, columns, and types in my dataset.	I explained why this dataset was interesting to me and at least one other person/group, and shared <i>something</i> about where it came from. I correctly identified most of the rows, columns, and types in my dataset.	I explained why this dataset was interesting to me, and shared <i>something</i> about where it came from. I correctly identified some rows, columns, and types in my dataset.

## My Questions

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I had lots of questions by the end of the exploration, and I chose at least two that I thought were most interesting. I explained why I thought they were interesting, and wrote about grouped samples that might be good to explore when answering those questions.	I had a few questions by the end of the exploration, and I chose at least one that was interesting. I wrote about grouped samples that might be good to explore.	I picked a question, and wrote about grouped samples.

### Analysis: Quantity, Variety, and Connectedness of Visualizations

❑ Wow!	❑ Getting There	❑ Needs Improvement
I used a variety of categorical and quantitative visualizations, including at least 10 different visualizations in my project. I gave each display a descriptive title. I specified how the display changed my thinking and influenced the next display that I chose to make.	Throughout my project, I used a limited assortment of visualizations. I included at least 8 different visualizations in my project. Most of my visualizations were descriptively titled. I attempted to describe how the display changed my thinking and influenced the next display that I made - but my descriptions were unclear.	I included 4 or fewer visualizations in my project. The visualizations did not include titles, or the titles were not descriptive. I did not adequately describe how each display changed my thinking.

## Discussion: Threats to Validity, Ethical Implications, Questions for Future Study

<input type="checkbox"/> Wow!	<input type="checkbox"/> Getting There	<input type="checkbox"/> Needs Improvement
I explained my findings clearly and in detail. I also wrote about possible threats to validity, considering all of the different threats we learned about in the context of diversity, bias, power, and discrimination. I explained why (or why not) the results were enough to make a strong claim. I thought about the ethical implications of collecting this data, or how my research might be used in good or bad ways. I wrote about how I would continue this research, with more data and/or more questions.	I explained my findings, and wrote about some threats to validity and ethical questions. I considered some issues regarding diversity, bias, power and discrimination - but not all of them. I wrote about possible ways to continue the research.	I talked about my findings, but only discussed some threats to validity, ethics, or possible future research. Other parts were missing.

### Additional Teacher Feedback



# Rubric: Research Project 2

**Students:** -In the left hand column, record the title of each display you made. Write titles in the order in which they appear in your slide deck. If you need additional copies of this page, ask your teacher.

## Analysis:

<input type="checkbox"/> <b>Wow!</b>	<input type="checkbox"/> <b>Getting There</b>	<input type="checkbox"/> <b>Needs Improvement</b>
I interpreted the display accurately and thoughtfully. I explained how the display helps me answer the question I chose to study.	I interpreted the display accurately. I attempted to connect the display to my research question, but that connection was sometimes unclear.	My interpretation of the display is inaccurate. It was unclear how the display connected to or answered my research question.

Display	Rating	Teacher Feedback
	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	
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	<input type="checkbox"/> Wow <input type="checkbox"/> Getting There <input type="checkbox"/> Needs Improvement	

# Data Cycle

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

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# Data Cycle

<b>Ask Questions</b> 	What question do you have? <hr/>	<b>Question Type</b> (circle one): Lookup Arithmetic Statistical
<b>Consider Data</b> 	Which Rows should we investigate? (All the rows, just the cats, fixed dogs, etc.) <hr/> What Column(s) do we need? (age, weight-in-kilograms, weeks, etc.) <hr/>	
<b>Analyze Data</b> 	If you only need some rows, define your filter function here (Need help? Use the Design Recipe!) <hr/> If you need to make a new column, define your builder function here (Need help? Use the Design Recipe!) <hr/> What code will make the table or display you want? <hr/>	
<b>Interpret Data</b> 	What did you find out? What can you infer? <hr/> What - if any - new question(s) does this raise? <hr/> <hr/>	

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# Design Recipe

Directions:

## Contract and Purpose Statement

Every contract has three parts...

# \_\_\_\_\_ :: \_\_\_\_\_ -> \_\_\_\_\_  
function name Domain Range

# \_\_\_\_\_  
what does the function do?

## Examples

Write some examples, then circle and label what changes...

examples:

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

\_\_\_\_\_ ( \_\_\_\_\_ ) is \_\_\_\_\_  
function name input(s) what the function produces

end

## Definition

Write the definition, giving variable names to all your input values...

fun \_\_\_\_\_ ( \_\_\_\_\_ ):  
function name variable(s)

\_\_\_\_\_  
what the function does with those variable(s)

end

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what the function does with those variable(s)

end

# The Animals Dataset

This is a printed version of the animals spreadsheet.

*\*The numbers on the left side are NOT part of the table!\* They are provided to help you identify the index of each row.*

	name	species	sex	age	fixed	legs	pounds	weeks
0	Sasha	cat	female	1	false	4	6.5	3
1	Snuffles	rabbit	female	3	true	4	3.5	8
2	Mittens	cat	female	2	true	4	7.4	1
3	Sunflower	cat	female	5	true	4	8.1	6
4	Felix	cat	male	16	true	4	9.2	5
5	Sheba	cat	female	7	true	4	8.4	6
6	Billie	snail	hermaphrodite	0.5	false	0	0.1	3
7	Snowcone	cat	female	2	true	4	6.5	5
8	Wade	cat	male	1	false	4	3.2	1
9	Hercules	cat	male	3	false	4	13.4	2
10	Toggle	dog	female	3	true	4	48	1
11	Boo-boo	dog	male	11	true	4	123	24
12	Fritz	dog	male	4	true	4	92	3
13	Midnight	dog	female	5	false	4	112	4
14	Rex	dog	male	1	false	4	28.9	9
15	Gir	dog	male	8	false	4	88	5
16	Max	dog	male	3	false	4	52.8	8
17	Nori	dog	female	3	true	4	35.3	1
18	Mr. Peanutbutter	dog	male	10	false	4	161	6
19	Lucky	dog	male	3	true	3	45.4	9
20	Kujo	dog	male	8	false	4	172	30
21	Buddy	lizard	male	2	false	4	0.3	3
22	Gila	lizard	female	3	true	4	1.2	4
23	Bo	dog	male	8	true	4	76.1	10
24	Nibblet	rabbit	male	6	false	4	4.3	2
25	Snuggles	tarantula	female	2	false	8	0.1	1
26	Daisy	dog	female	5	true	4	68	8
27	Ada	dog	female	2	true	4	32	3
28	Miaulis	cat	male	7	false	4	8.8	4
29	Heathcliff	cat	male	1	true	4	2.1	2
30	Tinkles	cat	female	1	true	4	1.7	3
31	Maple	dog	female	3	true	4	51.6	4

# Sentence Starters

Use these sentence starters to help describe patterns, make predictions, find comparisons, share discoveries, formulate hypotheses, and ask questions.

## Patterns:

- I noticed a pattern when I looked at the data. The pattern is \_\_\_\_\_
- I see a pattern in the data collected so far. My graph shows \_\_\_\_\_

## Predictions:

- Based on the patterns I see in the data collected so far, I predict that \_\_\_\_\_
- My prediction for \_\_\_\_\_ is \_\_\_\_\_

## Comparisons:

- When I compared \_\_\_\_\_ and \_\_\_\_\_, I noticed that \_\_\_\_\_
- The similarities I see between \_\_\_\_\_ and \_\_\_\_\_ are \_\_\_\_\_
- The differences I see between \_\_\_\_\_ and \_\_\_\_\_ are \_\_\_\_\_

## Surprises and Discoveries:

- I discovered that \_\_\_\_\_
- I was surprised by \_\_\_\_\_
- I noticed something unusual about \_\_\_\_\_

## Hypotheses:

- A possible explanation for what the data showed is \_\_\_\_\_
- A factor that affected this data might have been \_\_\_\_\_
- I think this data was affected by \_\_\_\_\_

## Questions:

- I wonder why \_\_\_\_\_
- I wonder how \_\_\_\_\_
- How are \_\_\_\_\_ affected by \_\_\_\_\_
- How will \_\_\_\_\_ change if \_\_\_\_\_

# Contracts for Data Science

Contracts tell us how to use a function, by telling us three important things:

1. The **Name**
2. The **Domain** of the function - what kinds of inputs do we need to give the function, and how many?
3. The **Range** of the function - what kind of output will the function give us back?

For example: The contract `triangle :: (Number, String, String) -> Image` tells us that the name of the function is `triangle`, it needs three inputs (a Number and two Strings), and it produces an Image.

With these three pieces of information, we know that typing `triangle(20, "solid", "green")` will evaluate to an Image.

Name	Domain	Range
# bar-chart	:: ( <u>Table</u> , <u>String</u> ) <small>table-name column</small>	-> Image
<code>bar-chart(animals-table, "species")</code>		
# bar-chart-summarized	:: ( <u>Table</u> , <u>String</u> , <u>String</u> ) <small>table-name labels values</small>	-> Image
<code>bar-chart-summarized(count(animals-table, "species"), "value", "count")</code>		
# box-plot	:: ( <u>Table</u> , <u>String</u> ) <small>table-name column</small>	-> Image
<code>box-plot(animals-table, "weeks")</code>		
# box-plot-scaled	:: ( <u>Table</u> , <u>String</u> , <u>Number</u> , <u>Number</u> ) <small>table-name column low high</small>	-> Image
<code>box-plot-scaled(animals-table, "weeks", 1, 40)</code>		
# build-column	:: ( <u>Table</u> , <u>String</u> , ( <u>Row -&gt; Value</u> ) ) <small>table-name column builder-function</small>	-> Table
<code>build-column(animals-table, "kilos", kilograms)</code>		
# circle	:: ( <u>Number</u> , <u>String</u> , <u>String</u> ) <small>radius fill-style color</small>	-> Image
<code>circle(50, "solid", "purple")</code>		
# count	:: ( <u>Table</u> , <u>String</u> ) <small>table-name column</small>	-> Table
<code>count(animals-table, "species")</code>		
# dot-plot	:: ( <u>Table</u> , <u>String</u> , <u>String</u> ) <small>table-name labels values</small>	-> Image
<code>dot-plot(animals-table, "name", "pounds")</code>		
# ellipse	:: ( <u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u> ) <small>width height fill-style color</small>	-> Image
<code>ellipse(100, 50, "outline", "orange")</code>		
# filter	:: ( <u>Table</u> , ( <u>Row -&gt; Boolean</u> ) ) <small>table-name tester-function</small>	-> Table
<code>filter(animals-table, is-dog)</code>		
# first-n-rows	:: ( <u>Table</u> , <u>Number</u> ) <small>table-name num-rows</small>	-> Table
<code>first-n-rows(animals-table, 15)</code>		
# fit-model	:: ( <u>Table</u> , <u>String</u> , <u>String</u> , <u>String</u> , <u>String</u> , ( <u>Num -&gt; Num</u> ) ) <small>table-name labels xs ys model-function</small>	-> Image
<code>fit-model(animals-table, "name", "pounds", "weeks", f)</code>		
# histogram	:: ( <u>Table</u> , <u>String</u> , <u>String</u> , <u>Number</u> ) <small>table-name labels values bin-size</small>	-> Image
<code>histogram(animals-table, "species", "weeks", 2)</code>		
# image-bar-chart	:: ( <u>Table</u> , <u>String</u> , ( <u>Row -&gt; Image</u> ) ) <small>table-name values draw-function</small>	-> Image
<code>image-bar-chart(animals-table, "species", f)</code>		
# image-histogram	:: ( <u>Table</u> , <u>String</u> , <u>Number</u> , ( <u>Row -&gt; Image</u> ) ) <small>table-name values bin-size draw-function</small>	-> Image
<code>image-histogram(animals-table, "pounds", 2, f)</code>		



Name	Domain	Range
# image-pie-chart	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>values</sub> , <u>(Row -&gt; Image)</u> <sub>draw-function</sub> )	-> Image
image-pie-chart(animals-table, "sex", f)		
# image-scatter-plot	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> , <u>(Row -&gt; Image)</u> <sub>draw-function</sub> )	-> Image
image-scatter-plot(animals-table, "pounds", "weeks", f)		
# isosceles-triangle	:: ( <u>Number</u> <sub>size</sub> , <u>Number</u> <sub>vertex-angle</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
isosceles-triangle(50, 20, "solid", "grey")		
# line-graph	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>labels</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> )	-> Image
line-graph(animals-table, "name", "pounds", "weeks")		
# lr-plot	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>labels</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> )	-> Image
lr-plot(animals-table, "name", "pounds", "weeks")		
# mean	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Number
mean(animals-table, "pounds")		
# median	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Number
median(animals-table, "pounds")		
# modes	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> List
modes(animals-table, "pounds")		
# modified-box-plot	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Image
modified-box-plot(animals-table, "pounds")		
# modified-box-plot-scaled	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> , <u>Number</u> <sub>low</sub> , <u>Number</u> <sub>high</sub> )	-> Image
modified-box-plot-scaled(animals-table, "weeks", 1, 40)		
# modified-vert-box-plot	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Image
modified-vert-box-plot(animals-table, "pounds")		
# modified-vert-box-plot-scaled	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> , <u>Number</u> <sub>low</sub> , <u>Number</u> <sub>high</sub> )	-> Image
modified-vert-box-plot-scaled(animals-table, "weeks", 1, 40)		
# multi-bar-chart	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>group</sub> , <u>String</u> <sub>subgroup</sub> )	-> Image
multi-bar-chart(animals-table, "species", "sex")		
# overlay	:: ( <u>Image</u> <sub>top</sub> , <u>Image</u> <sub>bottom</sub> )	-> Image
overlay(circle(10, "solid", "black"), square(50, "solid", "red"))		
# pie-chart	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Image
pie-chart(animals-table, "species")		
# pie-chart-summarized	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>labels</sub> , <u>String</u> <sub>values</sub> )	-> Image
pie-chart-summarized(count(animals-table, "species"), "value", "count")		
# r-value	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> )	-> Number
r-value(animals-table, "pounds", "weeks")		
# radial-star	:: ( <u>Num</u> <sub>points</sub> , <u>Num</u> <sub>outer</sub> , <u>Num</u> <sub>inner</sub> , <u>Str</u> <sub>fill-style</sub> , <u>Str</u> <sub>color</sub> )	-> Image
radial-star(6, 20, 50, "solid", "red")		

Name	Domain	Range
# random-rows	:: ( <u>Table</u> <sub>table-name</sub> , <u>Number</u> <sub>num-rows</sub> )	-> Table
<i>random-rows(animals-table, 10) # select 10 random rows from the table</i>		
# rectangle	:: ( <u>Number</u> <sub>width</sub> , <u>Number</u> <sub>height</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>rectangle(100, 50, "outline", "green")</i>		
# regular-polygon	:: ( <u>Number</u> <sub>size</sub> , <u>Number</u> <sub>vertices</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>regular-polygon(25,5, "solid", "purple")</i>		
# rhombus	:: ( <u>Number</u> <sub>size</sub> , <u>Number</u> <sub>top-angle</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>rhombus(100, 45, "outline", "pink")</i>		
# right-triangle	:: ( <u>Number</u> <sub>leg1</sub> , <u>Number</u> <sub>leg2</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>right-triangle(50, 60, "outline", "blue")</i>		
# rotate	:: ( <u>Number</u> <sub>degrees</sub> , <u>Image</u> <sub>img</sub> )	-> Image
<i>rotate(45, star(50, "solid", "dark-blue"))</i>		
# row-n	:: ( <u>Table</u> <sub>table-name</sub> , <u>Number</u> <sub>index</sub> )	-> Row
<i>row-n(animals-table, 2)</i>		
# S	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> , <u>(Num -&gt; Num)</u> <sub>model-function</sub> )	-> Number
<i>S(animals-table, "name", "pounds","weeks", f)</i>		
# scatter-plot	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>labels</sub> , <u>String</u> <sub>xs</sub> , <u>String</u> <sub>ys</sub> )	-> Image
<i>scatter-plot(animals-table, "name", "pounds","weeks")</i>		
# sort	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> , <u>Boolean</u> <sub>ascending</sub> )	-> Table
<i>sort(animals-table, "species", true)</i>		
# sqr	:: ( <u>Number</u> )	-> Number
<i>sqr(4)</i>		
# sqrt	:: ( <u>Number</u> )	-> Number
<i>sqrt(4)</i>		
# square	:: ( <u>Number</u> <sub>size</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>square(50, "solid", "red")</i>		
# stacked-bar-chart	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>group</sub> , <u>String</u> <sub>subgroup</sub> )	-> Image
<i>stacked-bar-chart(animals-table, "species", "sex")</i>		
# star	:: ( <u>Number</u> <sub>radius</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>star(50, "solid", "red")</i>		
# star-polygon	:: ( <u>Number</u> <sub>size</sub> , <u>Number</u> <sub>point-count</sub> , <u>Number</u> <sub>step-count</sub> , <u>String</u> <sub>fill-style</sub> , <u>String</u> <sub>color</sub> )	-> Image
<i>star-polygon(100, 10, 3 ,"outline", "red")</i>		
# stdev	:: ( <u>Table</u> <sub>table-name</sub> , <u>String</u> <sub>column</sub> )	-> Number
<i>stdev(animals-table, "pounds")</i>		
# string-contains	:: ( <u>String</u> <sub>haystack</sub> , <u>String</u> <sub>needle</sub> )	-> Boolean
<i>string-contains("hotdog", "dog")</i>		
# string-length	:: ( <u>String</u> )	-> Number
<i>string-length("rainbow")</i>		





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