

Student Workbook Fall, 2023 - Pyret Edition



Workbook v3.0

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Computing Needs All Voices!

The pioneers pictured below are featured in our Computing Needs All Voices lesson. To learn more about them and their contributions, visit <u>https://bit.ly/bootstrap-pioneers</u>.



We are in the process of expanding our collection of pioneers. If there's someone else whose work inspires you, please let us know at https://bit.ly/pioneer-suggestion.

Notice and Wonder

Write down what you Notice and Wonder from the What Most Schools Don't Teach video.

"Notices" should be statements, not questions. What stood out to you? What do you remember? "Wonders" are questions.

 What do you Notice?
 What do you Wonder?

Windows and Mirrors

Think about the images and stories you've just encountered. Identify something(s) that served as a mirror for you, connecting you with your own identity and experience of the world. Write about who or what you connected with and why.

Identify something(s) from the film or the posters that served as a window for you, giving you insight into other people's experiences or expanding your thinking in some way.

Reflection: Problem Solving Advantages of Diverse Teams

This reflection is designed to follow reading LA Times Perspective: A solution to tech's lingering diversity problem? Try thinking about ketchup

1) The author argues that tech companies with diverse teams have an advantage. Why?

2) What suggestions did the article offer for tech companies looking to diversify their teams?

3) What is one thing of interest to you in the author's bio?

4) Think of a time when you had an idea that felt "out of the box". Did you share your idea? Why or why not?

5) Can you think of a time when someone else had a strategy or idea that you would never have thought of, but was interesting to you and/or pushed your thinking to a new level?

6) Based on your experience of exceptions to mainstream assumptions, propose another pair of questions that could be used in place of "Where do you keep your ketchup?" and "What would you reach for instead?"

The Math Inside video games

- Video games are all about *change*! How fast is this character moving? How does the score change if the player collects a coin? Where on the screen should we draw a castle?
- We can break down a game into parts, and figure out which parts change and which ones stay the same. For example:
 - Computers use **coordinates** to position a character on the screen. These coordinates specify how far from the left (x-coordinate) and the bottom (y-coordinate) a character should be. Negative values can be used to "hide" a character, by positioning them somewhere off the screen.
 - When a character moves, those coordinates change by some amount. When the score goes up or down, it *also* changes by some amount.
- From the computer's point of view, the whole game is just a bunch of numbers that are changing according to some equations. We might not be able to see those equations, but we can definitely see the effect they have when a character jumps on a mushroom, flies on a dragon, or mines for rocks!
- Modern video games are *incredibly* complex, costing millions of dollars and several years to make, and relying on hundreds of programmers and digital artists to build them. But building even a simple game can give us a good idea of how the complex ones work!

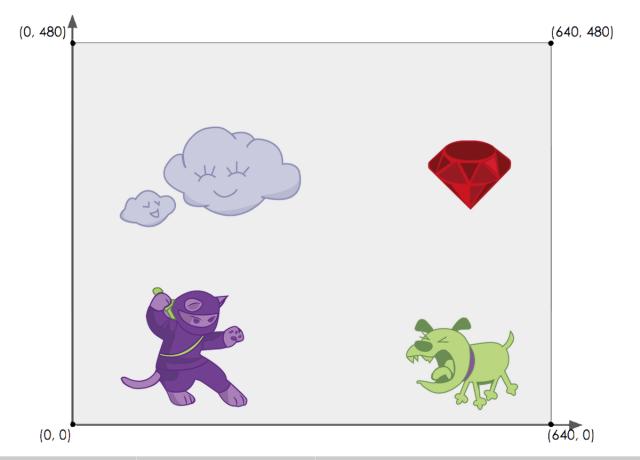
Notice and Wonder

| ices" should be statements, not questions. What stood out to you? | |
|---|---------------------|
| What do you Notice? | What do you Wonder? |
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Reverse Engineer a video game

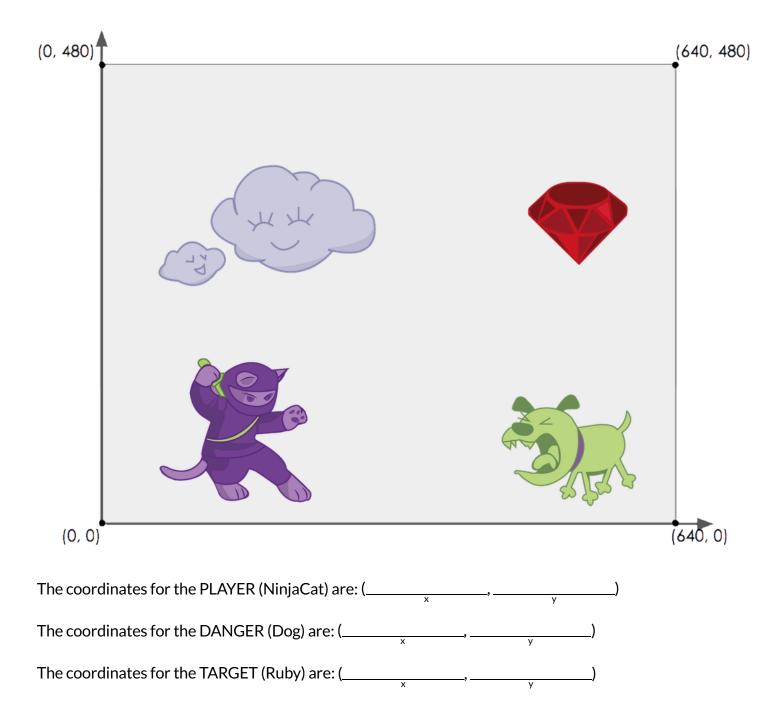
This page is designed to be used with the <u>Ninja Cat Game</u>.

What is changing in the game? What variables is the program keeping track of? The first example is filled in for you.



| Thing in the Game | What Changes About It? | More Specifically what variable(s) are being tracked? |
|-------------------|------------------------|---|
| Dog | Position | x-coordinate |
| | | |
| | | |
| | | |
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Estimating Coordinates



Brainstorm Your Own Game

| Created | by: |
|---------|-----|
|---------|-----|

Background

Our game takes place:

In space? The desert? A mall?

Player

The Player is a ______ The Player moves only up and down.

Target

Your Player GAINS points when they hit The Target.

The Target is a

The Target moves only to the left or right.

Danger

Your Player LOSES points when they hit The Danger.

The Danger is a _____ The Danger moves only to the left or right.

Artwork/Sketches/Proof of Concept

Below is a 640x480 rectangle, representing your game screen.

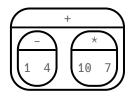
- Label the bottom-left corner (0,0).
- Label the other three corners with their corresponding coordinates.
- In the rectangle, sketch a picture of your game!

Order of Operations

If you were to write instructions for getting ready for school, it would matter very much which instruction came first: putting on your socks, putting on your shoes, etc.

Sometimes we need multiple expressions in mathematics, and the order matters there, too! Mathematicians didn't always agree on the **Order** of **Operations**, but at some point it became important to develop rules to help them work together.

To help us organize our math into something we can trust, we can *diagram* a math expression using the **Circles of Evaluation**. For example, the expression $1 - 4 + 10 \times 7$ can be diagrammed as shown below.



Order of Operations is important when programming, too!

To convert a **Circle of Evaluation** into code, we walk through the circle from outside-in, moving left-to-right. We type an open parenthesis when we *start* a circle, and a close parenthesis when we *end* one. Once we're in a circle, we write whatever is on the left of the circle, then the **operation** at the top, and then whatever is on the right. The circle above, for example, would be programmed as $((1 - 4) + (10 \times 7))$.

Completing Circles of Evaluation from Arithmetic Expressions

For each expression on the left, finish the Circle of Evaluation on the right by filling in the blanks.

| I OI Eaci | Arithmetic Expression | Circle of Evaluation on the right by filling in the blanks. Circle of Evaluation |
|-----------|--|---|
| 1 | $4+2-\frac{10}{5}$ | |
| 2 | 7-1+5	imes 8 | + (7 1) * |
| 3 | $\frac{-15}{5+-8}$ | / + 5 |
| 4 | (4+(9-8))	imes 5 | |
| 5 | $6 \ 	imes \ 4 + rac{96}{5}$ | |
| * | $rac{20}{6+4} - rac{5 	imes 9}{-12 - 3}$ | |

Matching Circles of Evaluation and Arithmetic Expressions

Draw a line from each Circle of Evaluation on the left to the corresponding arithmetic expression on the right.

| w a line from each Circle of Evaluation on th Circle of Evaluation | ne left to the correspondir | ig an infinetic expression on the | Arithmetic Expression |
|---|-----------------------------|-----------------------------------|--------------------------------|
| | 1 | A | 1÷(1×1) |
| | 2 | В | (1 + 1) – 1 |
| | 3 | С | $(1 \times 1) \div 1$ |
| $\begin{array}{c} - \\ + \\ 1 \\ 1 \end{array}$ | 4 | D | $(1 + (1 - 1)) \times (1 + 1)$ |
| $ \begin{array}{c} $ | 5 | E | $(1-1) \times (1+1)$ |

Translate Arithmetic to Circles of Evaluation & Code (Intro)

Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

| | Arithmetic Expression | Circle of Evaluation, then translate then | Code |
|---|-----------------------|---|------|
| 1 | (3 × 7) – (1 + 2) | | |
| 2 | 3 - (1 + 2) | | |
| 3 | 3 – (1 + (5 × 6)) | | |
| 4 | (1 + (5 × 6)) – 3 | | |

Completing Partial Code from Circles of Evaluation

For each Circle of Evaluation on the left, finish the Code on the right by filling in the blanks.

| | Circle of Evaluation | Code |
|---|---|-------------------|
| 1 | + 16 * 6 -3 | (+(6 *)) |
| 2 | - + 25 13 (2 4) | ((+ 13) (4)) |
| 3 | * + 28 10 4 | ((+ 4)) |
| 4 | × 13 / 7 + 2 -4 | (13 (7 (24))) |
| 5 | $\begin{array}{c c} + \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ 8 & 1 \end{array} \end{array} \begin{array}{c} - \\ \hline \\ 5 & 3 \end{array}$ | (((8 1) 3) (5 3)) |
| 6 | / + 7 9 2 4 | ((+) / (*)) |

Matching Circles of Evaluation & Code

Draw a line from each Circle of Evaluation on the left to the corresponding Code on the right.

| Draw a line from each Circle of Evaluation | on on the left to the corresponding | Code on the rig | ht. |
|--|-------------------------------------|-----------------|---------------------------|
| Circle of Evaluation | | | Code |
| + 1 1 + 1 1 | 1 | A | ((1 - (1 + 1)) * 1) |
| | 2 | В | ((1 - 1) * (1 + 1)) |
| $ \begin{array}{c} $ | 3 | С | ((1 + 1) * ((1 + 1) - 1)) |
| + | 4 | D | ((1 + 1) - 1) |
| $ \begin{array}{c} $ | 5 | Ε | ((1 - 1) + 1) |

Translate Arithmetic to Circles of Evaluation & Code (2)

Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

| nunsi | Arithmetic Expression | ns below into Circles of Evaluation, then translate then Circle of Evaluation | Code |
|-------|-------------------------|--|------|
| 1 | 6 × 8 + (7 – 23) | | |
| 2 | 18 ÷ 2 + 24 × 4 – 2 | | |
| 3 | (22 – 7) ÷ (3 + 2) | | |
| 4 | 24 ÷ 4 × 2 – 6 + 20 × 2 | | |

| A ILLINEED CAD ESSIDIE COLLECT CHARACTER OF EXPLICIENT CARACTER OF INTERPORT Table An interference interferenc | ransk | | ณ 17 | m |
|--|---|------------------------------|--------------------------------|---------------------------------|
| A location that translate them to Code. Hint: Two useful functions are num-sign and | ate each of the arithmetic expressions below Arithmetic Expression | $\frac{16+3^2}{\sqrt{49}-2}$ | 45 - 9 	imes (3 + (2 - 4)) - 7 | $50\div5	imes2-((3+4)	imes2-5)$ |
| tionsare num-sqr and num-sqr. | into Circles of Evaluation, then translate them to Code. Hint: Two useful fun Circle of Evaluation | | | |
| | tions are num-sqr and num-sqrt. | | | |

(

Introduction to Programming

The **Editor** is a software program we use to write Code. Our Editor allows us to experiment with Code on the right-hand side, in the **Interactions Area**. For Code that we want to *keep*, we can put it on the left-hand side in the **Definitions Area**. Clicking the "Run" button causes the computer to re-read everything in the Definitions Area and erase anything that was typed into the Interactions Area.

Data Types

Programming languages involve different data types, such as Numbers, Strings, Booleans, and even Images.

- Numbers are values like 1, 0.4, 1/3, and -8261.003.
 - Numbers are usually used for quantitative data and other values are usually used as categorical data.
 - In Pyret, any decimal *must* start with a 0. For example, 0.22 is valid, but .22 is not.
- Strings are values like "Emma", "Rosanna", "Jen and Ed", or even "08/28/1980".
- All strings *must* be surrounded in quotation marks.
- Booleans are either true or false.

All values evaluate to themselves. The program 42 will evaluate to 42, the String "Hello" will evaluate to "Hello", and the Boolean false will evaluate to false.

Operators

Operators (like +, -, *, <, etc.) work the same way in Pyret that they do in math.

- Operators are written between values, for example: 4 + 2.
- In Pyret, operators must always have a space around them. 4 + 2 is valid, but 4+2 is not.
- If an expression has different operators, parentheses must be used to show order of operations. 4 + 2 + 6 and 4 + (2 * 6) are valid, but 4 + 2 * 6 is not.

Applying Functions

Applying functions works much the way it does in math. Every function has a name, takes some inputs, and produces some output. The function name is written first, followed by a list of *arguments* in parentheses.

- In math this could look like f(5) or g(10, 4).
- In Pyret, these examples would be written as f(5) and g(10, 4).
- Applying a function to make images would look like star(50, "solid", "red").
- There are many other functions, for example num-sqr, num-sqrt, triangle, square, string-repeat, etc.

Functions have *contracts*, which help explain how a function should be used. Every Contract has three parts:

- The Name of the function literally, what it's called.
- The Domain of the function what types of values the function consumes, and in what order.
- The Range of the function what type of value the function produces.

Strings and Numbers

Make sure you've loaded the code.pyret.org (CPO), clicked "Run", and are working in the Interactions Area.

Strings

String values are always in quotes.

- Try typing your name (in quotes!).
- Try typing a sentence like "I'm excited to learn to code!" (in quotes!).
- Try typing your name with the opening quote, but without the closing quote. Read the error message!
- Now try typing your name without any quotes. Read the error message!

1) Explain what you understand about how strings work in this programming language.

Numbers

2) Try typing 42 into the Interactions Area and hitting "Enter".

3) Is 42 the same as "42"? Why or why not? Write your answer below:

4) What is the largest number the editor can handle?

5) Try typing 0.5. Then try typing .5. Then try clicking on the answer. Experiment with other decimals. Explain what you understand about

how decimals work in this programming language.

6) What happens if you try a fraction like 1/3?

7) Try writing **negative** integers, fractions and decimals. What do you learn?

Operators

8) Just like math, Pyret has *operators* like +, –, * and /. Try typing in 4 + 2, and then 4+2 (without the spaces). What can you conclude from this?

9) Type in the following expressions, one at a time: 4 + 2 * 6, (4 + 2) * 6, 4 + (2 * 6). What do you notice?

10) Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this?

Booleans

Boolean-producing expressions are yes-or-no questions and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down your prediction in the blanks provided and then type the code into the Interactions Area to see what it returns.

| | Prediction | Result | | Prediction | Result |
|-----------------------|---------------------------|------------------|-----------------------------------|----------------------|---------------|
| 1) 3 <= 4 | | | 2) "a" > "b" | | |
| 3) 3 == 2 | | | 4) "a" < "b" | | |
| 5) 2 < 4 | | | 6) "a" == "b" | | |
| 7) 5 >= 5 | | | 8) "a" <> "a" | | |
| 9) 4 >= 6 | | | 10) "a" >= "a" | | |
| 11) 3 <> 3 | | | 12) "a" <> "b" | | |
| 13) 4 <> 3 | | | 14) "a" >= "b" | | |
| 15) In your own words | s, describe what < do | es. | | | |
| 16) In your own words | s, describe what $\geq d$ | oes. | | | |
| 17) In your own words | s, describe what $<>$ d | oes. | | | |
| | | | Predictio | n: | Result: |
| 18) string-contai | ins("catnap", "c | at") | | | |
| 19) string-contai | ins("cat", "catn | ap") | | | |
| 20) In your own words | , describe what stri | .ng-contains doe | s. Can you generate another expre | ession using string- | contains that |

returns true?

²¹⁾ There are infinite numbers values out there (...-2,-1,0,-1,2...) and infinite string values ("a", "aa", "aaa"...) But how many different *Boolean* values are there?

Applying Functions

Make sure you've loaded the <u>code.pyret.org (CPO)</u>, clicked "Run", and are working in the *Interactions Area*. Type this line of code into the Interactions Area and hit "Enter":

triangle(50, "solid", "red")

| 1) What is the name of this function? |
|---|
| 2) What did the expression evaluate to? |
| 3) How many arguments does triangle expect? |
| 4) What data type does the triangle function produce? |
| |

Catching Bugs

The following lines of code are all BUGGY! Read the code and the error messages to identify the mistake.

5) triangle(20, "solid" "red")
 Pyret didn't understand your program around

triangle(20, "solid" "red")

Can you spot the mistake?

6) triangle(20, "solid")

This <u>application expression</u> errored: **triangle**(20, "solid") <u>2 arguments</u> were passed to the <u>operator</u>. The <u>operator</u> evaluated to a function accepting 3 parameters. An <u>application expression</u> expects the number of parameters and <u>arguments</u> to be the same.

Can you spot the mistake?

7) triangle(20, 10, "solid", "red")
 This <u>application expression</u> errored:
 triangle(20, 10, "solid", "red")`
 <u>4 arguments</u> were passed to the <u>operator</u>. The <u>operator</u> evaluated to a function accepting 3
 parameters. An <u>application expression</u> expects the number of parameters and <u>arguments</u> to be the
 same.

Can you spot the mistake? _____

8) triangle (20, "solid", "red")
Pyret thinks this code is probably a function call:
triangle (20, "solid", "red")
Function calls must not have space between the <u>function expression</u> and the <u>arguments</u>.

Can you spot the mistake?

Practicing Contracts: Domain & Range

13) Circle the expression below that shows the correct application of this function, based on its Contract.

A. cylinder("red", 10, 60)
B. cylinder(30, "green")
C. cylinder(10, 25, "blue")
D. cylinder(14, "orange", 25)

Matching Expressions and Contracts

Match the Contract (left) with the expression described by the function being used (right). Note: The contracts on this page are not defined in Pyret and cannot be tested in the editor.

| Contract | Expression |
|--|---|
| <pre># make-id :: String, Number -> Image</pre> | <pre>1 A make-id("Savannah", "Lopez", 32)</pre> |
| <pre># make-id :: String, Number, String -> Image</pre> | 2 B make-id("Pilar", 17) |
| <pre># make-id :: String -> Image</pre> | 3 C make-id("Akemi", 39, "red") |
| <pre># make-id :: String, String -> Image</pre> | 4 D make-id("Raïssa", "McCracken") |
| # make-id :: String, String, Number -> Image | <pre>5 E make-id("von Einsiedel")</pre> |

| Contract | | Expression |
|---|------|--|
| <pre># is-capital :: String, String -> Boolean</pre> | 6 A | show-pop("Juneau", "AK", 31848) |
| # is-capital :: String, String, String -> Boolean | 7 B | show-pop("San Juan", 395426) |
| <pre># show-pop :: String, Number -> Image</pre> | 8 C | is-capital("Accra", "Ghana") |
| <pre># show-pop :: String, String, Number -> Image</pre> | 9 D | show-pop(3751351 , "Oklahoma") |
| <pre># show-pop :: Number, String -> Number</pre> | 10 E | is-capital("Albany", "NY", "USA") |

Using Contracts

Use the contracts to write expressions to generate images similar to those pictured. Go to <u>code.pyret.org (CPO)</u> to test your code.

ellipse :: Number, Number, String, String -> Image Use the Contract to write an expression that generates a similar image: Use the Contract to write an expression that generates a similar image: Use the Contract to write an expression that generates a similar image: What changes with the first Number? What about the shape changes with the second Number? Write an expression using ellipse to produce a circle.

regular-polygon :: Number, Number, String, String -> Image

| | Use the Contract to write an expression that generates a similar image: |
|---|---|
| | Use the Contract to write an expression that generates a similar image: |
| What changes with the first Number? | |
| What about the shape changes with the second Number? | |
| Use regular-polygon to write an expression for a square! | |
| How would you describe a regular polygon to a friend? | |

Triangle Contracts

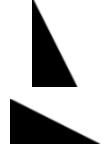
Respond to the questions. Go to <u>code.pyret.org (CPO)</u> to test your code.

1) What kind of triangle does the triangle function produce?

```
There are lots of other kinds of triangles! And Pyret has lots of other functions that make triangles!
triangle :: (size:: Number, style :: String, color :: String) -> Image
right-triangle :: (base::Number, height::Number, style::String, color::String) -> Image
isosceles-triangle :: (leg::Number, angle::Number, style::String, color::String) -> Image
```

2) Why do you think triangle only needs one number, while right-triangle and isosceles-triangle need two numbers and triangle-sas needs three?

3) Write right-triangle expressions for the images below. One argument for each should be 100.



4) What do you think the numbers in right-triangle represent?

5) Write isosceles-triangle expressions for the images below. 1 argument for each should be 100.



6) What do you think the numbers in isosceles-triangle represent?

7) Write 2 expressions that would build **right-isosceles** triangles. Use right-triangle for one expression and isosceles-triangle for the other expression.



Radial Star

radial-star :: (

```
points :: Number,
inner-radius :: Number,
full-radius :: Number,
style :: String,
color :: String
) -> Image
```

Using the detailed Contract above, match each image to the expression that describes it. Go to <u>code.pyret.org (CPO)</u> to test your code.

| Image | | | Expression |
|---------|---|---|---|
| * | 1 | A | radial-star(5, 50, 200, "solid", "black") |
| \star | 2 | В | <pre>radial-star(7, 100, 200, "solid", "black")</pre> |
| | 3 | с | <pre>radial-star(7, 100, 200, "outline", "black")</pre> |
| | 4 | D | <pre>radial-star(10, 150, 200, "solid", "black")</pre> |
| M. | 5 | E | radial-star(10, 20, 200, "solid", "black") |
| * | 6 | F | <pre>radial-star(100, 20, 200, "outline", "black")</pre> |
| * | 7 | G | <pre>radial-star(100, 100, 200, "outline", "black")</pre> |

Diagramming Function Composition

| f :: Number -> Number Consumes a number, multiplies by 3 to produce the result | g :: Number -> Number Consumes a number, adds six to produce the result | |
|--|---|--------------|
| f(x) = 3x | g(x) = x + 6 | h(x) = x - 1 |

For each function composition diagrammed below, translate it into the equivalent Circle of Evaluation for Order of Operations. Then write expressions for *both* versions of the Circles of Evaluation, and evaluate them for x = 4. The first one has been completed for you.

| | Function Composition | Order of Operations | | Translate & Evaluate |
|---|-------------------------|---|--------------------|----------------------|
| | h | - 1 | Composition: | h(g(f(x))) |
| 1 | | $\begin{pmatrix} \star & 6 \\ 3 & \chi & 6 \end{pmatrix}$ | Operations: | ((3 * x) + 6) - 1 |
| | | | Evaluate for x = 4 | h(g(f(4))) = 17 |
| | g f | | Composition: | |
| 2 | | | Operations: | |
| | | | Evaluate for x = 4 | |
| | h | | Composition: | |
| 3 | | | Operations: | |
| | | | Evaluate for x = 4 | |
| | f | | Composition: | |
| 4 | | | Operations: | |
| | | | Evaluate for x = 4 | |

Function Composition — Green Star

1) Draw a Circle of Evaluation and write the Code for a **solid**, **green star**, **size 50**. Go to <u>code.pyret.org (CPO)</u> to test your code. **Circle of Evaluation**:

Code: _____

Using the star described above as the **original**, draw the Circles of Evaluation and write the Code for each exercise below. Test your code in the editor.

| 2) A solid, green star, that is triple the size of the original (using scale) | 3) A solid, green star, that is half the size of the original (using scale) |
|--|--|
| 4) A solid, green star of size 50 that has been rotated 45 degrees counter-clockwise | 5) A solid, green star that is 3 times the size of the original and has been rotated 45 degrees |

Function Composition — Your Name

You'll be investigating these functions with your partner: # text :: String, Number, String -> Image # flip-horizontal :: Image -> Image # flip-vertical :: Image -> Image

frame :: Image -> Image # above :: Image, Image -> Image # beside :: Image, Image -> Image

1) In the editor, write the code to make an image of your name in big letters in a color of your choosing using text. Then draw the Circle of Evaluation and write the Code that will create the image.

Circle of Evaluation for an "image of your name":

Code for an "image of your name":

Using the "image of your name" described above as the **original**, draw the Circles of Evaluation and write the Code for each exercise below. Test your ideas in the editor to make sure they work.

| 2) The framed "image of your name". | 3) The "image of your name" flipped vertically. |
|---|---|
| 4) The "image of your name" above "the image of your name" flipped vertically. | 5) The "image of your name" flipped horizontally beside "the image of your name". |

Function Composition — scale-xy

You'll be investigating these two functions with your partner:

| <pre># scale-xy ::</pre> | (<u>Number</u> , <u>Number</u> , <u>Image</u>) -> Image x-scale-factor y-scale-factor img-to-scale | <pre># overlay :: (<u>Image</u>, <u>Image</u>) -> Image</pre> |
|--------------------------|---|--|
| The Image: | Circle of Evaluation: | Code: |
| \blacklozenge | rhombus 40 90 "solid" "purple" | rhombus(40, 90, "solid", "purple") |

Starting with the image described above, write the Circles of Evaluation and Code for each exercise below. Be sure to test your code in the editor!

| 1) A purple rhombus that is stretched 4 times as wide. | 2) A purple rhombus that is stretched 4 times as tall |
|--|---|
| -, -, -, -, -, -, -, -, -, -, -, -, -, - | -, · · · · · · · · · · · · · · · · · · · |
| | |
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| | |
| | |
| 3) The tall rhombus from #1 overlayed on the wide rhombus (#2). | |
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| | |
| \bigstar Overlay a red rhombus onto the last image you made in #3. | |
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| | | More than one way to Compose an Image! |
|--|------------------------------|--|
| What image will each of the fo the code constructs its image. | ne four expressior age. | What image will each of the four expressions below evaluate to? If you're not sure, go to code.pyret.org.(CPO) and type them into the Interactions Area and see if you can figure out how the code constructs its image. |
| beside(rectangle(| 200, 100, "s | beside(rectangle(200, 100, "solid", "black"), square(100, "solid", "black")) |
| scale-xy(1, 2, square(100, "solid", "black")) | quare(100, "s | solid", "black")) |
| scale(2, rectangl | le(100, 100, | scale(2, rectangle(100, 100, "solid", "black")) |
| above(rectangle(100, 50, "solid", "black"), |), 50, "solid | d", "black"), |
| above(rectangle rectangle | e(200, 100, e(100, 50, "s | e(rectangle(200, 100, "solid", "black"), rectangle(100, 50, "solid", "black"))) |
| For each image below, iden | ntify 2 expression | For each image below, identify 2 expressions that could be used to compose it. The bank of expressions at the top of the page includes one possible option for each image. |
| | | |
| 1 | • | |
| 31 | . 1 | |
| | | |
| | | |
| 2 | | |
| | • | |
| | | |
| | | |
| rn. | | |
| | | |
| | | |
| * | | |
| | | |
| | | |

Defining Values

In math, we use **values** like -98.1, $2/_3$ and 42. In math, we also use **expressions** like 1×3 , $\sqrt{16}$, and 5 - 2. These evaluate to results, and typing any of them in as code produces some answer.

Math also has **definitions**. These are different from values and expressions, because *they do not produce results*. Instead, they simply create names for values, so that those names can be re-used to make the Math simpler and more efficient.

Definitions always have both a name and an expression. The name goes on the left and the value-producing expression goes on the right, separated by an equals sign:

x = 4y = 9 + x

The name is defined to be the result of evaluating the expression. Using the above examples, we get "x is defined to be 4, and y is defined to be 13. **Important: there is no "answer" to a definition**, and typing in a definition as code will produce no result.

Notice that *definitions can refer to previous definitions*. In the example above, the definition of y refers to x. But x, on the other hand, *cannot* refer to y. Once a value has been defined, it can be used in later expressions.

In Pyret, these definitions are written the *exact same way* :

Try typing these definitions into the Definitions Area on the left, clicking "Run", and then using them in the Interactions Area on the right.

x = 4y = 9 + x

Just like in math, definitions in our programming language can only refer to previously-defined values.

Here are a few more value definitions. Feel free to type them in, and make sure you understand them.

x = 5 + 1 y = x * 7 food = "Pizza!" dot = circle(y, "solid", "red")

Defining Values - Explore

Open the Defining Values Starter File and click "Run".

1) What do you Notice?

2) What do you Wonder?

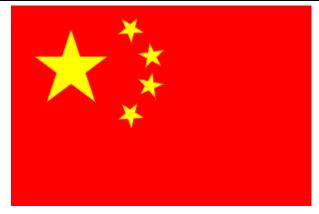
3) Look at the expressions listed below. What do you expect each of them to produce? Write your predictions below, and then test them out one at a time in the Interactions Area.

| ٠ | x |
|---|-----------|
| • | x + 5 |
| | y - 9 |
| • | x * y |
| • | Ζ |
| • | t |
| | gold-star |
| • | my-name |
| • | swamp |
| • | C |
| | |

4) What have you learned about defining values?

5) Define at least 2 more variables in the Definitions Area, click "Run" and test them out. Once you know they're working, record the code you used below.

Defining Values - Chinese Flag



1) What image do you see repeated in the flag?

2) In the code below, highlight or circle all instances of the expression that makes the repeated image.

```
china =
  put-image(
    rotate(40,star(15,"solid","yellow")),
    120, 175,
    put-image(
      rotate(80,star(15,"solid","yellow")),
      140, 150,
      put-image(
        rotate(60,star(15,"solid","yellow")),
        140, 120,
        put-image(
          rotate(40,star(15,"solid","yellow")),
          120, 90,
          put-image(scale(3,star(15,"solid","yellow")),
            60, 140,
            rectangle(300, 200, "solid", "red"))))))
```

3) Write the code to define a value for the repeated expression.

4) Open the Chinese Flag Starter File and click "Run".

- Type china into the Interactions Area and hit Enter.
- Save a copy of the file, and simplify the flag code using the value you defined.
- Click "Run", and confirm that you still get the same image as the original. ٠
- Now change the color of all of the stars to black, in both files.
- Then change the size of the stars.

5) Why is it helpful to define values for repeated images?

★ This file uses a function we haven't seen before! What is it? Can you figure out its Contract? Hint: Focus on the last instance of the function.

1) Complete the table using the first row as an example.

Why Define Values?

2) Write the code to define the value of sunny .

| \rightarrow Use the <i>defined value</i> sunny to simplify! | 3 sunny | <pre>Code: scale(3, sunny)</pre> | ↑ | Code: ↓ | <u> </u> | ellow")) |
|---|--|---|---|--|---|--|
| Original Circle of Evaluation & Code | 3 radial-star 30 20 50 "solid" "yellow" | Code: scale(3, radial-star(30, 20, 50, "solid", "yellow")) | frame radial-star 30 20 50 "solid" "yellow" | Code: frame(radial-star(30, 20, 50, "solid", "yellow")) | leverlay text adial-star "sun" 30 "black" 30 20 50 "solid" "yellow" | Code: overlay(text("sun", 30, "black"), radial-star(30, 20, 50, "solid", "yellow")) |

Which Value(s) Would it Make Sense to Define?

For each of the images below, identify which element(s) you would want to define before writing code to compose the image. *Hint: what gets repeated*?



Writing Code using Defined Values

1) On the line below, write the Code to define PRIZE-STAR as a pink, outline star of size 65.

| Using the <u>PRIZE-STAR</u> definition from above, draw the Circle of Eval Be sure to test out your code in <u>code.pyret.org (CPO)</u> before moving on | |
|---|--|
| 2 The outline of a pink star that is three times the size of the original (using scale) | 3 The outline of a pink star that is half the size of the original (using scale) |
| Circle of Evaluation: | Circle of Evaluation: |
| Code: | Code: |
| 4 The outline of a pink star that is rotated 45 degrees | 5 The outline of a pink star that is three times as big as the original |
| (It should be the same size as the original.) | and has been rotated 45 degrees |
| Circle of Evaluation: | Circle of Evaluation: |

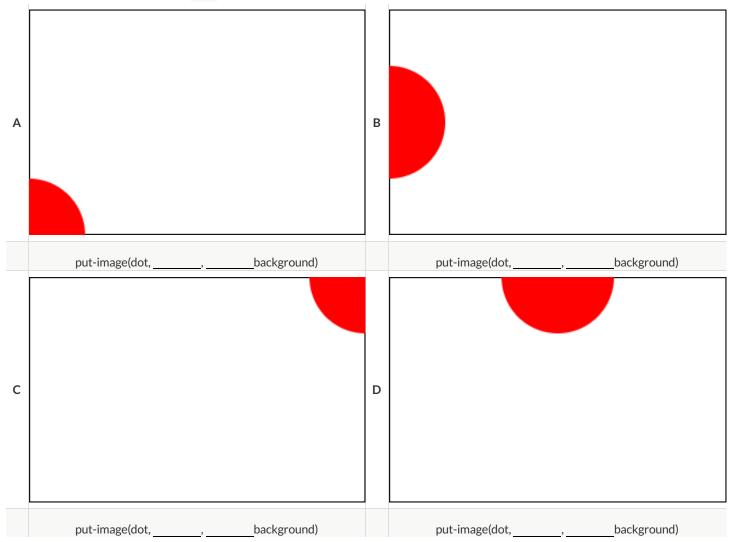
6) How does defining values help you as a programmer?

Estimating Coordinates

dot = circle(50, "solid", "red")
background = rectangle(300, 200, "outline", "black")

Think of the background image as a sheet of graph paper with the origin (0,0) in the bottom left corner. The width of the rectangle is 300 and the height is 200. The numbers in put-image specify a point on that graph paper, where the center of the top image (in this case dot) should be placed.

Estimate: What coordinates for the dot created each of the following images?



Decomposing Flags

Each of the flags below is shown with their width and height. Identify the shapes that make up each flag. Use the flag's dimensions to estimate the dimensions of the different shapes. Then estimate the x and y coordinates for the point at which the center of each shape should be located on the flag. *Hint: The bottom left corner of each flag is at (0,0) and the top right corner is given by the flags dimensions*.

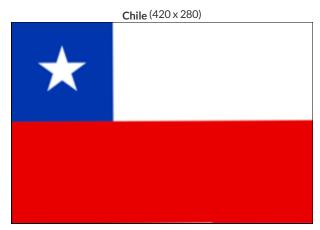


| shape: | color: | width: | height: | х | У |
|--------|--------|--------|---------|---|---|
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |

Panama (300 x 200)



| shape: | color: | width: | height: | х | У |
|--------|--------|--------|---------|---|---|
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |



| shape: | color: | width: | height: | х | у |
|--------|--------|--------|---------|---|---|
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |

Norway (330 × 240)

| shape: | color: | width: | height: | х | у |
|--------|--------|--------|---------|---|---|
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |

Notice and Wonder

As you investigate the <u>Blank Game Starter File</u> with your partner, record what you Notice, and then what you Wonder. *Remember*, "Notices" are statements, not questions.

 What do you Notice?
 What do you Wonder?

The Great gt domain debate!

Kermit: The domain of gt is Number, String, String.

Oscar: The domain of gt is Number.

Ernie: I'm not sure who's right!

In order to make a triangle, we need a size, a color and a fill style...

but all we had to tell our actor was gt(20) ...and they returned triangle(20, "solid", "green").

Please help us!

1) What is the correct domain for gt?

2) What could you tell Ernie to help him understand how you know?

Let's Define Some New Functions!

1) Let's define a function rs to generate solid red squares of whatever size we give them!

If I say rs(5), what would our actor need to say?

| Let's write a few more examples: | |
|---|-----|
| $rs(\underline{\hspace{0.5cm}}) \rightarrow \underline{\hspace{0.5cm}}$ | |
| rs()→ | |
| $rs(\underline{)} \rightarrow $ | |
| What changes in these examples? Name your variable(s): Let's define our function using the variable: | |
| fun rs(): | end |
| 2) Let's define a function bigc to generate big solid circles of size 100 in whatever color we give them! If I say bigc("orange"), what would our actor need to say? | |
| Let's write a few more examples: | |
| bigc() \rightarrow | |
| bigc() \rightarrow | |
| bigc()→ | L |
| What changes in these examples? Name your variable(s): Let's define our function using the variable: | |
| fun bigc(): | end |
| 3) Let's define a function ps to build a pink star of size 50, with the input determining whether it's solid or outline! If I say ps("outline"), what would our actor need to say? | |
| Write examples for all other possible inputs: | |
| ps()→ | |
| $ps(_) \rightarrow$ | |
| What changes in these examples? Name your variable(s): | |
| fun ps(): | end |

4) Add these new function definitions to your $\underline{\mathsf{gt}\,\mathsf{Starter}\,\mathsf{File}}$ and test them out!

Let's Define Some More New Functions!

1) Let's define a function sun to write SUNSHINE in whatever color and size we give it!

If I say sun(5, "blue"), what would our actor need to say?

| Let's write a few more ex | nples: |
|---|--|
| sun(, | $) \rightarrow$ |
| sun(, |)→ |
| sun(, | $) \rightarrow$ |
| What changes in these ex Let's define our function | mples? Name your variable(s): |
| fun sun(| ,): |
| | end |
| | me to generate your name in whatever size and color we give it!), what would our actor need to say? |
| Let's write a few more ex | nples: |
| me(, | $) \rightarrow$ |
| me(, | $) \rightarrow$ |
| me(, | $) \rightarrow$ |
| What changes in these ex Let's define our function | mples? Name your variable(s): |
| fun me(| ,); |
| | end |
| | gr to build a solid, green rectangle of whatever height and width we give it! at would our actor need to say? |
| Let's write a few more ex | nples: |
| $gr(\underline{\qquad}, \underline{\qquad}) \rightarrow rect$ | ngle(,, "solid", "green") |
| $gr(\underline{\qquad}, \underline{\qquad}) \rightarrow rect$ | ngle(,, "solid", "green") |
| $gr(\underline{\qquad},\underline{\qquad}) \rightarrow rect$ | ngle(,, "solid", "green") |
| What changes in these ex Let's define our function | mples? Name your variable(s): |
| fun gr(| ,): |

4) Add these new function definitions to your <u>gt Starter File</u> and test them out!

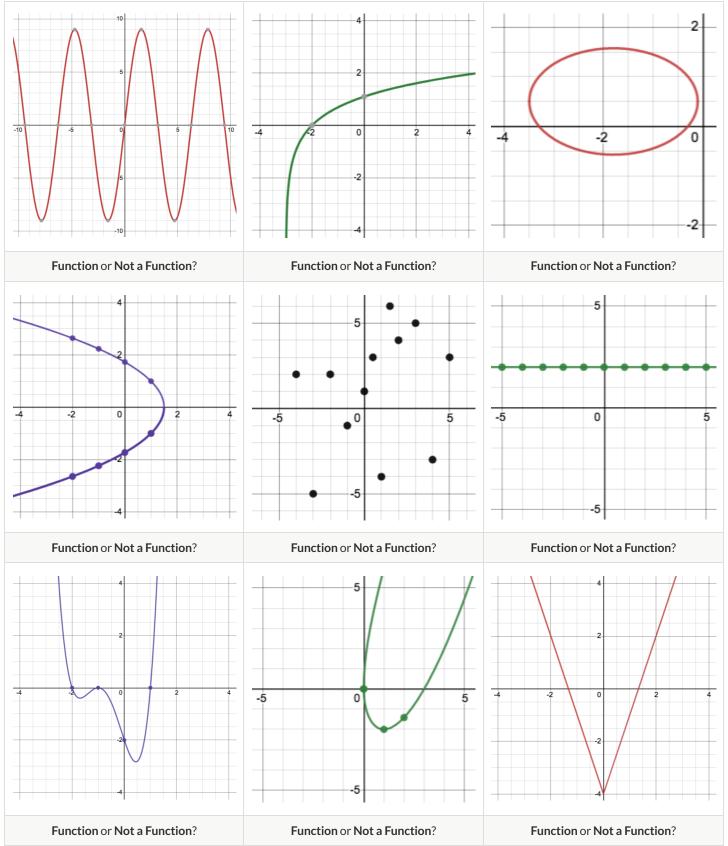
Describe and Define Your Own Functions!

| 1) Let's define a function | n | to generate | | |
|---------------------------------------|--------------------|--------------------------|---|-------|
| If I say | , what woul | d our actor need to say? | | |
| Let's write a few more ex | xamples: | | | |
| (| $) \rightarrow$ | (|) | |
| | | (| | |
| (| $) \rightarrow$ | _(|) | |
| What changes in these e | examples? Name ye | our variable(s): | | |
| Let's define our function | | | | |
| | - | (| |) end |
| 2) Let's define a functio | n | to generate | | |
| lf I say | , what woul | d our actor need to say? | | |
| Let's write a few more ex | xamples: | | | |
| | $) \rightarrow$ | (|) | |
| | | (| | |
| (| $) \rightarrow$ | ((|) | |
| What changes in these e | examples? Name ye | our variable(s): | | |
| Let's define our function | | | | |
| | - | (| |)end |
| 3) Let's define a functio | | | | |
| If I say Let's write a few more ex | | d our actor need to say? | | |
| (|) → | (|) | |
| (|) → | |) | |
| | $) \rightarrow$ | (|) | |
| What changes in these e | examples? Name ye | our variable(s): | | |
| Let's define our function | using the variable | | | |
| | - | (| |)end |

4) Add your new function definitions to your <u>gt Starter File</u> and test them out!

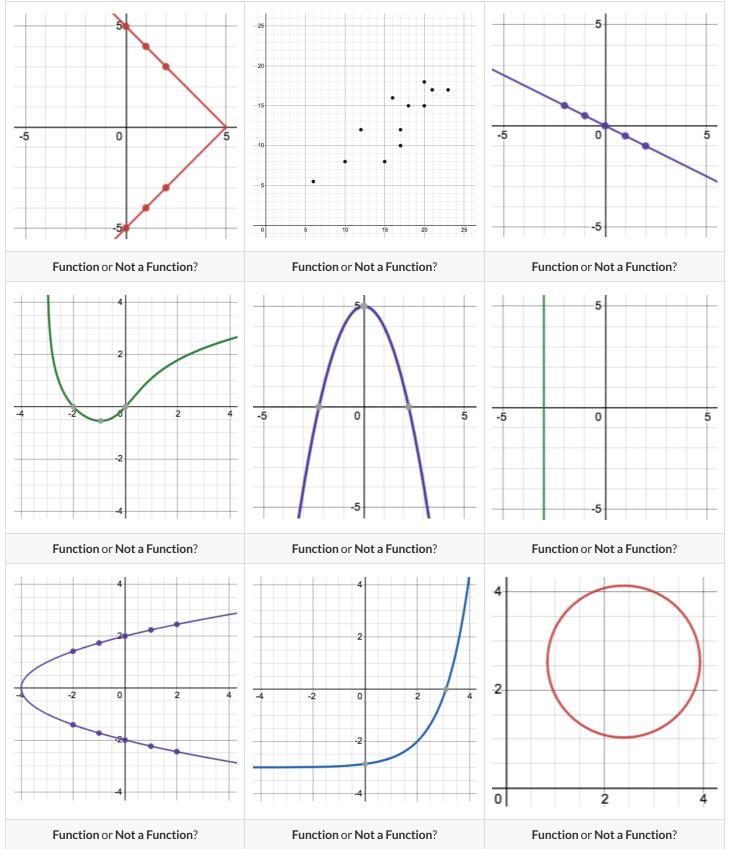
Identifying Functions from Graphs

Decide whether each graph below is a function. If it's not, prove it by drawing a vertical line that crosses the plot at more than one point.



Identifying Functions from Graphs (2)

Decide whether each graph below is a function. If it's not, prove it by drawing a vertical line that crosses the plot at more than one point.



Notice and Wonder - Functions

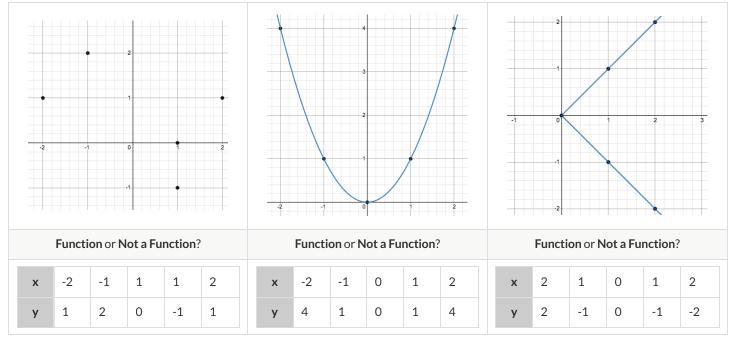
Write down what you Notice and Wonder about the graphs you've just seen. At a later point you will *also* use this page to record what you Notice and Wonder about the tables you'll see. *Remember: "Notices" should be statements, not questions!*

What do you Notice?

What do you Wonder?

How Tables Fail the Vertical Line Test

1) Each of the graphs below is also represented by a table. Use the vertical line test to determine whether or not each graph represents a function.



2) For each graph that failed the vertical line test, label the offending points with their coordinates.

3) Find the same coordinates in the table below the graph and circle or highlight them.

4) What do the tables of the non-functions have in common? What could you look for in other tables to identify whether or not they could represent a function?

5) Use the process you just described to determine whether each table below could represent a function. Circle or highlight the points that would end up on the same vertical line.

| x | У | x | У | x | у | x | у |
|----------|---------|----------|---------|----------|-----------|----------|-----------|
| 0 | -2 | 0 | -2 | 0 | 3 | 1 | 0 |
| 1 | -2 | 1 | 1 | 1 | 4 | 0 | 1 |
| 2 | -2 | 2 | 4 | -1 | 5 | 1 | 2 |
| 3 | -2 | 3 | 7 | 2 | 6 | 2 | 3 |
| 4 | -2 | 3 | 10 | -2 | 7 | 3 | 4 |
| Function | or Not? | Function | or Not? | Function | n or Not? | Function | n or Not? |

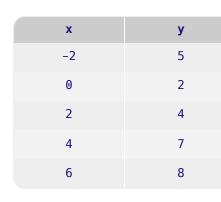
Identifying Functions from Tables

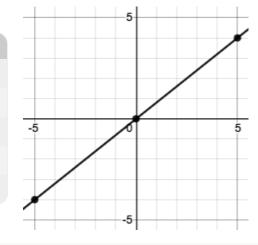
Decide whether or not each table below could represent a function. If not, circle what you see that tells you it's not a function. In a function, there is exactly one y-value (or output) for each x-value (or input). If a table has more than one y-value (or output) for the same x-value (or input), it can not represent a function.

| x | У | x | У | input | output | x | У |
|----------|-------------------|----------|-----------|----------|-----------|----------|-------------------|
| 0 | 3 | 5 | 3 | 0 | 2 | 1 | 0 |
| 1 | 2 | 1 | 4 | 5 | 2 | 1 | 1 |
| 2 | 5 | -3 | 5 | 2 | 2 | 1 | 2 |
| 3 | 6 | 3 | 6 | 6 | 2 | 1 | 3 |
| 4 | 5 | 2 | 7 | 3 | 2 | 1 | 4 |
| Functior | n or Not ? | Function | n or Not? | Function | n or Not? | Function | n or Not ? |
| tickets | \$ | input | output | x | у | C | F |
| 2 | 0 | -4 | -2 | 10 | 9 | -40 | -40 |
| 1 | 2 | -3 | -1 | 3 | 2 | 0 | 32 |
| 2 | 4 | -2 | 0 | 9 | 8 | 10 | 50 |
| 3 | 6 | -1 | 1 | 17 | 16 | 37 | 98.6 |
| 4 | 8 | 0 | 2 | 3 | 5 | 100 | 212 |
| Function | or Not? | Function | or Not? | Functio | n or Not? | Function | n or Not ? |
| input | output | \$ | games | x | у | miles | minutes |
| 0 | 7 | 10 | 5 | 8 | 10 | 0 | 0 |
| -1 | 2 | 11 | 25 | 6 | 5 | 1 | 2 |
| 4 | 3 | 12 | 45 | 4 | 0 | 2 | 4 |
| 8 | 6 | 13 | 65 | 6 | -5 | 3 | 6 |
| -5 | -8 | 14 | 85 | 8 | -10 | 4 | 8 |
| Function | n or Not? | Function | or Not? | Function | n or Not? | Function | n or Not? |

Identifying Functions from Tables & Graphs

Decide whether or not each table or graph below could represent a function. If not, circle what tells you it's not a function. In a function, there is exactly one y-value for each x-value. If a table or graph has more than one y-value for the same x-value, it can not represent a function.





 x
 y

 0
 7

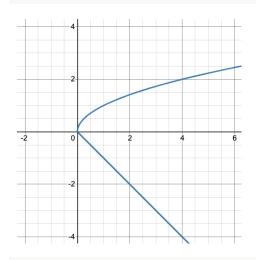
 1
 2

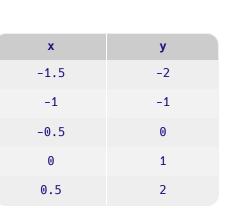
 1
 3

 2
 6

 3
 -8

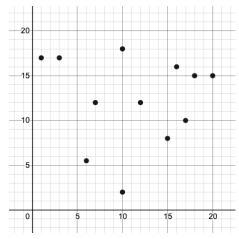
Function or Not a Function?





Function or Not a Function?

Function or Not a Function?



Function or Not a Function?

 x
 y

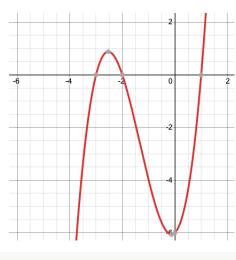
 -1
 1.5

 0
 1.5

 1
 1.5

 2
 1.5

 3
 1.5



Function or Not a Function?

Function or Not a Function?

| x | У |
|---|---|
| 8 | 1 |
| 5 | 2 |
| 4 | 3 |
| 5 | 4 |
| 8 | 5 |
| | |

Function or Not a Function?

Function or Not a Function?

Function or Not a Function?

Matching Examples and Definitions (Math)

Match each of the function definitions on the left with the corresponding table on the right.

It may help to circle or highlight what's changing in the f(x) column of the table!

f(x) = 1 - 2x

f(x) = 2 + x

| Function Definitions | | | Example Tables | |
|-----------------------------|---|---|-----------------------|-------|
| | | | | |
| | | | x | f(x) |
| | | | 1 | 2 × 1 |
| f(x) = x - 2 | 1 | A | 2 | 2 × 2 |
| | | | 3 | 2×3 |

| | <u>,</u> | 2 | 15 | 15 – 2 | |
|-----------|----------|---|----|--------|--|
| f(x) = 2x | 2 | В | 25 | 25 – 2 | |
| | | | 35 | 35 - 2 | |

D

Е

| | 2 | <u> </u> | |
|---------------|---|----------|--|
| f(x) = 2x + 1 | 3 | C | |
| | | | |

4

5

| x | $f(\mathbf{x})$ |
|----|-----------------|
| 10 | 2 + 10 |
| 15 | 2 + 15 |
| 20 | 2 + 20 |

x

f(x)

| x | f(x) |
|---|----------|
| 0 | 1 – 2(0) |
| 1 | 1 – 2(1) |
| 2 | 1 – 2(2) |

| x | f(x) |
|----|-----------|
| 10 | 2(10) + 1 |
| 20 | 2(20) + 1 |
| 30 | 2(30) + 1 |

Function Notation - Substitution

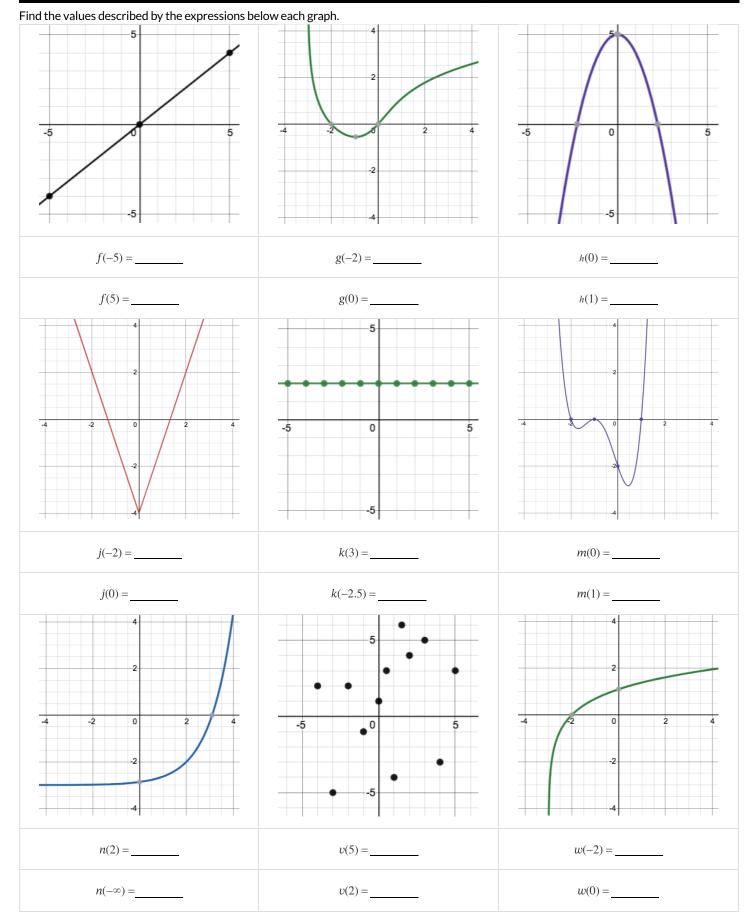
Complete the table below, by substituting the given value into the expression and evaluating.

| Function Definition | Expression | Substitution | Evaluates to |
|---------------------|--------------|--------------|--------------|
| f(x) = x + 2 | <i>f</i> (3) | 3 + 2 | 5 |
| g(x) = x - 1 | g(6) | | |
| h(x) = 3x | h(4) | | |
| k(x) = 2x - 1 | k(5) | | |

Now that you understand how to evaluate an expression, let's get some more practice! The table below includes four different functions. Beneath each of them are a collection of different expressions to evaluate.

| m(x) = -2x + 3 | n(x) = -x + 7 | v(x) = 10x - 8 | $w(x) = x^2$ |
|------------------|----------------|------------------|-----------------|
| m(3) = -2(3) + 3 | <i>n</i> (5) = | <i>v</i> (7) = | w(-2) = |
| -3 | | | |
| <i>m</i> (-4) = | n(-2) = | <i>v</i> (0) = | <i>w</i> (10) = |
| | | | |
| <i>m</i> (0) = | n(3.5) = | <i>v</i> (-10) = | <i>w</i> (0) = |
| | | | |
| <i>m</i> (0.5) = | <i>n</i> (0) = | v(2.5) = | w(1.5) = |
| | | | |
| What do y | ou Notice? | What do yo | ou Wonder? |

Function Notation - Graphs



Function Notation - Tables

Find the values described by the expressions below each table. Note: not all of the relationships here are actually functions!

| x | f(x) | x | g (x) | x | $h(\mathbf{x})$ | x | y (x) |
|-----------------|-----------------------|-----------------|-----------------------|-----------------|-----------------------|-----------------|-----------------------|
| 0 | 0 | 5 | 3 | 0 | 2 | 1 | 0 |
| 1 | 2 | 1 | 4 | 5 | 2 | 1 | 1 |
| 2 | 4 | -3 | 5 | 2 | 2 | 1 | 2 |
| 3 | 6 | 3 | 6 | 6 | 2 | 1 | 3 |
| 4 | 8 | 2 | 7 | 3 | 2 | 1 | 4 |
| | | | | | | | |
| <i>f</i> (3) = | | g(1) = | | h(0) = | | <i>y</i> (1) = | |
| 6 (4) | | | | | | | |
| f(4) = | | g(3) = | | h(3) = | | y(8) = | |
| a | <i>b</i> (<i>a</i>) | с | <i>d</i> (<i>c</i>) | n | <i>m</i> (<i>n</i>) | q | n(a) |
| -4 | -2 | 0 | 3 | 0 | 0 | 2 2 | <i>p(q)</i> 0 |
| -4 | -2 | 1 | 2 | -1 | -1 | 1 | 2 |
| -2 | -1 | 2 | | -1 | -1 -2 | 2 | |
| -2 | 1 | 3 | 6 | -2 | | 3 | 6 |
| -1 | 2 | 4 | 5 | -3 | | 4 | 8 |
| U | 2 | 4 | J | -4 | -4 | 4 | 0 |
| | | | | | | | |
| <i>b</i> (-1) = | | d(2) = | | <i>m</i> (0) = | | <i>p</i> (1) = | |
| <i>b</i> (0) = | | d(4) = | | <i>m</i> (-3) = | | p(2) = | |
| | | | | | | | |
| S | r (s) | w | v (w) | у | z(y) | time | l(time) |
| 0 | 7 | 10 | 5 | 8 | 10 | 10 | 9 |
| -1 | 2 | 11 | 25 | 6 | 5 | 3 | 2 |
| 4 | 3 | 12 | 45 | 4 | 0 | 9 | 8 |
| 8 | 6 | 13 | 65 | 5 | -5 | 17 | 16 |
| -5 | -8 | 14 | 85 | 8 | -10 | 5 | 5 |
| | | | | | | | |
| <i>r</i> (-1) = | | v(11) = | | 7(6) - | | l(10) = | |
| r(-1) - | | U(11) = | | <i>z</i> (6) = | | <i>l</i> (10) = | |
| <i>r</i> (8) = | | <i>v</i> (14) = | | <i>z</i> (2) = | | <i>l</i> (3) = | |

Defining Functions

Functions can be viewed in *multiple representations*. You already know one of them: *Contracts*, which specify the Name, Domain, and Range of a function. Contracts are a way of thinking of functions as a *mapping* between one set of data and another. For example, a mapping from Numbers to Strings:

f :: Number -> String

Another way to view functions is with *Examples*. Examples are essentially input-output tables, showing what the function would do for a specific input:

In our programming language, we focus on the last two columns and write them as code:

```
examples:
f(1) is 1 + 2
f(2) is 2 + 2
f(3) is 3 + 2
f(4) is 4 + 2
end
```

Finally, we write a formal **function definition** ourselves. The pattern in the Examples becomes *abstract* (or "general"), replacing the inputs with *variables*. In the example below, the same definition is written in both math and code:

f(x) = x + 2fun f(x): x + 2 end

Look for connections between these three representations!

- The function name is always the same, whether looking at the Contract, Examples, or Definition.
- The number of inputs in the Examples is always the same as the number of types in the Domain, which is always the same as the number of variables in the Definition.
- The "what the function does" pattern in the Examples is almost the same in the Definition, but with specific inputs replaced by variables.

| Examples | | | Contract |
|--|---|---|--------------------------------|
| examples: f(5) is 5 / 2 f(9) is 9 / 2 f(24) is 24 / 2 end | 4 | Þ | #f::Number -> Number |
| <pre>examples: f(1) is rectangle(1, 1, "outline", "red") f(6) is rectangle(6, 6, "outline", "red") end</pre> | N | B | # f :: String -> Image |
| <pre>examples: f("pink", 5) is star(5, "solid", "pink") f("blue", 8) is star(8, "solid", "blue") end</pre> | ω | 0 | #f::Number → Image |
| <pre>examples: f("Hi!") is text("Hi!", 50, "red") f("Ciao!") is text("Ciao!", 50, "red") end</pre> | 4 | D | # f :: Number, String -> Image |
| <pre>examples: f(5, "outline") is star(5, "outline", "yellow") f(5, "solid") is star(5, "solid", "yellow") end</pre> | ч | m | # f :: String, Number -> Image |

Matching Examples and Function Definitions

Find the variables in gt and label them with the word "size".

examples:

end

gt(20) is triangle(20, "solid", "green")
gt(50) is triangle(50, "solid", "green")

gr(Ju) is rrangre(Ju, sorra, green

fun gt(size): triangle(size, "solid", "green") end

Highlight and label the variables in the example lists below. Then, using gt as a model, match the examples to their corresponding function definitions.

Examples Definition examples: f("solid") is circle(8, "solid", "red") fun f(s): star(s, "outline", "red") end Α 1 f("outline") is circle(8, "outline", "red") end examples: f(2) is 2 + 2 f(4) is 4 + 4 2 В fun f(num): num + num end f(5) **is** 5 + 5 end examples: f("red") is circle(7, "solid", "red") fun f(c): star(9, "solid", c) end С 3 f("teal") is circle(7, "solid", "teal") end examples: f("red") is star(9, "solid", "red") f("grey") is star(9, "solid", "grey") fun f(s): circle(8, s, "red") end 4 D f("pink") is star(9, "solid", "pink") end examples: f(3) is star(3, "outline", "red") fun f(c): circle(7, "solid", c) end Е 5 f(8) is star(8, "outline", "red") end

Creating Contracts From Examples

Write the contracts used to create each of the following collections of examples. The first one has been done for you.

```
1) # big-triangle :: Number, String -> Image
```

```
examples:
    big-triangle(100, "red") is triangle(100, "solid", "red")
    big-triangle(200, "orange") is triangle(200, "solid", "orange")
end
```

2)

```
examples:
    purple-square(15) is rectangle(15, 15, "outline", "purple")
    purple-square(6) is rectangle(6, 6, "outline", "purple")
end
```

3)

```
examples:
   banner("Game Today!") is text("Game Today!", 50, "red")
   banner("Go Team!") is text("Go Team!", 50, "red")
   banner("Exit") is text("Exit", 50, "red")
end
```

4)

```
examples:
   twinkle("outline", "red") is star(5, "outline", "red")
   twinkle("solid", "pink") is star(5, "solid", "pink")
   twinkle("outline", "grey") is star(5, "outline", "grey")
end
```

Contracts, Examples & Definitions - bc

gt

Directions: Define a function called gt, which makes solid green triangles of whatever size we want.

Every contract has three parts...

| # | gt:: | | | Numi | ber | | -> | Image |
|---------------|------------------|-----------------|----------------|----------------------|----------------|----------------------------|----|-------|
| function na | me | | | Dom | nain | | | Range |
| Write some | examples, the | en circle and l | label what ch | anges | | | | |
| examples: | | | | | | | | |
| | <u>gt(</u> | 10 |) i: | triangle(10, ' | "solid", | "green") | | |
| function | name | input(s) | | | | what the function produces | | |
| | gt(| 20 |) i: | triangle(20, ' | "solid", | "green") | | |
| function | name | input(s) | | | | what the function produces | | |
| end | | | | | | | | |
| Write the d | efinition, givir | ng variable na | ames to all yo | ur input values | | | | |
| fun | at(| | size |). | | | | |
| | on name | | variable(s) |). | | | | |
| <u>triang</u> | le(size, | "solid", | "green") | | | | | |
| _ | | | | what the function of | does with thos | e variable(s) | | |

end

bc

Directions: Define a function called bc, which makes solid blue circles of whatever radius we want.

| Every contract has three parts |
|--------------------------------|
|--------------------------------|

| # | | :: | | | | -> |
|----------|-------------------------|-----------------------------|---------------------|-------------------|----------------------------|-------|
| | function name | | | Domain | | Range |
| Write so | ome examples, then cir | cle and label what change | 25 | | | |
| exampl | es: | | | | | |
| | | (|)is | | | |
| | function name | input(s) | | | what the function produces | |
| | | (|) is | | | |
| _ | function name | input(s) | | | what the function produces | |
| end | | | | | | |
| Write th | e definition, giving va | riable names to all your in | put values | | | |
| fun | | (| |): | | |
| | function name | Va | riable(s) | | | |
| | | | what the function d | and with those we | riable/c) | |

end

what the function does with those variable(s)

Contracts, Examples & Definitions - Stars

sticker

Directions: Define a function called sticker, which consumes a color and draws a 50px solid star of the given color.

| Every c | contract has three parts | | | | | |
|---------|-----------------------------------|-------------------------------|----------------------------------|-----------------------------|---|-------|
| # | function name | | Domain | | > | Range |
| Write s | some examples, then circle and | label what changes | Bonian | | | Range |
| examp | | 0 | | | | |
| | (|) is | | | | |
| | function name | input(s) | | what the function produces | | |
| | (|) is | | what the function was done. | | |
| end | function name | input(s) | | what the function produces | | |
| Write t | the definition, giving variable n | ames to all your input values | 5 | | | |
| fun | function name | variable(s) |): | | | |
| | | | | | | |
| - | | what the fu | unction does with those variable | e(s) | | |
| end | | | | | | |

gold-star

Directions: Define a function called gold-star, which takes in a radius and draws a solid gold star of that given size.

Every contract has three parts...

| # | :: | | | -> |
|------------------------------|----------------------------------|-----------------------------|----------------------------|-------|
| function name | | Domain | | Range |
| Write some examples, then | circle and label what changes | | | |
| examples: | | | | |
| • | | | | |
| | (|)is | | |
| function name | input(s) | | what the function produces | |
| | , | . . | | |
| | (|) is | | |
| function name | input(s) | | what the function produces | |
| end | | | | |
| Write the definition, giving | variable names to all your input | values | | |
| | | | | |
| fun | (|): | | |
| function name | variable | e(s) | | |
| | | | | |
| | | | | |
| | what | the function does with thos | e variable(s) | |

end

Contracts, Examples & Definitions - Name

name-color

Directions: Define a function called name-color, which makes an image of your name at size 50 in whatever color is given.

| Every contract has three parts | | | |
|---------------------------------------|---------------------------------|------------------------------------|----------|
| <u>#:</u> | | | > |
| function name | | Domain | Range |
| Write some examples, then circle ar | d label what changes | | |
| examples: | | | |
| (|) is | | |
| function name | input(s) | what the function | produces |
| (|) is | | |
| function name | input(s) | what the function | produces |
| end | | | |
| Write the definition, giving variable | names to all your input values. | | |
| fun(| variable(s) |): | |
| | 14.142.10(6) | | |
| | what the fur | nction does with those variable(s) | |

end

name-size

Directions: Define a function called name-size, which makes an image of your name in your favorite color (be sure to specify your name and favorite color!) in whatever size is given.

| Every contract has three parts. | | | | | |
|---|------------------------------|-------------------------|----------------------|-------------------|-------|
| <u>#:</u> : | : | | | | > |
| function name Write some examples, then circ | cle and label what changes | | main | | Range |
| examples: | | | | | |
| | (|) is | | | |
| function name | input(s) | | what the | function produces | |
| function name | (input(s) |) is | what the | function produces | |
| end | mput(s) | | what the | function produces | |
| Write the definition, giving var | iable names to all your inpu | t values | | | |
| fun | (varial | | _): | | |
| function name | Varia | 016(2) | | | |
| | wh | at the function does wi | th those variable(s) | | |

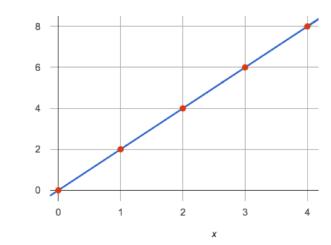
end

Notice and Wonder (Linearity)

>

Part 1:

| x | У |
|---|---|
| 0 | 0 |
| 1 | 2 |
| 2 | 4 |
| 3 | 6 |
| 4 | 8 |



| What do you Notice? | What do you Wonder? |
|---------------------|---------------------|
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| Danit de | |

Part 2:

- What would be the next (x,y) pair for each of the tables?
- What would the y-value for each table be when x is 0?

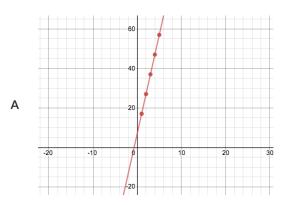
| x | У |
|---|---|
| 0 | |
| 1 | 2 |
| 2 | 3 |
| 3 | 4 |
| 4 | 5 |
| 5 | 6 |

| x | у |
|---|----|
| 0 | |
| 1 | 20 |
| 2 | 17 |
| 3 | 14 |
| 4 | 11 |
| 5 | 8 |

Matching Tables to Graphs

For each of the tables below, find the graph that matches.

Note: Scales on the graphs vary. The tables are shown sideways to save space.



| х | -5 | -4 | -3 | -2 | -1 |
|---|----|----|----|----|----|
| у | 5 | 4 | 3 | 2 | 1 |

| х | 1 | 2 | 3 | 4 | 5 | |
|---|----|----|----|----|----|--|
| у | 17 | 27 | 37 | 47 | 57 | |

3

4

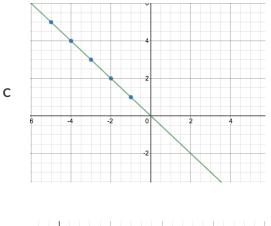
1

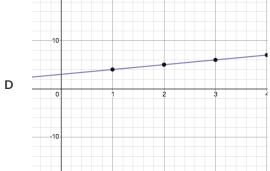
2

| x | -2 | -1 | 0 | 1 | 2 |
|---|----|----|---|---|---|
| у | -6 | -3 | 0 | 3 | 6 |

-10

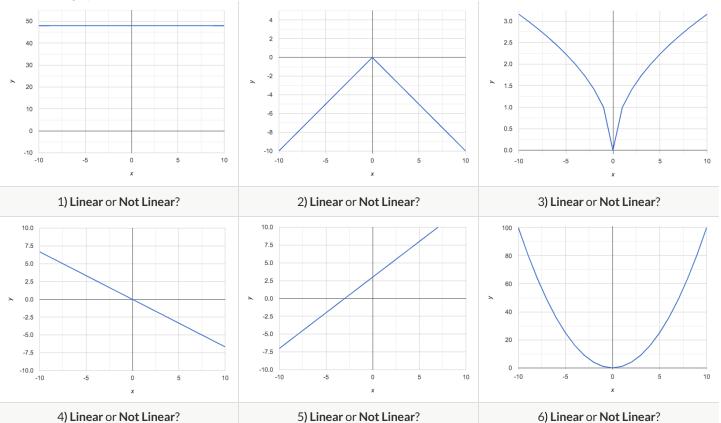
В





Are All Graphs Linear?

If all linear relationships can be shown as points on a graph, does that mean all graphs are linear? Beneath each graph circle **Linear** or **Not Linear**.



What do you Notice?

What do you Wonder?

Are All Tables Linear?

If all linear relationships can be shown as tables, does that mean all tables are linear? Look at the six tables shown below.

1) Extend as many of the tables as you can by adding the next (x,y) pair in the sequence.

2) If the table is linear, write down your prediction of what the y-value will be when x = 0.

3) If the table is not linear, write **not linear** instead of an answer for y.

| Α | | | | | В | | | | | | | | |
|---|----|----|----|----|----|--|---|-----|-----|-----|-----|-----|--|
| x | -2 | -1 | 0 | 1 | 2 | | x | 2 | 3 | 4 | 5 | 6 | |
| У | -2 | -3 | -4 | -5 | -6 | | У | -12 | -14 | -16 | -18 | -20 | |

when x=0, y will equal

when x=0, y will equal

| x 1 2 3 4 5 y 1 4 9 16 25 | С | | | | | | | |
|---|---|---|---|---|---|----|----|--|
| y 1 4 9 16 25 | | x | 1 | 2 | 3 | 4 | 5 | |
| | | у | 1 | 4 | 9 | 16 | 25 | |

| D | | | | | | |
|---|---|---|---|---|---|--|
| х | 5 | 6 | 7 | 8 | 9 | |
| У | 3 | 3 | 3 | 3 | 3 | |

when x=0, y will equal _____

| E | | | | | | |
|---|----|----|-----|-----|-----|--|
| x | 1 | 2 | 3 | 4 | 5 | |
| у | 84 | 94 | 104 | 114 | 124 | |

| F | | | | | | |
|---|-------|------------------|------|------|------|--|
| х | -10 | -9 | -8 | -7 | -6 | |
| У | -1/10 | -1/ ₉ | -1/8 | -1/7 | -1/6 | |

when x=0, y will equal _____

when x=0, y will equal _____

when x=0, y will equal

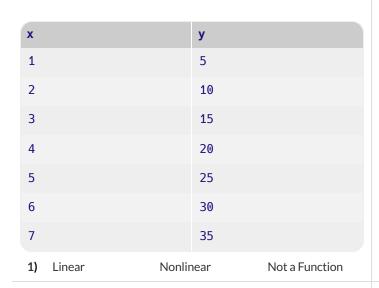
| What do you Notice? | What do you Wonder? |
|---------------------|---------------------|
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |

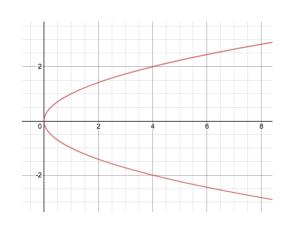
Linear, Non-linear, or Bust?

2)

Linear

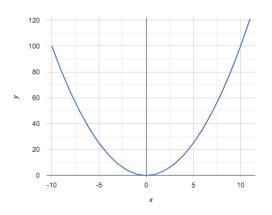
Circle whether each representation is of a linear function, a nonlinear function or is not a function at all! Remember: Functions will pass the Vertical Line Test!





Nonlinear

Not a Function

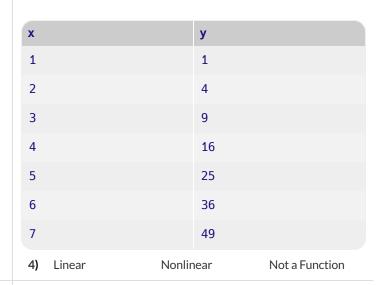


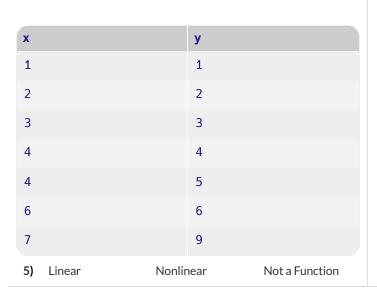
Nonlinear

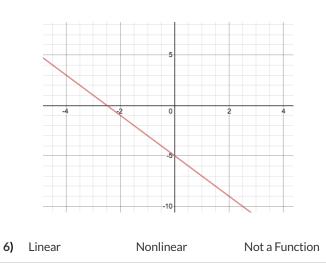
3)

Linear

Not a Function







Slope & y-Intercept from Tables (Intro)

slope (rate): how much y changes as x-increases by 1

| y-intercept : the y-value when $x = 0$ | | | | | | |
|--|--|--|--|--|--|--|
| x -1 0 1 2 3 4 | | | | | | |
| y -1 11 33 55 77 9 | | | | | | |
| 1) Compute the slope: | | | | | | |
| 3) What strategies did you use to compute the slope and y-intercept? | | | | | | |
| | | | | | | |

The slope and y-intercept in this table are harder to find, because the x-values don't go up by 1 and we can't see a value for x = 0. Try filling in the points that have been skipped to compute the slope and y-intercept.

| x | 2 | 5 | 8 | 11 | | | |
|-------------------------|---|---|----|----|--|--|--|
| У | 3 | 9 | 15 | 21 | | | |
| 4) Compute the slope: 2 | | | | | | | |

The slope and y-intercept in this table are even harder to find, because the x-values are out of order! Calculate the slope and y-intercept from any two points! Be sure to show your work.

| x | 3 | 20 | 5 | 9 | 1 |
|---|---|----|----|----|----|
| У | 5 | 56 | 11 | 23 | -1 |

6) Compute the slope: _____

7) Compute the y-intercept: _____

⁵⁾ Compute the y-intercept: _____

Slope & y-Intercept from Tables (Practice)

| | x | -1 | 0 | 1 | 2 | 3 | 4 |
|------------------------|------------------------|----|------|-----------|------|----------|------|
| | у | -1 | 2 | 5 | 8 | 11 | 14 |
| 1) slope: | 1) slope: y-intercept: | | | | | | |
| | | | | | | | |
| | x | -2 | -1 | 0 | 1 | 2 | 3 |
| | у | 15 | 10 | 5 | 0 | -5 | -10 |
| 2) slope: | 2) slope: y-intercept: | | | | | | |
| _, stope | | | | | | | |
| | x | -3 | -2 | -1 | 0 | 1 | 2 |
| | у | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 |
| a) i | | | | | | | |
| 3) slope: | | | y-ir | itercept: | | | |
| | x | -1 | 0 | 1 | 2 | 3 | 4 |
| | | | | | | | |
| | У | -7 | -3 | 1 | 5 | 9 | 13 |
| 4) slope: y-intercept: | | | | | | | |
| | | 1 | | | | | |
| | x | -5 | -4 | -3 | -2 | -1 | 0 |
| | у | 1 | 2.5 | 4 | 5.5 | 7 | 8.5 |
| 5) slope: | | | y-ir | ntercent. | | | |
| 5/ Slope. | | | y ii | | | | |
| | x | -3 | -2 | -1 | 0 | 1 | 2 |
| | у | 0 | 12.5 | 25 | 37.5 | 50 | 62.5 |
| | | | | | | | |
| 6) slope: y-intercept: | | | | | | | |
| | x | 1 | 2 | 3 | 4 | 5 | 6 |
| | у | 5 | 3 | 1 | -1 | -3 | -5 |
| | | | | | | | |
| 7) slope: | | | y-ir | ntercept: | | | |
| | x | -4 | -2 | 0 | 2 | 4 | 6 |
| | у | 0 | 4 | 8 | 12 | 16 | 20 |
| 8) slope. | | | v-ir | ntercept: | | | |
| c, c. opc. | | | ; ii | | | <u> </u> | |

Identifying Slope in Tables

Can you identify the **slope** for the functions represented in each of these tables? Note: Some tables may have their rows out of order!

| | Х | у |
|---|---|---|
| | 0 | 3 |
| 1 | 1 | 5 |
| | 2 | 7 |
| | 3 | 9 |

| | Х | у |
|---|----|----|
| | -5 | 35 |
| 2 | -4 | 28 |
| | -3 | 21 |
| | -2 | 14 |

| | х | у |
|---|----|------|
| | 12 | 15 |
| 3 | 13 | 15.5 |
| | 14 | 16 |
| | 16 | 17 |

| | Х | У |
|---|---|----|
| | 1 | 39 |
| 4 | 4 | 36 |
| | 3 | 37 |
| | 2 | 38 |

| | Х | У |
|---|----|----|
| | 13 | 57 |
| 5 | 9 | 41 |
| | 11 | 49 |
| | 7 | 33 |

slope/rate:

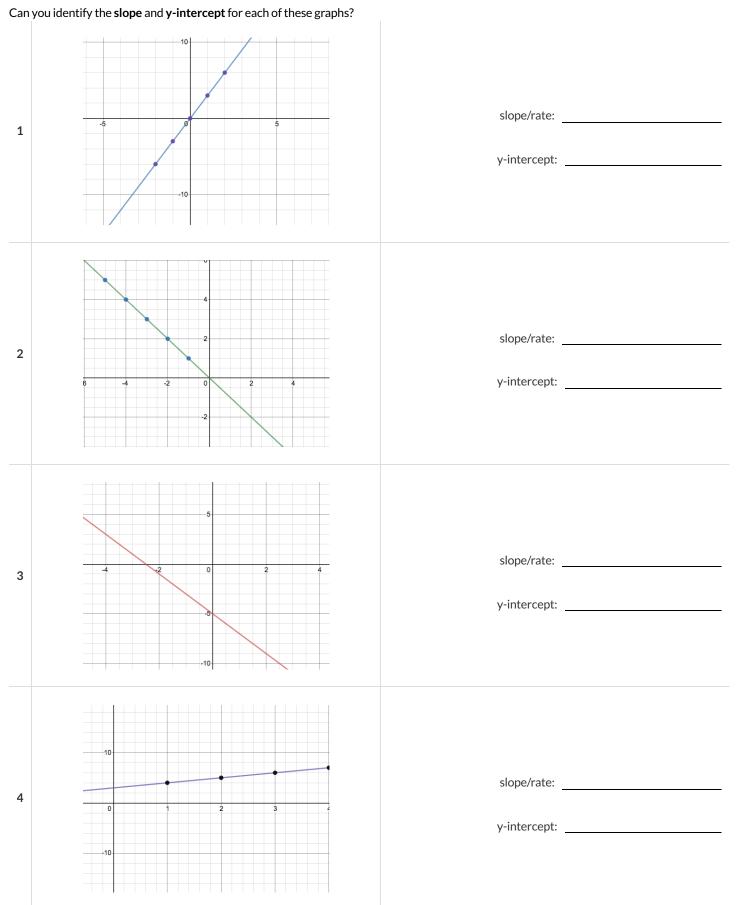
slope/rate:

slope/rate:

slope/rate: _____

slope/rate: _____

Identifying Slope and y-intercept in Graphs



Identifying Slope and y-intercept in Definitions

The following function definitions are written in math notation and in Pyret. Can you identify their slope and y-intercept?

| 1 | $f(x)=\frac{3}{4}x+19$ | slope/rate: y-intercept: |
|---|-------------------------------|-----------------------------|
| 2 | fun c(d): (7.5 * d) + 22 end | slope/rate: y-intercept: |
| 3 | fun g(h): 20 - (16 * h) end | slope/rate: y-intercept: |
| 4 | g(x) = 91 + 4x | slope/rate: y-intercept: |
| 5 | fun i(j): –15 + (1.5 * j) end | slope/rate: y-intercept: |
| 6 | $h(x)=10x-\frac{2}{5}$ | slope/rate: y-intercept: |

Matching Graphs to Function Definitions

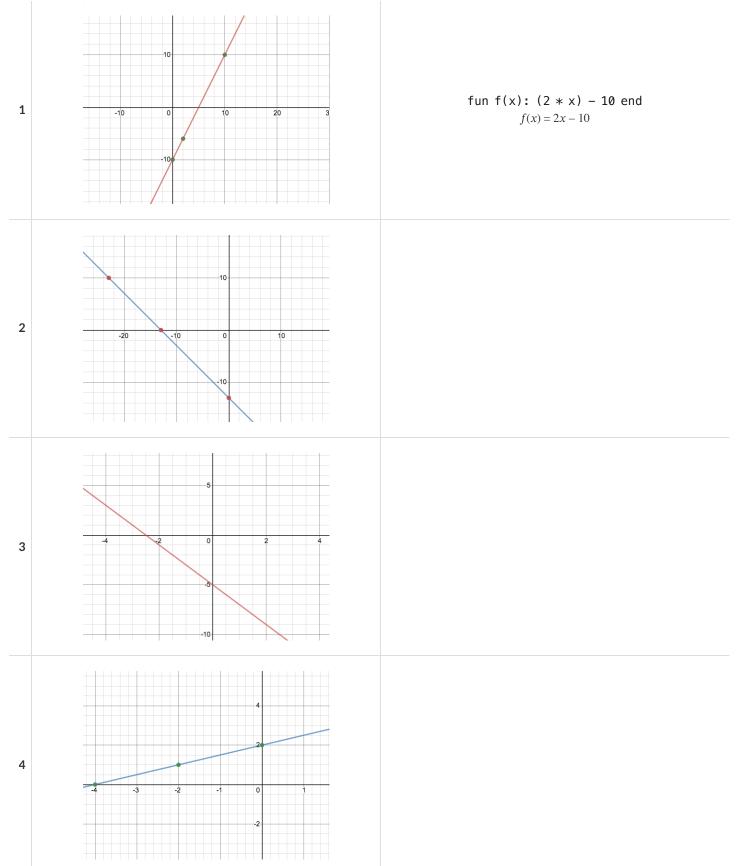
Match the function definitions to the graphs.

-200 -100 fun f(x): (-5 * x) - 10 end 1 Α 100 50 0 g(x) = 0.5x + 2 2 В 0 fun h(x): (2/3 * x) + 4 end 3 С 0 -2 -20 10 i(x) = 6x + -280 **4** D 0 10 -10

-20

Summarizing Graphs with Function Definitions

For each of the Graphs below, write the corresponding function definition, using both Pyret notation *and* function notation. The first one has been done for you.



Matching Tables to Function Definitions

Match each function definition to the corresponding table. **Note:** The tables are shown sideways to save space.

| fun f(x): $(-1 * x)$ end | 1 | А | x | 1 | 2 | 3 | 4 | 5 |
|-----------------------------|---|---|---|-----|----|----|----|----|
| | | | У | 1 | 4 | 9 | 16 | 25 |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| fun $f(x)$: $x + 3$ end | 2 | в | х | 1 | 2 | 3 | 4 | 5 |
| | 2 | В | у | -1 | -2 | -3 | -4 | -5 |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | 3 | С | х | 1 | 2 | 3 | 4 | 5 |
| fun f(x): $3 * x$ end | | | у | 4 | 5 | 6 | 7 | 8 |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| | | D | х | -2 | -1 | 0 | 1 | 2 |
| fun f(x): $(3 * x) - 5$ end | 4 | | y | -11 | -8 | -5 | -2 | 1 |
| | | | , | | 0 | 3 | - | - |
| | | | | | | | | |
| | | | | | | | | |
| | | | | | | | | |
| fun f(x): num-sqr(x) end | 5 | E | x | 1 | 2 | 3 | 4 | 5 |
| | | | У | 3 | 6 | 9 | 12 | 15 |

Summarizing Tables with Function Definitions

For each of the Tables below, define corresponding function using Pyret code and function notation. We've started the first function out for you. (**Note:** The tables have been turned on their sides, to save space!)

| 1 x 0 1 2 3 4 y -2 0 2 4 6 end f(x) = - - - - - 2 x -2 -1 0 1 2 3 x -2 -1 0 1 2 3 x -5 -4 -3 -2 -1 4 x 1 2 3 4 5 y -1 -2 -3 4 -5 y -1 -2 -3 -4 -5 y 14 16 18 20 22 | | | | | | | | |
|--|----------|----|----|------|----|------|----|----------------------|
| 1 y -2 0 2 4 6 end 2 x -2 -1 0 1 2 2 3 x -2 -1 0 1 2 2 4 x 1 2 3 4 5 3 5 x 9 10 11 12 13 | | | | | | | | <pre>fun f(x):</pre> |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | L | х | 0 | 1 | 2 | 3 | 4 | |
| 2 x -2 -1 0 1 2 3 x -2 -1 0 1 2 3 x -5 -4 -3 -2 -1 4 x 1 2 3 1 5 x 9 10 11 12 | | У | -2 | 0 | 2 | 4 | 6 | end |
| 2 y -2 -1 0 1 2 3 x -5 -4 -3 -2 -1 3 x -5 -4 -3 -2 -1 4 x 1 2 3 4 5 y 9 7 5 3 1 | | | | | | | | f(x) = |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | | | | | |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | | | | | |
| y -2 -1 0 1 2 x -5 -4 -3 -2 -1 y 9 7 5 3 1 4 x 1 2 3 4 5 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | , | x | -2 | -1 | 0 | 1 | 2 | |
| 3 y 9 7 5 3 1 4 x 1 2 3 4 5 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | • | у | -2 | -1 | 0 | 1 | 2 | |
| 3 y 9 7 5 3 1 4 x 1 2 3 4 5 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | | | | | | | | |
| 3 y 9 7 5 3 1 4 x 1 2 3 4 5 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | | | | | | | | |
| y 9 7 5 3 1 4 x 1 2 3 4 5 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | | х | -5 | -4 | -3 | -2 | -1 | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 3 | У | 9 | 7 | 5 | 3 | 1 | |
| 4 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | | | | | | | | |
| 4 y -1 -2 -3 -4 -5 5 x 9 10 11 12 13 | | | | | | | | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | х | 1 | 2 | 3 | 4 | 5 | |
| 5 | ł | у | -1 | -2 | -3 | -4 | -5 | |
| 5 | | | | | | | | |
| 5 | | | | | | | | |
| 5 | | х | 9 | 10 | 11 | 12 | 13 | |
| | i | | | | | | | |
| | | | | | | | | |
| | _ | | | | | | | |
| x 20 21 22 23 24 | | ×. | 20 | 21 | 22 | 22 | 24 | |
| 6 | | | | | | | | |
| y 15 15.5 16 16.5 17 | 5 | y | TD | 12.2 | 10 | 10.2 | 1/ | |

Solving Word Problems

Being able to see functions as Contracts, Examples or Definitions is like having three powerful tools. These representations can be used together to solve word problems!

1) When reading a word problem, the first step is to figure out the **Contract** for the function you want to build. Remember, a Contract must include the Name, Domain and Range for the function!

2) Then we write a **Purpose Statement**, which is a short note that tells us what the function *should do*. Professional programmers work hard to write good purpose statements, so that other people can understand the code they wrote! Programmers work on teams; the programs they write must outlast the moment that they are written.

3) Next, we write at least two **Examples**. These are lines of code that show what the function should do for a *specific* input. Once we see examples of at least two inputs, we can *find a pattern* and see which parts are changing and which parts aren't.

4) To finish the Examples, we circle the parts that are changing, and label them with a short variable name that explains what they do.

5) Finally, we **define the function** itself! This is pretty easy after you have some examples to work from: we copy everything that didn't change, and replace the changeable stuff with the variable name!

Matching Word Problems and Purpose Statements

Match each word problem below to its corresponding purpose statement.

Annie got a new dog, Xavier, that eats about 5 times as much as her little dog, Rex, who is 10 years old. She hasn't gotten used to buying enough dogfood for the household yet. Write a function that generates an estimate for how many pounds of food Xavier will eat, given the amount of food that Rex usually consumes in the same amount of time.

A Consume the pounds of food Rex eats and add 5.

Adrienne's raccoon, Rex, eats 5 more pounds of food each week than her pet squirrel, Lili, who is 7 years older. Write a function to determine how much Lili eats in a week, given how much Rex eats.

2

Alejandro's rabbit, Rex, poops about 1/5 of what it eats. His rabbit hutch is 10 cubic feet. Write a function to figure out how much rabbit poop Alejandro will have to clean up depending on how much Rex has eaten.

ო

Max's turtle, Rex, eats 5 pounds less per week than his turtle, Harry, who is 2 inches taller. Write a function to calculate how much food Harry eats, given the weight of Rex's food.

B Consume the pounds of food Rex eats and subtract 5.

C Consume the pounds of food Rex eats and multiply by 5.

Consume the pounds of food Rex eats and divide by 5.

۵

4

Writing Examples from Purpose Statements

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

Contract and Purpose Statement

Every contract has three parts...

| # triple:: function name | | Number Domain | | > | Number Range |
|---|----------------------------|----------------------------|----------------------------|---|-----------------|
| <u># Consumes a Number ar</u> | nd triples it. | | | | _ |
| Examples | | what does the function do? | | | |
| Write some examples, then circ examples: | le and label what changes. | | | | |
| function_name(| input(s) | _) is | what the function produces | | |
| function name | input(s) | _) is | what the function produces | | |

end

| Contract and Purpose Statement | | | | | | | | |
|---|--|--|--|--|--|--|--|--|
| Every contract has three parts | | | | | | | | |
| # upside-down:: Image -: function name Domain | | | | | | | | |
| # Consumes an image, and turns it upside down by rotating it 180 degrees. what does the function do? | | | | | | | | |
| Examples | | | | | | | | |
| Write some examples, then circle and label what changes | | | | | | | | |
| examples: | | | | | | | | |
| () is | | | | | | | | |
| function name input(s) what the function produces | | | | | | | | |
| () is function name input(s) what the function produces end | | | | | | | | |

Fixing Purpose Statements

Beneath each of the word problems below is a purpose statement (generated by ChatGPT!) that is either missing information or includes unnecessary information. Write an improved version of each purpose statement beneath the original, then explain what was wrong with the ChatGPT-generated Purpose Statement.

1) Word Problem: The New York City ferry costs \$2.75 per ride. The Earth School requires two chaperones for any field trip. Write a function fare that takes in the number of students in the class and returns the total fare for the students and chaperones.

ChatGPT's Purpose Statement: Take in the number of students and add 2.

Improved Purpose Statement:

Problem with ChatGPT's Purpose Statement:

2) Word Problem: It is tradition for the Green Machines to go to Humpy Dumpty's for ice cream with their families after their soccer games. Write a function cones to take in the number of kids and calculate the total bill for the team, assuming that each kid brings two family members and cones cost \$1.25.

ChatGPT's Purpose Statement: Take in the number of kids on the team and multiply it by 1.25.

Improved Purpose Statement:

Problem with ChatGPT's Purpose Statement:

3) Word Problem: The cost of renting an ebike is \$3 plus an additional \$0.12 per minute. Write a function ebike that will calculate the cost of a ride, given the number of minutes ridden.

ChatGPT's Purpose Statement: Take in the number of minutes and multiply it by 3.12.

Improved Purpose Statement:

Problem with ChatGPT's Purpose Statement:

4) Word Problem: Suleika is a skilled house painter at only age 21. She has painted hundreds of rooms and can paint about 175 square feet an hour. Write a function paint that takes in the number of square feet of the job and calculates how many hours it will take her.

ChatGPT's Purpose Statement: Take in the number of square feet of walls in a house and divide them by 175 then add 21 years.

Improved Purpose Statement:

Problem with ChatGPT's Purpose Statement: _____

Word Problem: rocket-height

Directions: A rocket blasts off, and is now traveling at a constant velocity of 7 meters per second. Use the Design Recipe to write a function rocket-height, which takes in a number of seconds and calculates the height.

| Contract and Purpose Stater | nent | | | | |
|---|------------------------|---------------------------|----------------------------|----|-------|
| Every contract has three parts. | | | | | |
| #:_ | | | | -> | |
| function name | | Do | main | | Range |
| # | | | | | |
| | | what does the fund | tion do? | | |
| Examples | | | | | |
| Write some examples, then circ examples: | le and label what chan | ges | | | |
| (| |) is | | | |
| function name | input(s) | / .c | what the function produces | | |
| (| |)is | | | |
| function name | input(s) | / 13 | what the function produces | | |
| end | | | | | |
| Definition | | | | | |
| Write the definition, giving vari | able names to all your | input values | | | |
| fun | (| |): | | |
| function name | v | riable(s) | | | |
| | | | | | |
| | , | what the function does wi | th those variable(s) | | · |

end

Danger and Target Movement

Directions: Use the Design Recipe to write a function update-danger, which takes in the danger's x- and y-coordinate and produces the

| next x- | coordinate, which is 50 pixels t | o the left. | | | | | |
|----------------------|--|--------------------|--------------------|--------------------|----------------------------|---|-------|
| Con | tract and Purpose Statement | | | | | | |
| Every | contract has three parts | | | | | | |
| # | function name | | | Domain | | > | Range |
| # | | | | | | | |
| Fxar | nples | | what does t | ne function do? | | | |
| Write exam | some examples, then circle and lles: | label what chang | jes | | | | |
| | function name | input(s) |) is | | what the function produces | | |
| end | function name | input(s) |) is | | what the function produces | | |
| | nition the definition, giving variable n | ames to all your i | nput values | | | | |
| fun _ | function name (| varia | able(s) |): | | | |
| end | | w | hat the function d | oes with those var | iable(s) | | |

Directions: Use the Design Recipe to write a function update-target, which takes in the target's x- and y-coordinate and produces the next x-coordinate, which is 50 pixels to the right.

| Contract and Purpose Statement | | | |
|---|------------------------------|----------------------------|---------|
| Every contract has three parts | | | |
| #:::::: | | Domain | ->Range |
| # | what does th | e function do? | |
| Examples | what does th | | |
| Write some examples, then circle and la examples: | abel what changes | | |
| ((|) is | what the function produces | |
| ((|) is | what the function produces | |
| end Definition | | | |
| Write the definition, giving variable na | mes to all your input values | | |
| fun((| variable(s) |): | |
| | what the function do | pes with those variable(s) | |

Surface Area of a Rectangular Prism - Explore

1) What do you picture in your mind when you hear *rectangular prism*?

2) What do you picture in your mind when you hear surface area?

3) Open the <u>Surface Area of a Rectangular Prism Starter File</u> and click "Run". Type prism into the Interactions Area (on the right) and hit "enter" to see an image of a rectangular prism. What do you notice about the image?

4) How many faces does this prism have? _____

Find PART 1 in the Definitions Area of the starter file (on the left). You will see a definition for front and back .

5) How did the author know to use width and height as the dimensions for front and back?

6) Why are front and back defined to be the same thing?

7) Add definitions for the other faces of the prism, using these definitions as a model, and the image of the prism as a support.

Find PART 2 in the starter file. You'll see faces = [list: front, back,] ... so far the list only includes front and back.

8) Complete the faces list, then type print-imqs(faces) into the Interactions Area. What do you see?

We're going to print the faces following directions in PART 3 and build a paper model of a rectangular prism. Before you print and build your prism, you can change the length, width, and height of your prism at the top of the starter file. Be sure that all 3 dimensions are different, and that they are all small enough to fit on a sheet of paper. If you change them, record your new dimensions here.

| LENGTH: | HEIGHT: |
|---------|---------|
| | |

11) Calculate the surface area of your prism, by adding the area of each face. ______ Show your work below.

12) In PART 4 of the starter file, you wrote code to calculate the surface area. How many definitions did you use?

13) How does the surface area that the computer returns compare to the surface area you calculated by hand?

Problem Decomposition

- Sometimes a problem is too complicated to solve all at once. Maybe there are too many variables, or there is just so much information that we can't get a handle on it!
- We can use **Problem Decomposition** to break those problems down into simpler pieces, and then work with the pieces to solve the whole. There are two strategies we can use for decomposition:
 - **Top-Down** Start with the "big picture", writing functions or equations that describe the connections between parts of the problem. Then, work on defining those parts.
 - **Bottom-Up** Start with the smaller parts, writing functions or equations that describe the parts we understand. Then, connect those parts together to solve the whole problem.
- You may find that one strategy works better for some types of problems than another, so make sure you're comfortable using either one!

Word Problems: revenue, cost

Directions: Use the Design Recipe to write a function revenue, which takes in the number of glasses sold at \$1.75 apiece and calculates the

| total revenue. | | | | | |
|----------------------------------|-----------------------|----------------------|-----------------------|----------------------------|-------|
| Contract and Purpose State | ment | | | | |
| Every contract has three parts | | | | | |
| # :: | | | | | -> |
| function name | | | Domain | | Range |
| # | | | | | |
| | | what does th | e function do? | | |
| Examples | | | | | |
| Write some examples, then cir | cle and label what cl | nanges | | | |
| examples: | | | | | |
| | (|) is | | | |
| function name | input(s) | / 13 | | what the function produces | |
| | (|) is | | | |
| function name | input(s) | / | | what the function produces | |
| end | | | | | |
| Definition | | | | | |
| Write the definition, giving var | iable names to all yo | our input values | | | |
| fun | (| |). | | |
| function name | | variable(s) | /. | | |
| | | | | | |
| | | what the function do | oes with those variat | ble(s) | |
| end | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |

Directions: Use the Design Recipe to write a function cost, which takes in the number of glasses sold and calculates the total cost of materials if each glass costs \$.30 to make.

| Contract and Purpos | Se Statement | | | | | | |
|---------------------------------------|--------------------|--------------------|----------------------|------------------|----------------------------|----|-------|
| Every contract has thre | ee parts | | | | | | |
| # | :: | | | | | -> | |
| function name | | | | Domain | | | Range |
| # | | | | | | | |
| | | | what does the | function do? | | | |
| Examples | | | | | | | |
| Write some examples, examples: | then circle and la | bel what chang | es | | | | |
| | (| |)is | | | | |
| function name | <u>(</u> | input(s) | , | | what the function produces | | |
| | (| |)is | | | | |
| function name | \ | input(s) | / | | what the function produces | | |
| end | | | | | | | |
| Definition | | | | | | | |
| Write the definition, gi | ving variable nan | nes to all your in | nput values | | | | |
| fun | (| | |). | | | |
| function na | me | varia | able(s) | /· | | | |
| | | | | | | | |
| | | w | hat the function doe | s with those var | iable(s) | | |

Word Problem: profit

Directions: Use the Design Recipe to write a function profit that calculates total profit from glasses sold, which is computed by subtracting the total cost from the total revenue.

| Contract and Purpose Statem | ent | | | |
|------------------------------------|-----------------------|---------------------------|----------------------------|-------|
| Every contract has three parts | | | | |
| <u>#:</u> ::::::: | | | | -> |
| function name | | Do | main | Range |
| # | | | | |
| | | what does the fund | ction do? | |
| Examples | | | | |
| Write some examples, then circle | e and label what chan | ges | | |
| examples: | | - | | |
| (| |)is | | |
| function name | input(s) | | what the function produces | |
| (| |) is | | |
| function name | input(s) | | what the function produces | |
| end | | | | |
| Definition | | | | |
| Write the definition, giving varia | ble names to all your | input values | | |
| fun | (| |): | |
| function name | <u>,</u> var | iable(s) | <u>_</u> | |
| | | | | |
| | ٧ | vhat the function does wi | th those variable(s) | |

end

Profit - More than one Way!

Four students defined the same revenue and cost functions, shown below:

fun revenue(g): 1.75 * g end
fun cost(g): 0.3 * g end

However, they came up with four different definitions for profit :

| Khalil: | fun | <pre>profit(g):</pre> | (1.75 * g) - | (0.3 * g) end |
|----------|-----|-----------------------|--------------|------------------------|
| Samaria: | fun | <pre>profit(g):</pre> | (1.75 - 0.3) | * g end |
| Alenka: | fun | <pre>profit(g):</pre> | 1.45 * g end | |
| Fauzi: | fun | <pre>profit(g):</pre> | revenue(g) - | <pre>cost(g) end</pre> |

1) Which of these four definitions do you think is "best", and why?

2) If lemons get more expensive, which definitions of profit need to be changed?

3) If Sally raises her prices, which definitions of profit need to be changed?

4) Which definition of profit is the most flexible? Why?

Top Down or Bottom Up

Jamal's trip requires him to drive 20 mi to the airport, fly 2,300 mi, and then take a bus 6 mi to his hotel. His average speed driving to the airport is 40 mph, the average speed of an airplane is 575 mph, and the average speed of his bus is 15 mph. Aside from time waiting for the plane or bus, how long is Jamal in transit?

| Bear's Strategy: | Lion's Strategy: |
|---|---|
| ${ m Drive Time} = 20 \ { m miles} 	imes rac{1 \ { m hour}}{40 \ { m miles}} = 0.5 \ { m hours}$ | In Transit Time = Drive Time + Fly Time + Bus Time |
| ${ m Fly\ Time}=2300\ { m miles}	imesrac{1\ { m hour}}{575\ { m miles}}=4\ { m hours}$ | ${ m Drive Time} = 20 \; { m miles} 	imes rac{1 \; { m hour}}{40 \; { m miles}} = 0.5 \; { m hours}$ |
| $	ext{Bus Time} = 6 	ext{ miles} 	imes rac{1 	ext{ hour}}{15 	ext{ miles}} = 0.4 	ext{ hours}$ | ${\rm Fly \ Time} = 2300 \ {\rm miles} \times \frac{1 \ {\rm hour}}{575 \ {\rm miles}} = 4 \ {\rm hours}$ |
| $\label{eq:In Transit Time} \mbox{In Transit Time} = \mbox{Drive Time} + \mbox{Fly Time} + \mbox{Bus Time}$ | $	ext{Bus Time} = 6 	ext{ miles} 	imes rac{1 	ext{ hour}}{15 	ext{ miles}} = 0.4 	ext{ hours}$ |
| $0.5 + 4 + 0.4 = 4.9 	ext{ hours}$ | 0.5 + 4 + 0.4 = 4.9 hours |

1) Whose Strategy was Top Down? How do you know?

2) Whose Strategy was Bottom Up? How do you know?

3) Which way of thinking about the problem makes more sense to you?

 What's happening with that Math?!

 When calculating Jamal's drive time, we multiplied distance by speed. More specifically, we multiplied the starting value (20 miles) by

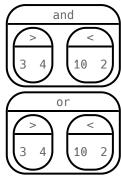
 $\frac{1 \text{ hour}}{40 \text{ miles}}$. Why? Why not reverse it, to use $\frac{40 \text{ miles}}{1 \text{ hour}}$, as stated in the problem?

 Time is the desired outcome. Looking at the units, we can see that speed must have miles as its denominator to *cancel out* the miles in the starting value.

 $\frac{20 \text{ miles}}{1} \times \frac{1 \text{ hour}}{40 \text{ miles}} = \frac{20 \text{ miles} \times 1 \text{ hour}}{40 \text{ miles}} = \frac{20}{40} \text{ hour} = \frac{1}{2} \text{ hour}$

Inequalities

- Sometimes we want to *ask questions* about data. For example, is x greater than y ? Is one string equal to another? These questions can't be answered with **Numbers**. Instead, they are answered with a new data type called a **Boolean**.
- Video games use Booleans for many things: asking when a player's health is equal to zero, whether two characters are close enough to bump into one another, or if a character's coordinates put it off the edge of the screen.
- A Boolean value is either true or false. Unlike Numbers, Strings, and Images, Booleans have only two possible values.
- You already know some functions that produce Booleans, such as < and > ! Our programming language has them, too: 3 < 4, 10 > 2, and -10 == 19.
- We also have ways of writing Compound Inequalities, so we can ask more complicated questions using the and and or functions.
 - (3 > 4) and (10 < 2) translates to "three is greater than four *and* ten is less than two". This will evaluate to false, since the and function requires that both sub-expressions be true.
 - (3 > 4) or (10 < 2), which translates to "three is greater than four or ten is less than two". This will evaluate to true, since the or function only requires that one sub-expression be true.
- The Circles of Evaluation work the same way with Booleans that they do with Numbers, Strings and Images:



Boolean Functions

Make a prediction about what each function in the **Boolean Starter File** does.

| Now, experiment with the functions. Fill in the blanks below so that each of the five functions returns true. |
|---|
| 1) is-odd() |
| 2) is-even() |
| 3) is-less-than-one() |
| <pre>4) is-continent()</pre> |
| 5)is-primary-color() |
| Fill in the blanks below so that each of the five functions returns false. |
| 6) is-odd() |
| 7) is-even() |
| 8) is-less-than-one() |
| 9) is-continent() |
| 10) is-primary-color() |

Simple Inequalities

Each inequality expression in the first column contains a number.

Decide whether or not that number is a solution to the expression and place it in the appropriate column.

Then identify 4 solution values and 4 non-solution values for \times .

- Solutions will make the expression true .
- Non-Solutions will make the expression false.

You can see graphs of the solution sets of these inequalities and test out each of your lists in the <u>Simple Inequalities Starter File</u>. The comments in the starter file will help you learn how it works!

 \star Challenge yourself to use negatives, positives, fractions, decimals, etc. for your imes values.

| | Expression | 4 solutions that evaluate to true | 4 non-solutions that evaluate to false |
|---|------------|--|---|
| а | x > 2 | | |
| b | x <= -2 | | |
| С | x < 3.5 | | |
| d | x >= -1 | | |
| е | x > -4 | | |
| f | x <> 2 | | |

1) For which inequalities was the number from the expression part of the solution?

2) For which inequalities was the number from the expression not part of the solution?

3) For which inequalities were the solutions on the left end of the number line?

4) For which inequalities were the solutions on the right end of the number line?

Converting Circles of Evaluation to Code

Circle of Evaluation Code 9 1 and < < 2 10 10 15 5 or == == 3 "apple" "banana" /um yum $\geq =$ string-length 6 4 "My Game" or and and 5 < < < 5 8 10 Х х

Compound Inequalities – Practice

Create the Circles of Evaluation, then convert the expressions into Code in the space provided.

1) 2 is less than 5, and 0 is equal to 6

What will this evaluate to? _____

2) 6 is greater than 8, or -4 is less than 1

What will this evaluate to? _____

3) The String "purple" is the same as the String "blue", and 3 plus 5 equals 8

What will this evaluate to? _____

4) Write the contracts for and & or in your Contracts page.

Compound Inequality Warmup

1) What are 4 solutions for x > 5?

2) What are 4 non-solutions for x > 5?

3) What are 4 solutions for $x \le 15$?

4) What are 4 non-solutions for $x \le 15$?

5) What 4 numbers are in the solution set of x > 5 and $x \le 15$, making both of these inequalities true?

6) How would that be different from the solution set of x > 5 or $x \le 15$, making at least one of these inequalities true?

Exploring Compound Inequality

This page is designed to accompany <u>Compound Inequalities Starter File</u>. When you click "Run" you will see 4 graphs. The first two are simple inequalities and the second two are compound inequalities.

1) What does and - intersection do?

2) Why is the circle on 5 red and the circle on 15 green?

3) Do you think every graph made with and-intersection will have different color dots at the ends? Why or why not?

4) What does or-union do?

5) Why did the graph of this or-union result in the whole numberline being shaded blue?

6) Not all graphs of or-union will look like this. Can you think of a pair of inequalities whose union won't shade the whole graph?

Change the function definition on *line* 8 to x < 5 and the definition on *line* 9 to $x \ge 15$ and, before you click "Run", take a moment to think about what the new graphs of and-intersection and or-union will look like. Then click "Run" and take a look.

7) What does the new and-intersection graph look like?

8) What does the new or-union graph look like?

9) Why is the dot for 5 red and the dot for 15 green?

10) Which of the 8 numbers from the list are part of the solution set? How do you know?

11) Is 3 part of the solution set? Explain.

12) Is 10 part of the solution set? Explain.

Compound Inequalities: Solutions & Non-Solutions

For each Compound Inequality listed below, identify 4 solutions and 4 non-solutions.

- If there are **no solutions** or the solution set includes **all real numbers**, write that instead of making a list.
- Solutions for *intersections*, which use **and** will make both of the expressions true.
- Solutions for *unions*, which use **or** will make at least one of the expressions true.

Pay special attention to the numbers in the sample expression! Challenge yourself to use negatives, positives, fractions, decimals, etc. for your x values.

The first two have been done for you - Answers will vary!

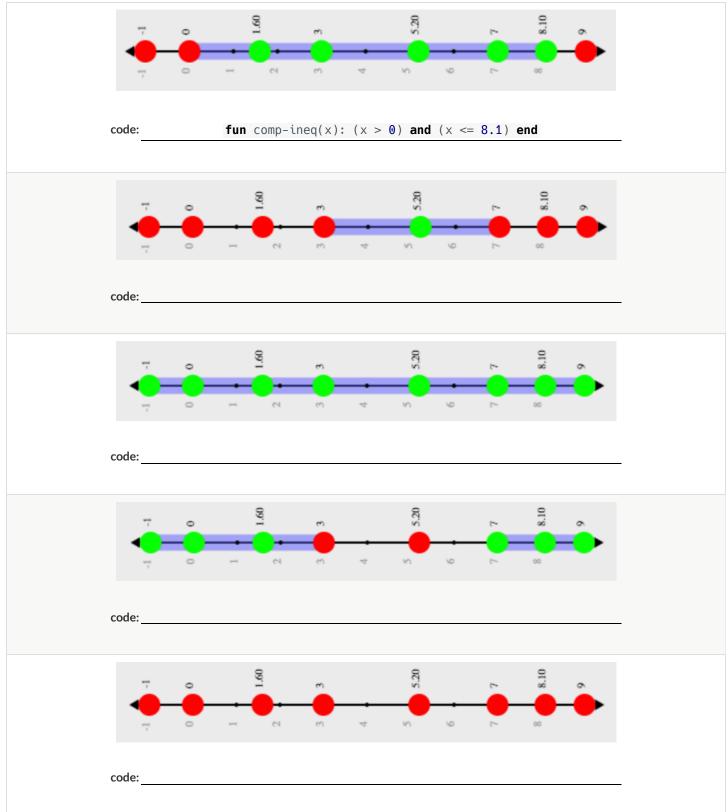
| | Expression | 4 solutions that evaluate to true | 4 non-solutions that evaluate to false |
|---|---------------------------|-----------------------------------|--|
| а | x > 5 and $x < 15$ | 6, 9.5, 12, 14.9 | -2, 5, 15, 16.1 |
| b | x > 5 or x < 15 | All real numbers | No non-solutions |
| с | $x \le -2$ and $x > 7$ | | |
| d | x <= -2 or x > 7 | | |
| е | x < 3.5 and $x > -4$ | | |
| f | x < 3.5 or x > -4 | | |
| g | $x \ge -1$ and $x \ge -5$ | | |
| h | x >= -1 or x > -5 | | |
| i | x < -4 and $x > 2$ | | |

1) Could there ever be a union with no solutions? Explain your thinking.

2) Could there ever be an intersection whose solution is all real numbers? Explain your thinking.

Compound Inequality Functions

Each of the plots below was generated using the code inequality(comp-ineq, [list: -1, 0, 1.6, 3, 5.2, 7, 8.1, 9]). Using the numbers 3 and 7, write the code to define comp-ineq for each plot. Note: The example is defined using 0 and 8.1 rather than 3 and 7.



Sam the Butterfly

Open the <u>Sam the Butterfly Starter File</u> starter file and click "Run". (*Hi, Sam*!) Move Sam around the screen using the arrow keys.

1) What do you Notice about the program?

2) What do you Wonder?

3) What do you see when Sam is at (0,0)? Why is that?

4) What changes as the butterfly moves left and right?

5) Sam is in a 640 × 480 yard. Sam's mom wants Sam to stay in sight. How far to the left and right can Sam go and still remain visible?

Use the new inequality functions to answer the following questions with code:

6) Sam hasn't gone off the left edge of the screen as long as...

7) Sam hasn't gone off the right edge of the screen as long as...

8) Use the space below to draw Circles of Evaluation for these two expressions:

Left and Right

| Directions: Use the Design Recipe to write a function is-safe-left, which takes in an x-coordinate and checks to see if it is gree -50. | eater than |
|--|------------|
| Contract and Purpose Statement | |
| Every contract has three parts | |
| # :> | |
| function name Domain | Range |
| # | |
| what does the function do? | |
| Examples | |
| Write some examples, then circle and label what changes | |
| examples: | |
| () is | |
| function name input(s) what the function produces | |
| () is | |
| function name input(s) what the function produces | |
| end | |
| Definition | |
| Write the definition, giving variable names to all your input values | |
| fun (): | |
| function name variable(s) | |
| | |
| what the function does with those variable(s) | |
| end | |
| | |
| | |
| | |
| | |
| | |

Directions: Use the Design Recipe to write a function is-safe-right, which takes in an x-coordinate and checks to see if it is less than 690.

| Contr | act and Purpose Sta | tement | | | | | |
|----------|-------------------------|----------------------------|---------------------|---------------------|----------------------------|---|-------|
| Every co | ontract has three par | ts | | | | | |
| # | | | | | | > | |
| | function name | | | Domain | | | Range |
| # | | | | | | | |
| | | | what does t | he function do? | | | |
| Exam | ples | | | | | | |
| Write so | ome examples, then o | circle and label what char | iges | | | | |
| example | es: | | | | | | |
| | | , | | | | | |
| | function name | (|) is | | what the function produces | | |
| | | input(s) | | | what the function produces | | |
| | | (|) is | | | | |
| | function name | input(s) | | | what the function produces | | |
| end | | | | | | | |
| Defini | ition | | | | | | |
| Write th | ne definition, giving v | ariable names to all your | input values | | | | |
| fun | | (| |): | | | |
| | function name | vvai | riable(s) | /` | | | |
| | | | | | | | |
| | | | what the function o | loes with those var | riable(s) | | |
| | | | mat the function t | abes with those val | | | |

Word Problem: is-onscreen

Directions: Use the Design Recipe to write a function is-onscreen, which takes in an x- and y-coordinate, and checks to see if Sam is safe on the left while also being safe on the right.

| Contract and Purpose Stateme | ent | | | |
|-------------------------------------|-----------------------|---------------------------|----------------------------|-------|
| Every contract has three parts | | | | |
| # :: | | | | -> |
| function name | | Do | main | Range |
| # | | | | |
| | | what does the fund | ction do? | |
| Examples | | | | |
| Write some examples, then circle | and label what chan | ges | | |
| examples: | | 0 | | |
| (| |) is | | |
| function name | input(s) | | what the function produces | |
| (| |) is | | |
| function name | input(s) | / 13 | what the function produces | |
| end | | | | |
| Definition | | | | |
| Write the definition, giving varial | ole names to all your | input values | | |
| fun | (| |): | |
| function name | var | iable(s) | — | |
| | | | | |
| | ١ | what the function does wi | th those variable(s) | |

end

Piecewise Functions

- Sometimes we want to build functions that act differently for different inputs. For example, suppose a business charges \$10/pizza, but only \$5 for orders of six or more. How could we write a function that computes the total price based on the number of pizzas?
- In math, **Piecewise Functions** are functions that can behave one way for part of their Domain, and another way for a different part. In our pizza example, our function would act like cost(pizzas) = 10 * pizzas for anywhere from 1-5 pizzas. But after 5, it acts like cost(pizzas) = 5 * pizzas.
- Piecewise functions are divided into "pieces". Each piece is divided into two parts:
 1. How the function should behave

2. The domain where it behaves that way

• Our programming language can be used to write piecewise functions, too! Just as in math, each piece has two parts:

```
fun cost(pizzas):
    if pizzas < 6: 10 * pizzas
    else if pizzas >= 6: 5 * pizzas
    end
end
```

Piecewise functions are powerful, and let us solve more complex problems. We can use piecewise functions in a video game to add or subtract from a character's x-coordinate, moving it left or right depending on which key was pressed.

Red Shape - Explore

1) Open the <u>Red Shape Starter File</u>, and read through the code you find there. This code contains new programming that you haven't seen yet! Take a moment to list everything you Notice, and then everything you Wonder...

| Notice | Wonder |
|--------|--------|
| | |
| | |
| | |
| | |
| | |
| | |
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| | |
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| | |
| | |
| | |
| | |
| | |

2) What happens if you click "Run" and type red-shape("ellipse")?

3) Add another example for "triangle".

4) Add another line of code to the definition, to define what the function should do with the input "triangle".

5) Come up with some new shapes, and add them to the code. Make sure you include examples or you will get an error message!

6) In your own words, describe how *piecewise functions* work in this programming environment.

Word Problem: red-shape

Directions: A friend loves red shapes so we've decided to write a program that makes it easy to generate them. Write a function called red-shape which takes in the name of a shape and makes a 20-pixel, solid, red image of the shape.

| Contract and Purpose Statement | | |
|--|---|----------------|
| Every contract has three parts | | |
| # red-shape:: String function name Domain | > | Image Range |
| # Given a shape name, produce a solid, red, 20-pixel image of the shape. what does the function do? | | |
| Examples | | |
| Write some examples, then circle and label what changes examples: | | |
| <u>red-shape(</u> "circle") is <u>circle(20, "solid", "red")</u> function name input(s) what the function produces | | |
| <u>red-shape(</u> "triangle") is <u>triangle(20, "solid", "red")</u> function name input(s) what the function produces | | |
| <u>red-shape("rectangle")</u> is <u>rectangle(20, 20, "solid", "red")</u> function name input(s) what the function produces | | |
| <u>red-shape(</u> "star") is <u>star(20, "solid", "red")</u> function name input(s) what the function produces | | |
| end | | |
| Definition Write the definition, giving variable names to all your input values | | |
| write the definition, giving variable names to all your input values | | |
| fun(): | | |
| if | | |
| else if | | _ |
| else if | | _ |
| else if | | |
| else: | | _ |
| end end | | |

Word Problem: update-player

Directions: The player moves up and down by 20 pixels each time. Write a function called update-player, which takes in the player's x- and y-coordinate and the name of the key pressed ("up" or "down"), and returns the new y-coordinate.

| Contract and Purpose Statement | | |
|---|--|---------|
| Every contract has three parts | | |
| #:;;;;;; | Domain | ->Range |
| # | | |
| | what does the function do? | |
| Examples | | |
| Write some examples, then circle and label what changes. examples: | | |
| update-plaver(100, 200, "up") is | | |
| <u>update-player(100, 200, "up"</u>) is function name input(s) | what the function produces | |
| (|) is | |
| function name input(s) | | |
| (|) is | |
| function name input(s) | _) is what the function produces | |
| (|) is | |
| function name input(s) | what the function produces | |
| end | | |
| Definition | | |
| Write the definition, giving variable names to all your input | it values | |
| fun (|): | |
| function name variable | (s) / | |
| | | |
| what | the function does with those variable(s) | |
| | | |
| what | the function does with those variable(s) | |
| what | the function does with those variable(s) | |
| | | |
| what | the function does with those variable(s) | |

end

Challenges for update-player

For each of the challenges below, see if you can come up with two EXAMPLEs of how it should work!

| 1) Warping - Program one key to "warp" the player to a set location, such as the center of the screen. | | |
|--|--|--|
| examples: | | |
| update-player(,,) is | | |
| update-player(,,) is end | | |
| | | |
| 2) Boundaries - Change update-player such that PLAYER cannot move off the top or bottom of the screen. | | |
| examples: | | |
| update-player(,,) is | | |
| update-player(,,) is) | | |
| end | | |
| | | |
| 3) Wrapping - Add code to update-player such that when PLAYER moves to the top of the screen, it reappears at the bottom, and vice | | |
| versa. | | |
| examples: | | |
| update-player(,,) is | | |

| update-player(| |
|----------------|--|
| end | |

4) Hiding - Add a key that will make PLAYER seem to disappear, and reappear when the same key is pressed again.

examples:

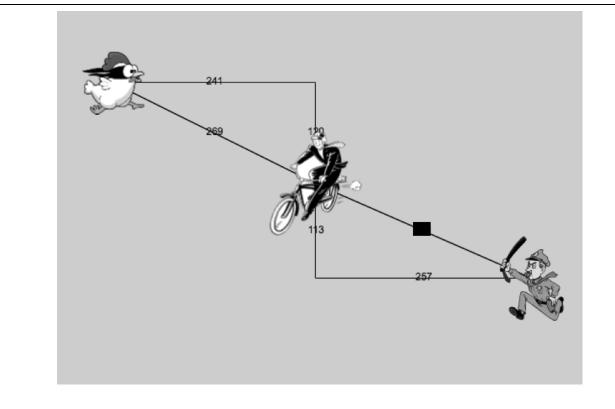
| update-player(| 2 | |) | is |
|----------------|---|---|---|----|
| update-player(| , | , |) | is |

) is

Writing Code to Calculate Missing Lengths

In each of the game screenshots below, one of the distance labels has been hidden. Write the code to generate the missing distance on the line below each image. *Hint: Remember the Pythagorean Theorem*!

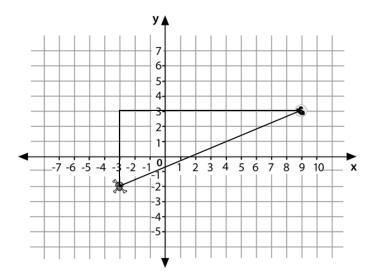




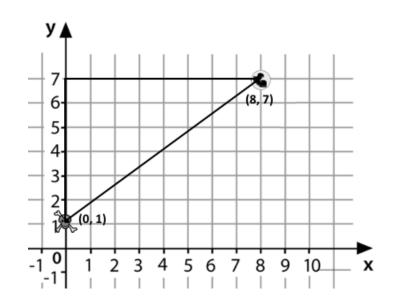
Distance on the Coordinate Plane

Distance between the pyret and the boot:

num-sqrt(num-sqr(line-length(9, -3)) + num-sqr(line-length(3, -2)))



Explain how the code works.



Now write the code to find the distance between this boot and pyret.

Circles of Evaluation: Distance between (0, 2) and (4, 5)

The distance between x_1 and x_2 is computed by line-length(x2, x1). The distance between y_2 and y_1 is computed by line-length(y2, y1). Below is the equation to compute the hypotenuse of a right triangle with legs the lengths of those distances:

$\sqrt{\text{line-length}(x_2, x_1)^2 + \text{line-length}(y_2, y_1)^2}$

Suppose your player is at (0, 2) and a character is at (4, 5). What is the distance between them? 1. Identify the values of x_1 , y_1 , x_2 , and y_2

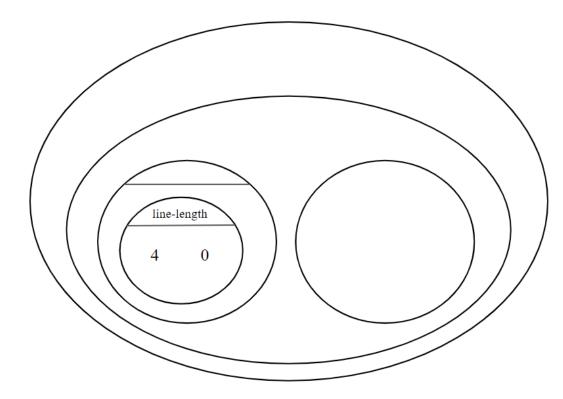
| У1 | <i>x</i> ₂ | У2 |
|------------------------|------------------------|------------------------|
| (y-value of 1st point) | (x-value of 2nd point) | (y-value of 2nd point) |
| | | |
| | (y-value of 1st point) | v 1 |

The equation to compute the distance between these points is:

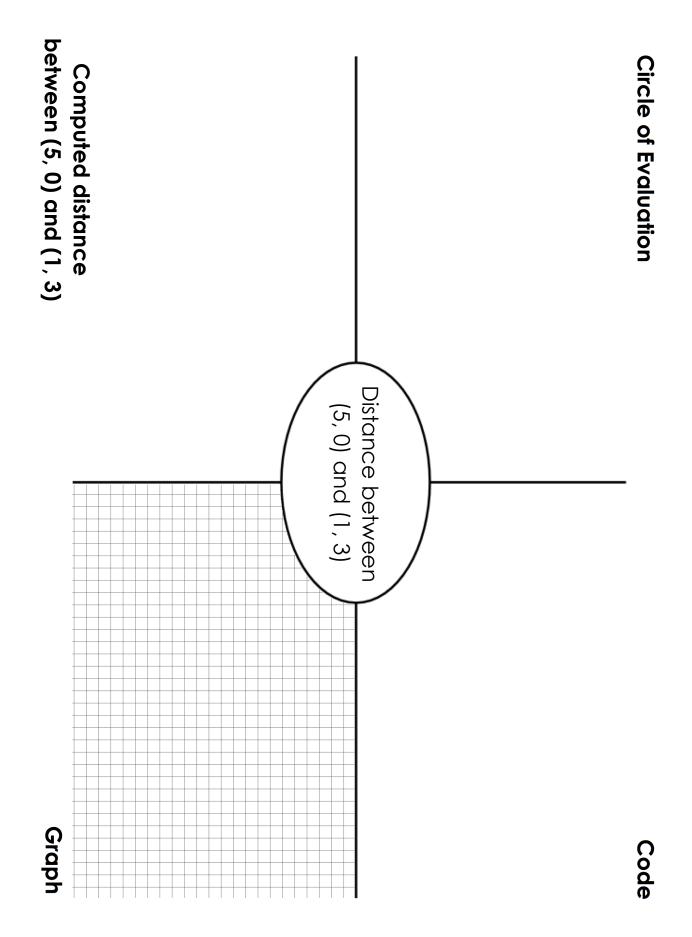
$\sqrt{\text{line-length}(4,0)^2 + \text{line-length}(5,2)^2}$

2. Translate the expression above, for (0,2) and (4,5) into a Circle of Evaluation below.

Hint: In our programming language num-sqr is used for x^2 and num-sqrt is used for \sqrt{x}

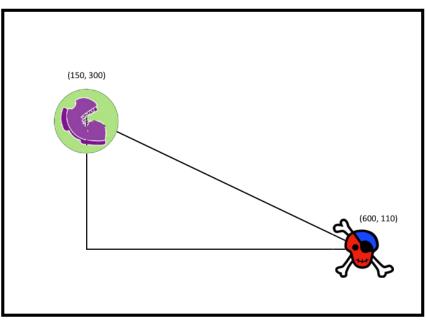


3. Convert the Circle of Evaluation to Code below.

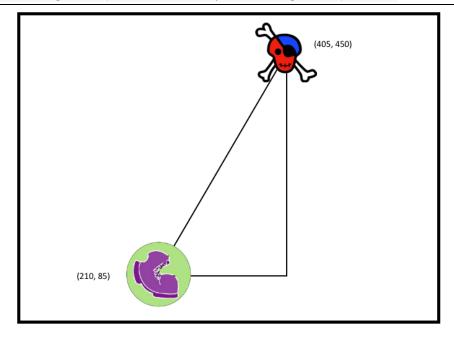


Distance From Game Coordinates

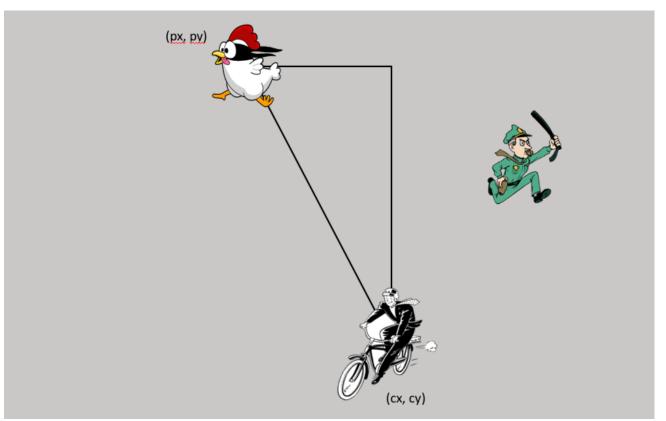
For each of the game screenshots, write the code to calculate the distance between the indicated characters. The first one has been done for you.



num-sqrt(num-sqr(line-length(600, 150)) + num-sqr(line-length(110, 300)))



Distance (px, py) to (cx, cy)

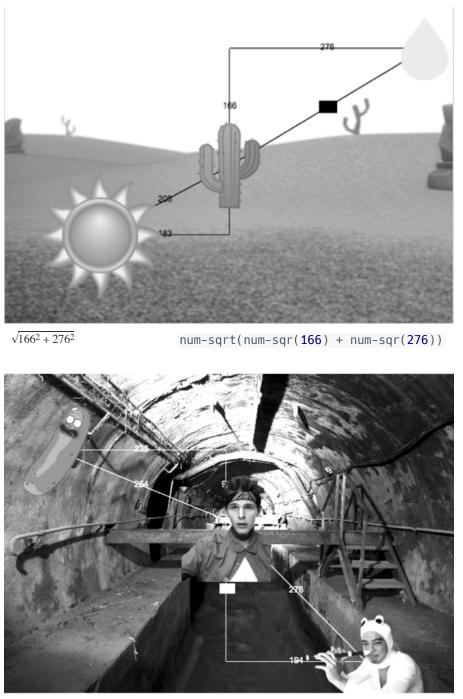


Directions: Use the Design Recipe to write a function distance, which takes in FOUR inputs: px and py (the x- and y-coordinate of the Player) and cx and cy (the x- and y-coordinates of another character), and produces the distance between them in pixels.

| Contract and Purpose Staten | nent | | | | | |
|------------------------------------|---------------------------|-------------------------|------------------------|-------------------------|---|-------|
| Every contract has three parts | | | | | | |
| <u>#:</u> | | | | | > | |
| function name | | D | Domain | | | Range |
| # | | | | | | |
| | | what does the fu | nction do? | | | |
| Examples | | | | | | |
| Write some examples, then circ | le and label what change | es | | | | |
| examples: | | | | | | |
| (| |) is | | | | |
| function name | input(s) | | wha | t the function produces | | |
| (| |)is | | | | |
| function name | input(s) | , * | wha | t the function produces | | |
| end | | | | | | |
| Definition | | | | | | |
| Write the definition, giving varia | able names to all your in | put values | | | | |
| fun | (| |): | | | |
| function name | varia | ble(s) | | | | |
| | | | | | | |
| | wh | nat the function does w | with those variable(s) | | | |
| end | | | | | | |

Comparing Code: Finding Missing Distances

For each of the game screenshots below, the math and the code for computing the covered distance is shown. Notice what is similar and what is different about how the top and bottom distances are calculated. Think about why those similarities and differences exist and record your thinking.

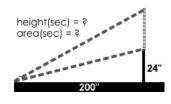


num-sqrt(num-sqr(276) - num-sqr(194))

 $\sqrt{276^2 - 194^2}$

Top Down / Bottom Up

A retractable flag pole starts out 24 inches tall, and grows taller at a rate of 0.6in/sec. An elastic is anchored 200 inches from the base and attached to the top of the pole, forming a right triangle. Using a top-down or bottom-up strategy, define functions that compute the *height* of the pole and the *area* of the triangle after a given number of seconds.



| # | : | | | | -: | > |
|-------|---------------|----------|-------------------|-----------------------------|-----------------|-------|
| | function name | | | Domain | | Range |
| # | | | | | | |
| | | | what does | the function do? | | |
| exam | ples: | | | | | |
| | | (|) is | | | |
| | function name | input(s) | | what the fur | nction produces | |
| | | (|) is | | | |
| _ | function name | input(s) | | what the fur | nction produces | |
| end | | | | | | |
| fun _ | | (| |): | | |
| | function name | vari | able(s) | | | |
| | | | that the function | doog with those warishin(a) | | |
| | | w. | hat the function | does with those variable(s) | | |
| end | | | | | | |
| | | | | | | |

| # | | | | | | > |
|------|---------------|----------|---------------------|--------------------|----------------------------|-------|
| | function name | | | Domain | | Range |
| # | | | | | | |
| | | | what does t | the function do? | | |
| exam | ples: | | | | | |
| | | (|) is | | | |
| | function name | input(s) | | | what the function produces | |
| | | (|) is | | | |
| | function name | input(s) | | | what the function produces | |
| end | | | | | | |
| fun | | (| |): | | |
| | function name | vari | able(s) | | | |
| | | | | | | |
| | | W | hat the function of | does with those va | riable(s) | |
| end | | | | | | |

Word Problem: is-collision

Directions: Use the Design Recipe to write a function is-collision, which takes in FOUR inputs: px and py (the x- and y-coordinate of the Player) and cx and cy (the x- and y-coordinates of another character), and checks if they are close enough to collide.

| Contract and | d Purpose Statemen | t | | | |
|-----------------|-------------------------|--------------------|--------------------------|---------------------------|-------|
| Every contract | has three parts | | | | |
| # | | | | | -> |
| function | n name | | Do | omain | Range |
| # | | | | | |
| | | | what does the fun | ction do? | |
| Examples | | | | | |
| Write some exa | amples, then circle a | nd label what chan | ges | | |
| examples: | 1 / | | 0 | | |
| | 1 | |)is | | |
| functi | ion name | input(s) | / 13 | what the function produce | 25 |
| | (| |)is | | |
| functi | ion name | input(s) | , | what the function produce | 25 |
| end | | | | | |
| Definition | | | | | |
| Write the defir | nition, giving variable | names to all your | input values | | |
| fun | (| | |). | |
| | nction name | var | iable(s) | <u>_</u> . | |
| | | | | | |
| | | ١ | what the function does w | ith those variable(s) | |

end

Contracts for Algebra (Pyret)

Contracts tell us how to use a function, by telling us three important things:

1. The Name

- 2. The Domain of the function what kinds of inputs do we need to give the function, and how many?
- 3. The Range of the function what kind of output will the function give us back?

For example: The contract triangle :: (Number, String, String) -> Image tells us that the name of the function is triangle, it needs three inputs (a Number and two Strings), and it produces an Image.

With these three pieces of information, we know that typing triangle(20, "solid", "green") will evaluate to an Image.

| Name | Domain | | Range |
|--|---|----|--------|
| # above :: | (<u>Image</u> , <u>Image</u>) above below | -> | Image |
| above(circle(10, "solid", " | 'black"), square(50, "solid", "red")) | | |
| # beside :: | (<u>Image</u> , <u>Image</u>) left right | -> | Image |
| <pre>beside(circle(10, "solid",</pre> | "black"), square(50, "solid", "red")) | | |
| # circle :: | (<u>Number</u> , <u>String</u> , <u>String</u>) radius fill-style color | -> | Image |
| circle(50, "solid", "purple | 2") | | |
| # ellipse :: | (<u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) width height fill-style color | -> | Image |
| ellipse(100, 50, "outline", | , "orange") | | |
| # flip-horizontal :: | (Image) | -> | Image |
| flip-horizontal(text("Lion" | ', 50, "maroon")) | | |
| # flip-vertical :: | (<u>Image</u>) | -> | Image |
| <pre>flip-vertical(text("Orion",</pre> | 65, "teal")) | | |
| # image-url :: | (<u>String</u>) url | -> | Image |
| image-url("https://bootstra | apworld.org/images/icon.png") | | |
| <pre># isosceles-triangle ::</pre> | (<u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) size vertex-angle fill-style color | -> | Image |
| isosceles-triangle(50, 20, | "solid", "grey") | | |
| <pre># num-expt ::</pre> | (<u>Number</u> , <u>Number</u>) base power | -> | Number |
| <pre>num-expt(3, 4) # three to t</pre> | the fourth power | | |
| #num-sqr :: | (<u>Number</u>) | -> | Number |
| num-sqr(4) | | | |
| # num-sqrt :: | (<u>Number</u>) | -> | Number |
| num-sqrt(4) | | | |

| Range | | ame Domain |
|---------|----|---|
| Image | -> | overlay :: (<u>Image</u> , <u>Image</u>) top bottom |
| | | overlay(circle(10, "solid", "black"), square(50, "solid", "red")) |
| Image | -> | put-image :: (<u>Image</u> , <u>Number</u> , <u>Number</u> , <u>Image</u>) ront x-coordinate y-coordinate behind |
| | | <pre>put-image(circle(10, "solid", "black"), 10, 10, square(50, "solid", "red"))</pre> |
| Image | -> | radial-star :: (<u>Num</u> , <u>Num</u> , <u>Num</u> , <u>Str</u> , <u>Str</u>) |
| | | radial-star(6, 20, 50, "solid", "red") |
| Image | -> | rectangle :: (<u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) width height fill-style color |
| | | rectangle(100, 50, "outline", "green") |
| Image | -> | regular-polygon :: (<u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) |
| - | | regular-polygon(25,5, "solid", "purple") |
| Image | -> | rhombus (Number , Number , String , String) |
| | | <pre>rhombus(60, 90, "outline", "pink")</pre> |
| Image | -> | |
| Tillaye | | <pre>right-triangle :: (<u>Number</u>, <u>Number</u>, <u>String</u>, <u>String</u>) right-triangle(50, 60, "outline", "blue")</pre> |
| Trees | | |
| Image | -> | degrees img |
| - | | <pre>rotate(45, star(50, "solid", "dark-blue")) scale (Number , Image)</pre> |
| Image | -> | factor img |
| | | <pre>scale(1/2, star(50, "solid", "light-blue"))</pre> |
| Image | -> | square :: (<u>Number</u> , <u>String</u> , <u>String</u>) size fill-style color |
| | | square(50, "solid", "red") |
| Image | -> | star :: (<u>Number</u> , <u>String</u> , <u>String</u>) radius fill-style color |
| | | star(50, "solid", "red") |
| Image | -> | star-polygon :: (<u>Number</u> , <u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) size |
| | | <pre>star-polygon(100, 10, 3 ,"outline", "red")</pre> |
| Boolean | -> | string-contains :: (<u>String</u> , <u>String</u>) haystack, needle |
| | | <pre>string-contains("hotdog", "dog")</pre> |
| Number | -> | string-length :: (<u>String</u>) |
| | | string-length("rainbow") |
| Table | -> | sum :: (<u>Table</u> , <u>String</u>) table-name column |
| | -> | <pre>sum :: (<u>lable</u>, <u>String</u>) sum(animals-table, "pounds")</pre> |

| Name | | Domain | | Range |
|---------------------------|----------|---|----|-------|
| # text | :: | (<u>String</u> , <u>Number</u> , <u>String</u>) message size color | -> | Image |
| text("Zari", 85, " | orange") | | | |
| <pre># triangle</pre> | | (<u>Number</u> , <u>String</u> , <u>String</u>) size fill-style color | -> | Image |
| triangle(50, "soli | d", "fuc | hsia") | | |
| <pre># triangle-asa</pre> | :: | (<u>Number</u> , <u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) top-left-angle, left-side | -> | Image |
| triangle-asa(90, 2 | 00, 10, | "solid", "purple") | | |
| <pre># triangle-sas</pre> | :: | (<u>Number</u> , <u>Number</u> , <u>Number</u> , <u>String</u> , <u>String</u>) top-side , <u>Number</u> , <u>String</u> , <u>String</u>) | -> | Image |
| triangle-sas(50, 2 | 0,70,' | outline", "dark-green") | | |

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